Problem 1  Write the best title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```c++
int main() {
    int a[] = {10, 20, 30};
    double x;
    string b = "thing1", c = "thing2";

    // set x to be the average of a[0], a[1] and a[2]
    x = average(a[0], a[1], a[2]); // (a)
    cout << x << endl;
    // print the average to screen
    average(a, 3); // (b)
    // print to screen: The strings are thing1 and thing2
    cout << "The strings are " << whatStrings(b, c) << endl; // (c)
    if (mystery(mystery(function()))) // (d)
        cout << mystery(function()) << endl; // (e)
    return 0;
}
```

(a) Title line for `average` as called at the line marked (a).
Answer: double average(int a, int b, int c)
(b) Title line for `average` as called at the line marked (b).
Answer: void average(int a[], int c)
(c) Title line for `whatStrings` as called at the line marked (c).
Answer: string whatStrings(string a, string b)
(d) Title line for `function` as called at the line marked (d).
Answer: bool function()
(e) Title line for `mystery` as called at the line marked (e).
Answer: bool mystery(bool b)

Problem 2  Consider the following C++ program.

```c++
int main() {
    cout << words[3].substr(2) << endl; // line (a)
    words[3].replace(1,2,"8");
    cout << words[3] << endl; // line (b)
    cout << words[2][2] << endl; // line (c)
    cout << words[1].rfind("1") << endl; // line (d)
    for (int i = 1; i <= 2; i++) cout << words[i].substr(1,i); // line (e)
    cout << endl;
    return 0;
}
```

(a) What is the output at line (a)?
Answer:
19

(b) What is the output at line (b)?
Answer:
289
(c) What is the output at line (c)?

Answer:

\[ y \]

(d) What is the output at line (d)?

Answer:

\[ 2 \]

(e) What is the output at line (e)?

Answer:

\[ 1\text{ay} \]

Problem 3

Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function that is written only in the designated answer space.

```c
int main() {
    double x = 1.0, y = -0.5;
    int a[5] = {81, 3, 4, 1024, 0};
    // (a) Return true if both parameters are positive. Here NOT is printed.
    if (!bothPositive(x, y)) cout << "NOT" << endl;
    // (b) Swap the parameters if the 2nd is larger. Here 43 is printed.
    makeDecrease(a[1], a[2]); cout << a[1] << a[2] << endl;
    // (c) Return true if array contains a 0 entry. Here YES is printed.
    if (hasZero(a, 5)) cout << "YES\n";
    // (d) Return minimum number of coins to make given amount in change. Here 5.
    cout << numberCoins(a[0]) << endl;
    // (e) Returns the number of digits in a positive parameter. Here 4 is printed.
    cout << numberDigits(a[3]) << endl;
    return 0;
}
```

Answer:

(a)

```c
bool bothPositive(double x, double y) {
    return x > 0 && y > 0;
}
```

(b)

```c
void makeDecrease(int &x, int &y) {
    if (x < y) {
        double temp = x;
        x = y;
        y = temp;
    }
}
```

(c)
bool hasZero(int x[], int capacity) {
    for (int i = 0; i < capacity; i++)
        if (x[i] == 0) return true;
    return false;
}

int numberCoins(int amount) {
    int ans = amount / 25;
    amount = amount % 25;
    ans += amount / 10;
    amount = amount % 10;
    return ans + amount / 5 + amount % 5;
}

int numberDigits(int x) {
    if (x < 10) return 1;
    return 1 + numberDigits(x / 10);
}

Problem 4 Write a function called maximumGap that finds the maximum difference between corresponding entries in two arrays (that have the same capacity). There are 3 parameters, the 2 arrays and their capacity. If the arrays store 9, 0, 3 and 4, 7, 6 the maximum gap is 7 (between the second elements of the two arrays).

Excessively long solutions that use more than 8 lines of code may lose points. A program that uses the function maximumGap follows.

```c
int main() {
    int pi[8] = {3, 1, 4, 1, 5, 9, 2, 6};
    int e[8] = {2, 7, 1, 8, 2, 8, 1, 8};

    cout << maximumGap(pi, e, 8) << endl; // prints 7 the gap between 1 and 8
    return 0;
}
```

Answer:

```c
int maximumGap(int a[], int b[], int c) {
    int gap = 0;
    for (int i = 0; i < c; i++) {
        if (a[i] - b[i] > gap) gap = a[i] - b[i];
        if (b[i] - a[i] > gap) gap = b[i] - a[i];
    }
    return gap;
}
```
Problem 5  Write a function called maskDigits that takes a positive integer parameter and returns a string of * symbols with one * for each digit. For example, if the parameter is 19683 the function will return. *****. Your function can return any convenient value if it is given illegal input.

Excessively long solutions that use more than 6 lines of code may lose points. A program that uses the function maskDigits follows.

```cpp
int main() {
    cout << maskDigits(19683) << endl;  // prints *****
    cout << maskDigits(19) << endl; // prints **
    cout << maskDigits(1) << endl; // prints *
    return 0;
}
```

Answer:

```cpp
string maskDigits(int a) {
    if (a <= 0) return "";
    return "*" + maskDigits(a / 10);
}
```

Problem 6  Write a program that reads 100 single digit numbers from the user. It then prints them as in a square with 10 columns so that the first 10 numbers occupy the first column, the next 10 occupy the next column and so on.

Excessively long solutions that use more than 15 lines of code may lose points.

Answer:

```cpp
int main() {
    int x[10][10];
    cout << "Enter 100 digits: ";
    for (int c = 0; c < 10; c++)
        for (int r = 0; r < 10; r++) cin >> x[r][c];

    for (int r = 0; r < 10; r++) {
        for (int c = 0; c < 10; c++)
            cout << x[r][c] << " ";
        cout << endl;
    }
    return 0;
}
```

Problem 7  Write the best title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    int nn = 5, num[3] = {0, 1, 2};
    double rl[3] = {1.9, 2.3, 3.0};
    char ch = 'b';

    nn = add(ch, 1);  // (a)
    printProduct(num[2], rl[1]);  // (b)
    if (qn(rl, 3)) cout << "Yes\n";  // (c)
    d(nn, 2);  // (d)
    e(d(nn, rl[1]), e('n', e('b', rl[2])));  // (e)
    return 0;
}
```
Problem 8 Consider the following C++ program.

```cpp
void a(int &x, int y) {
    x = y;
    y = x + 1;
}

int b(int &x, int y) {
    y = x + 1;
    x = y;
    return y;
}

void c(int x[], int y) {
    if (y < 1) return;
    cout << x[y - 1] - y;
    c(x, y - 1);
}

int main() {
    int x[6] = {1, 2, 3, 4, 5, 6};
    int y[3] = {5, 4, 3};
    cout << y[x[1]] % x[y[1]] << endl; // line (a)
    a(x[0], x[1]);
    cout << x[0] << x[1] << endl; // line (b)
    cout << b(x[2], x[3]) << endl; // line (c)
    c(y, 3); cout << endl; // line (e)
}
```

(a) What is the output at line (a)?
Answer: 3

(b) What is the output at line (b)?
Answer: 22

(c) What is the output at line (c)?
Answer: 4
Problem 9  Write a program that reads a positive integer n from the user. If the user gives a non-positive value for n the program should terminate immediately. Otherwise, the program should print a triangle with n rows that looks like the following sample when n is 4.

```
  *
 ** *
*** *
```

The triangle should be made with * and blank symbols with one extra * per row. The *s should be separated by blanks and the picture should be symmetric about a vertical line through its middle.

Excessively long solutions that use more than 20 lines of code may lose points.

**Answer:**

```cpp
int main() {
    int n;
    cout << "Enter a non-negative number n: ";
    cin >> n;
    if (n <= 0) return 0;

    for (int r = 0; r < n; r++) {
        for (int c = -(n - 1); c <= n - 1; c++)
            if (c < -r || c > r || (c + r) % 2 != 0) cout << " ";
            else cout << "*";
        cout << endl;
    }
    return 0;
}
```

Alternative solution:

```cpp
void triangle(int n, int indent) {
    if (n == 0) return;
    triangle(n - 1, indent + 1);
    for (int c = 1; c <= indent; c++) cout << " ";
    for (int c = 1; c <= n; c++) cout << "* ";
    cout << endl;
}

int main() {
    int n;
    cout << "Enter a non-negative number n: ";
    cin >> n;
    if (n <= 0) return 0;
    triangle(n, 0);
    return 0;
}
```
Problem 10  The recursive function removeFirst removes the first digit of a positive integer. It is applied in another recursive function middle that returns the middle digit (or middle two digits) of a positive integer none of whose digits are 0. For example the middle of 12345 is 3 but the middle of 1234 is 23.

Implementations of these functions with parts of the code covered up are given below. There is also a main program that uses them.

Some pieces of code have been replaced by PART (a), PART (b), and so on. To answer the 5 parts of this question you should supply the C++ code that was replaced. Each answer must fit on a single line.

```cpp
int removeFirst(PART (a)) {
    if (PART (b))
        return 0;
    PART (c)
}

int middle(int x) {
    if (PART (d))
        return x;
    PART (e)
}

int main() {
    cout << middle(19683) << endl; // prints 6
    cout << middle(1968) << endl; // prints 96
    return 0;
}

(a) Give a replacement for PART (a) to declare the parameter x
Answer: PART (a) is int x
(b) Give a replacement for PART (b) to test for the base case of recursion:
Answer: PART (b) is x < 10
(c) Give a replacement for PART (c) as a useful recursive call:
Answer: PART (c) is return 10 * removeFirst(x / 10) + x % 10;
(d) Give a replacement for PART (d) to test for the base case of recursion:
Answer: PART (d) is x < 100
(e) Give a replacement for PART (e) as a useful recursive call:
Answer: PART (e) is return middle(removeFirst(x) / 10);
```

Problem 11  Write a function called peaks that counts the number of elements in an array that are larger than both of their neighbors. (The first and last elements do not have 2 neighbors and are not to be counted.)

Excessively long solutions that use more than 8 lines of code may lose points. A program that uses the function peaks follows.

```cpp
int main() {
    int x[8] = {3,1,4,1,5,9,2,6};
    cout << peaks(x, 8) << endl; // prints 2 since the elements 4 and 9 are counted
    return 0;
}

Answer:

int peaks(int a[], int c) {
```

Answer:
```cpp
int ans = 0;
for (int i = 1; i < c - 1; i++)
    if (a[i] > a[i - 1] & a[i] > a[i + 1]) ans++;
return ans;
}

Problem 12
Write a function called sizes that has a single parameter that is an integer greater than 99. It returns the integer obtained by changing each of the first 3 digits of the parameter to 6. Your function can return any result of your choice if it is given an illegal parameter value. Excessively long solutions that use more than 8 lines of code may lose points. A program that uses the function sizes follows.

```cpp
int main() {
    cout << sixes(6789) << endl; // prints 6669
    cout << sixes(123) << endl; // prints 666
    cout << sixes(12345) << endl; // prints 66645
    return 0;
}
```

Answer:

```cpp
int sixes(int x) {
    if (x < 1000) return 666;
    return 10 * sixes(x / 10) + x % 10;
}
```

Problem 13
Write the best title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    int nn = 5, num[3] = {0, 1, 2};
    double rl[3] = {1.9, 2.3, 3.0};
    char ch = 'b';

    swap(num[1], nn); // (a)
    cout << num[1] << nn << endl; // prints 51
    remove(nn, num, 3); // (b)
    // the next line prints 3.1415926
    cout << qn(rl, 3) << "\n"; // (c)
    d(num, 2); // (d)
    e(d(num, 1), e(true, e(true, ch))); // (e)
    return 0;
}
```

(a) Title line for swap as called at the line marked (a).
**Answer:** void swap(int &x, int &y)

(b) Title line for remove as called at the line marked (b).
**Answer:** void remove(int x, int y[], int z)

(c) Title line for qn as called at the line marked (c).
**Answer:** double qn(double x[], int c)

(d) Title line for d as called at the line marked (d).
**Answer:** bool d(int x[], int y)

(e) Title line for e as called at the line marked (e).
**Answer:** char e(bool x, char y)
Problem 14  Consider the following C++ program.

```cpp
void a(int x, int &y) {
    x = y;
    y = x + 1;
}

int b(int &x, int &y) {
    y = x + 1;
    x = y;
    return y - 2;
}

void c(int x[], int y) {
    if (y < 1) return;
    c(x, y - 1);
    cout << x[y - 1] * y;
}

int main() {
    int x[6] = {2, 3, 4, 5, 6, 7};
    int y[4] = {6, 5, 4, 3};
    cout << x[y[1]] % y[x[1]] << endl;  // line (a)
    a(x[0], x[1]);
    cout << x[0] << x[1] << endl;  // line (b)
    cout << b(x[2], x[3]) << endl;  // line (c)
    c(y, 3); cout << endl;  // line (e)
}
```

(a) What is the output at line (a)?

Answer:

1

(b) What is the output at line (b)?

Answer:

24

(c) What is the output at line (c)?

Answer:

3

(d) What is the output at line (d)?

Answer:

55

(e) What is the output at line (e)?

Answer:

61012
Problem 15  Write a program that reads a positive integer \( n \) from the user. If the user gives a non-positive value for \( n \) the program should terminate immediately. Otherwise, the program should print an upside down triangle with \( n \) rows that looks like the following sample when \( n \) is 4.

\[
\begin{align*}
&X X X X \\
&X X X \\
&X X \\
&X
\end{align*}
\]

The triangle should be made with \( X \) and blank symbols with one fewer \( X \) per row. The \( X \)s should be separated by blanks and the picture should be symmetric about a vertical line through its middle.

Excessively long solutions that use more than 20 lines of code may lose points.

Answer:

```cpp
int main() {
    int n;
    cout << "Enter a non-negative number n: ";
    cin >> n;
    if (n <= 0) return 0;

    for (int r = n - 1; r >= 0; r--) {
        for (int c = -(n - 1); c <= n - 1; c++)
            if (c < -r || c > r || (c + r) % 2 != 0) cout << " ";
        else cout << "X";
        cout << endl;
    }
    return 0;
}
```

Alternative solution:

```cpp
void triangle(int n, int indent) {
    if (n == 0) return;
    for (int c = 1; c <= indent; c++) cout << " ";
    for (int c = 1; c <= n; c++) cout << "X ";
    cout << endl;
    triangle(n - 1, indent + 1);
}

int main() {
    int n;
    cout << "Enter a non-negative number n: ";
    cin >> n;
    if (n <= 0) return 0;
    triangle(n, 0);
    return 0;
}
```

Problem 16  The recursive function `append` uses two positive integer parameters \( x \) and \( y \) and returns an answer formed from the digits of \( x \) followed by those of \( y \). For example, if the parameters are 196 and 83 the returned value is 19683.

The function is applied in another recursive function `reverse` that reverses a positive integer none of whose digits are 0. For example the reverse of 12345 is 54321.

Implementations of these functions with parts of the code covered up are given below. There is also a main program that uses them.

Some pieces of code have been replaced by PART (a), PART (b), and so on. To answer the 5 parts of this question you should supply the C++ code that was replaced. Each answer must fit on a single line.
int append(PART (a)) {
    if (PART (b))
        return x;
    PART (c)
}

int reverse(int x) {
    if (PART (d))
        return x;
    PART (e)
}

int main() {
    cout << reverse(19683) << endl; // prints 38691
    cout << reverse(1968) << endl;  // prints 8691
    return 0;
}

(a) Give a replacement for PART (a) to declare parameters x and y
Answer: PART (a) is int x, int y

(b) Give a replacement for PART (b) to test for the base case of recursion:
Answer: PART (b) is y == 0

(c) Give a replacement for PART (c) as a useful recursive call:
Answer: PART (c) is return 10 * append(x, y / 10) + y % 10;

(d) Give a replacement for PART (d) to test for the base case of recursion:
Answer: PART (d) is x < 10

(e) Give a replacement for PART (e) as a useful recursive call:
Answer: PART (e) is return append(x % 10, reverse(x / 10));

Problem 17  Write a function called peaks that prints the elements in an array that are larger than both of their neighbors. (The first and last elements do not have 2 neighbors and are not to be counted.) Different elements to be printed should be separated by spaces.
Excessively long solutions that use more than 8 lines of code may lose points. A program that uses the function peaks follows.

int main() {
    int x[8] = {3,1,4,1,5,9,2,6};
    peaks(x, 8);  // prints 4 9
    return 0;
}

Answer:

void peaks(int a[], int c) {
    for (int i = 1; i < c - 1; i++)
        if (a[i] > a[i - 1] && a[i] > a[i + 1]) cout << a[i] << " ";
    cout << endl;
}
Problem 18  Write a function called *duplicates* that has a single parameter that is a positive integer. It returns the integer obtained by changing all digits in the parameter to the first digit. Your function can return any result of your choice if it is given an illegal parameter value. Excessively long solutions that use more than 8 lines of code may lose points. A program that uses the function *duplicates* follows.

```cpp
int main() {
    cout << duplicates(6789) << endl;  // prints 6666
    cout << duplicates(123) << endl;   // prints 111
    cout << duplicates(12345) << endl; // prints 11111
    return 0;
}
```

Answer:

```cpp
int duplicates(int x) {
    if (x < 10) return x;
    int y = duplicates(x / 10);
    return 10 * y + y % 10;
}
```

Problem 19  Write the best title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    double xx = 5, xVals[3] = {0, 1, 2};
    int ins[3] = {1, 2, 3};
    string stg = "b";

    xx = combine(stg, 1);     // (a)
    combine(xVals[2], ins[1]); // (b)
    if (partC(ins, 3)) cout << "Yes\n";  // (c)
    d(xx, 2);                 // (d)
    e(d(xx, ins[1]), e((char) e('b', ins[2]), 0)); // (e)
    return 0;
}
```

(a) Title line for *combine* as called at the line marked (a).
Answer: `double combine(string x, int y)`
(b) Title line for *combine* as called at the line marked (b).
Answer: `void combine(double x, int y)`
(c) Title line for *partC* as called at the line marked (c).
Answer: `bool partC(int x[], int c)`
(d) Title line for *d* as called at the line marked (d).
Answer: `char d(double x, int y)`
(e) Title line for *e* as called at the line marked (e).
Answer: `int e(char x, int y)`

Problem 20  Consider the following C++ program.
void a(int &x, int y) {
    x = y;
    y = x + 1;
}
int b(int &x, int y) {
    y = x + 1;
    x = y;
    return y;
}
void c(int x[], int y) {
    if (y < 1) return;
    cout << x[y - 1] - y;
    c(x, y - 1);
}

int main() {
    int x[6] = {0, 2, 4, 6, 8, 10};
    int y[3] = {6, 4, 2};
    cout << y[x[1]] % x[y[1]] << endl; // line (a)
    a(x[0], x[1]);
    cout << x[0] << x[1] << endl; // line (b)
    cout << b(x[2], x[3]) << endl; // line (c)
    c(y, 3); cout << endl; // line (e)
}

(a) What is the output at line (a)?
Answer: 2
(b) What is the output at line (b)?
Answer: 22
(c) What is the output at line (c)?
Answer: 5
(d) What is the output at line (d)?
Answer: 56
(e) What is the output at line (e)?
Answer: -125

Problem 21  Write a program that uses a standard C++ function to generate a random integer secret between 1 and 10. It then asks the user to guess the secret number and gives at most 3 guesses. Your program should run to produce sample output as shown here:
You have 3 guesses to find my secret number.
What's your next guess: 3
What's your next guess: 4
Correct!

You have 3 guesses to find my secret number.
What's your next guess: 1
What's your next guess: 7
What's your next guess: 5
You couldn't guess it. My number was 4

Excessively long solutions that use more than 20 lines of code may lose points.

Answer:

```cpp
#include <cstdlib>

int main() {
    int secret = rand() % 10 + 1;
    cout << "You have 3 guesses to find my secret number.\n";
    int guess, strikes = 0;
    while (strikes < 3) {
        cout << "What's your next guess: ";
        cin >> guess;
        if (guess == secret) {
            cout << "Correct!\n";
            return 0;
        }
        strikes++;
    }
    cout << "You couldn't guess it. My number was " << secret << endl;
    return 0;
}
```

Problem 22  The recursive function `containsDigit` uses two parameters. The first represents a positive integer and the second represents a digit (an integer between 0 and 9). The function returns a result of true if the first parameter has the second as one of its digits.

It is applied in another recursive function `removeDuplicates` that returns a result that keeps only the leftmost occurrence of each digit in a positive integer. For example `removeDuplicates(1123243)` would return 1234.

Implementations of these functions with parts of the code covered up are given below. There is also a main program that uses them.

Some pieces of code have been replaced by PART (a), PART (b), and so on. To answer the 5 parts of this question you should supply the C++ code that was replaced. Each answer must fit on a single line.

```cpp
bool containsDigit(int x, int d) {
    if (PART (a)) return false;
    if (PART (b)) return true;
    return PART (c);
}

int removeDuplicates(int x) {
    if (x < 10) return x;
    if (containsDigit(x / 10, x % 10))
        return PART (d);
    return PART (e);
}

int main() {
    cout << removeDuplicates(1123243) << endl; // prints 1234
    cout << removeDuplicates(1143223) << endl; // prints 1432
    return 0;
}
```
(a) Give a replacement for PART (a) to test for the base case of recursion:

Answer: PART (a) is  \( x == 0 \)

(b) Give a replacement for PART (b) to test the last digit

Answer: PART (b) is  \( x \% 10 == d \)

(c) Give a replacement for PART (c) as a useful recursive call:

Answer: PART (c) is  \( \text{containsDigit}(x / 10, d) \)

(d) Give a replacement for PART (d) as a useful recursive call:

Answer: PART (d) is  \( \text{removeDuplicates}(x / 10) \)

(e) Give a replacement for PART (e) as another useful recursive call

Answer: PART (e) is  \( 10 * \text{removeDuplicates}(x / 10) + x \% 10 \)

Problem 23  Write a function called `peaks` that prints the elements in an array that are larger than the average of the entries in the array. Different elements to be printed should be separated by spaces.

Excessively long solutions that use more than 10 lines of code may lose points. A program that uses the function `peaks` follows.

```c
int main() {
    int x[8] = {3,1,4,1,5,9,2,6}; // has average 3.875
    peaks(x, 8); // prints 4 5 9 6
    return 0;
}
```

Answer:

```c
void peaks(int a[], int c) {
    int sum = 0;
    for (int i = 0; i < c ; i++)
        sum += a[i];
    double average = sum / (int) c;
    for (int i = 0; i < c; i++)
        if (a[i] > average) cout << a[i] << " ";
    cout << endl;
}
```

Problem 24  Write a function called `sixes` that has a single parameter that is a positive integer. It returns the integer obtained by changing all digits of the parameter to 6.

Your function can return any result of your choice if it is given an illegal parameter value. Excessively long solutions that use more than 8 lines of code may lose points. A program that uses the function `sixes` follows.

```c
int main() {
    cout << sixes(6789) << endl; // prints 6666
    cout << sixes(123) << endl; // prints 666
    cout << sixes(12345) << endl; // prints 66666
    return 0;
}
```

Answer:
int sixes(int x) {
    if (x < 10) return 6;
    return 10 * sixes(x / 10) + 6;
}

Problem 25  Write the best title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

int main() {
    int nn = 5, num[3] = {0, 1, 2};
    double rl[3] = {1.9, 2.3, 3.0};
    string ch = "h";

    swap(rl[1], rl[2]); // (a)
    reOrder(num, 3); // (b)
    // the next line prints No
    cout << qn(rl, 3) << "\n"; // (c)
    d(num, 2); // (d)
    if (d(num, e(e(e(nn))))) cout << "Yes\n"; // (e)
    return 0;
}

(a) Title line for swap as called at the line marked (a).
Answer: void swap(double &x, double &y)

(b) Title line for reOrder as called at the line marked (b).
Answer: void reOrder(int y[], int z)

(c) Title line for qn as called at the line marked (c).
Answer: string qn(double x[], int c)

(d) Title line for d as called at the line marked (d).
Answer: bool d(int x[], int y)

(e) Title line for e as called at the line marked (e).
Answer: int e(int x)

Problem 26  Consider the following C++ program.

void a(int &x, int &y) {
    x = y;
    y = x + 1;
}

int b(int &x, int y) {
    y = x + 1;
    x = y;
    return y - 2;
}

void c(int x[], int y) {
    if (y < 1) return;
    c(x, y - 1);
    cout << x[y - 1] * y;
}

int main() {

Problem 27 Write a math tutor program that uses a standard C++ function to generate two random integers \( x \) and \( y \) between 6 and 12 (inclusive). Then ask the user to enter the product of the numbers and say whether the user’s answer is right or wrong. If the user is wrong give them a second chance to answer. Your program should produce output as shown here:

```
What's the product of 10 and 8? 100
Wrong!
Try again: 80
Correct!
```

Excessively long solutions that use more than 20 lines of code may lose points.

Answer:

```cpp
#include <cstdlib>

int main() {
  int x = rand() % 7 + 6;
  int y = rand() % 7 + 6;
  cout << "What's the product of " << x << " and " << y << "? ";
  int answer;
```
Problem 28  The recursive function removeDigit uses two parameters. The first represents a positive integer and the second represents a digit (an integer between 0 and 9). The function returns a result obtained by removing the digit from the first parameter. For example removeDigit(11231,1) returns 23.

It is applied in another recursive function removeDuplicates that returns a result that keeps only the rightmost occurrence of each digit in a positive integer. For example removeDuplicates(1123243) would return 1243.

Implementations of these functions with parts of the code covered up are given below. There is also a main program that uses them.

Some pieces of code have been replaced by PART (a), PART (b), and so on. To answer the 5 parts of this question you should supply the C++ code that was replaced. Each answer must fit on a single line.

```cpp
int removeDigit(int x, int d) {
    if (PART (a))
        return 0;
    if (x % 10 == d)
        return PART (b);
    return PART (c);
}

int removeDuplicates(int x) {
    if (x < 10) return x;
    int y = removeDuplicates(PART (d));
    return PART (e);
}

int main() {
    cout << removeDuplicates(1123243) << endl; // prints 1243
    cout << removeDuplicates(1143223) << endl; // prints 1423
    return 0;
}

(a) Give a replacement for PART (a) to test for base cases of recursion:
Answer: PART (a) is x == 0

(b) Give a replacement for PART (b) as a useful recursive call:
Answer: PART (b) is removeDigit(x / 10, d);

(c) Give a replacement for PART (c) to apply another useful recursive call:
Answer: PART (c) is removeDigit(x / 10, d) * 10 + x % 10

(d) Give a replacement for PART (d) as a useful recursive call
Answer: PART (d) is removeDigit(x / 10, x % 10)

(e) Give a replacement for PART (e) to compute an answer using x and y
Answer: PART (e) is y * 10 + x % 10;
```
Problem 29  Write a function called `peaks` that returns the number of elements in an array that are larger than the average of the entries in the array.

Excessively long solutions that use more than 10 lines of code may lose points. A program that uses the function `peaks` follows.

```cpp
int main() {
    int x[8] = {3,1,4,1,5,9,2,6}; // has average 3.875
    cout << peaks(x, 8) << endl; // prints 4 since the elements 4, 5, 9, 6 are above average
    return 0;
}
```

Answer:

```cpp
int peaks(int a[], int c) {
    int sum = 0, count = 0;
    for (int i = 0; i < c; i++)
        sum += a[i];
    double average = sum / (int) c;
    for (int i = 0; i < c; i++)
        if (a[i] > average) count++;
    return count;
}
```

Problem 30  Write a function called `duplicates` that has a single parameter that is an integer greater than 99. It returns the integer obtained by changing each of the first 3 digits in the parameter to the first digit.

Your function can return any result of your choice if it is given an illegal parameter value. Excessively long solutions that use more than 8 lines of code may lose points. A program that uses the function `duplicates` follows.

```cpp
int main() {
    cout << duplicates(6789) << endl; // prints 6669
    cout << duplicates(123) << endl; // prints 111
    cout << duplicates(12345) << endl; // prints 11145
    return 0;
}
```

Answer:

```cpp
int duplicates(int x) {
    if (x < 1000) return x/100 * 111;
    return 10 * duplicates(x / 10) + x % 10;
}
```

Problem 31  Write the best title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    int nn = 5, num[3] = {0, 1, 2};
    double r1[3] = {1.9, 2.3, 3.0};
    cout << endl; // prints blank line
    return 0;
}
```
Problem 32
Consider the following C++ program.

```cpp
void a(int &x, int y) {
    x = y;
    y = x + 1;
}

int b(int &x, int y) {
    y = x + 1;
    x = y;
    return y;
}

void c(int x[], int y) {
    if (y < 1) return;
    cout << x[y - 1] - y;
    c(x, y - 1);
}

int main() {
    int x[6] = {3, 2, 1, 6, 5, 4};
    int y[3] = {3, 4, 5};
    cout << y[x[1]] % x[y[1]] << endl; // line (a)
a(x[0], x[1]);
    cout << x[0] << x[1] << endl; // line (b)
cout << b(x[2], x[3]) << endl; // line (c)
c(y, 3); cout << endl; // line (e)
}
```

(a) What is the output at line (a)?
Answer: 0

(b) What is the output at line (b)?
Answer:
(c) What is the output at line (c)?
Answer:
2

(d) What is the output at line (d)?
Answer:
26

(e) What is the output at line (e)?
Answer:
222

Problem 33  Write a program that reads a positive integer n from the user. If the user gives a non-positive value for n the program should terminate immediately. Otherwise, the program should print a triangle with n rows that looks like the following sample when n is 4.

```
*   *
*X*X*
*X*X*X*
```

The triangle should be made with * and X symbols with one extra of each per row. The *s should be separated by Xs and the picture should be symmetric about a vertical line through its middle.

Excessively long solutions that use more than 20 lines of code may lose points.

Answer:
```
int main() {
    int n;
    cout << "Enter a non-negative number n: ";
    cin >> n;
    if (n <= 0) return 0;

    for (int r = 0; r < n; r++) {
        for (int c = -(n - 1); c <= n - 1; c++)
            if (c < -r || c > r) cout << " ";
            else if ((c + r) % 2 != 0) cout << "X";
            else cout << "*";
        cout << endl;
    }
    return 0;
}
```

Problem 34  The recursive function removeFirst removes the first digit of a positive integer. It is applied in another recursive function middle that also has a positive integer parameter. The function middle returns either the middle digit if the parameter has an odd number of digits or the middle two digits if it has an even number of digits. For example the middle of 12345 is 3 but the middle of 1234 is 23.

Implementations of these functions with parts of the code covered up are given below. There is also a main program that uses them.

Some pieces of code have been replaced by PART (a), PART (b), and so on. To answer the 5 parts of this question you should supply the C++ code that was replaced. Each answer must fit on a single line.
int removeFirst(PART (a)) {
    if (PART (b))
        return PART (c);
    PART (d)
}

int middle(int x) {
    if (x < 100) return x;
    PART (e)
}

int main() {
    cout << middle(19683) << endl; // prints 6
    cout << middle(1968) << endl;  // prints 96
    return 0;
}

(a) Give a replacement for PART (a) to declare the parameter x
Answer: PART (a) is int x

(b) Give a replacement for PART (b) to test for the base case of recursion:
Answer: PART (b) is x < 10

(c) Give a replacement for PART (c) the result for the base case
Answer: PART (c) is 0

(d) Give a replacement for PART (d) as a useful recursive call:
Answer: PART (d) is return 10 * removeFirst(x / 10) + x % 10;

(e) Give a replacement for PART (e) as a useful recursive call:
Answer: PART (e) is return middle(removeFirst(x) / 10);

Problem 35  Write a function called lows that counts the number of elements in an array that are smaller than both of their neighbors. (The first and last elements do not have 2 neighbors and are not to be counted.) Excessively long solutions that use more than 8 lines of code may lose points. A program that uses the function lows follows.

int main() {
    int x[8] = {3,1,4,1,5,9,2,6};
    cout << lows(x, 8) << endl;  // prints 3 since the elements 1,1 and 2 are counted
    return 0;
}

Answer:

int lows(int a[], int c) {
    int ans = 0;
    for (int i = 1; i < c - 1; i++)
        if (a[i] < a[i - 1] && a[i] < a[i + 1]) ans++;
    return ans;
}

Problem 36  Write a function called twos that has a single parameter that is an integer greater than 9. It returns the integer obtained by changing each of the first 2 digits of the parameter to 2. Your function can return any result of your choice if it is given an illegal parameter value. Excessively long solutions that use more than 8 lines of code may lose points. A program that uses the function twos follows.
int main() {
    cout << twos(6789) << endl;  // prints 2289
    cout << twos(123) << endl;   // prints 223
    cout << twos(12345) << endl; // prints 22345
    cout << twos(13) << endl;    // prints 22
    return 0;
}

Answer:

int twos(int x) {
    if (x < 100) return 22;
    return 10 * twos(x / 10) + x % 10;
}

Problem 37  Write the best title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

Problem 38  Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out abcabc abc123.

#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    string words[4] = {"A ", "very ", "easy", "question "};
    cout << words[1].substr(2) << endl;  // line (a)
    for (int i = 0; i <= 2; i++) cout << words[i][i]; cout << endl; // line (b)
    cout << argv[1] << endl;   // line (c)
    cout << words[3].find("u") << endl; // line (d)
    cout << argc << endl;    // line (e)
    return 0;
}

(a) What is the output at line (a)?
Answer:
ry

(b) What is the output at line (b)?
Answer:
Aes

(c) What is the output at line (c)?
Answer:
abcabc

(d) What is the output at line (d)?
Answer:
(e) What is the output at line (e)?

**Answer:**

```c++

int main() {
    int x[5] = {3, 1, 4, 1, 5};
    // (a) Return the average. Here 2.5 is printed.
    cout << average(2, 3) << endl;
    // (b) Return the middle of 3 numbers, here 5 is printed.
    cout << middle(5, 6, 4) << endl;
    // (c) Return the middle entry of an array with odd capacity. Here 4.
    cout << middleEntry(x, 5) << endl;
    // (d) Return the first index of 7 in the array or -1 if not present. Here -1 is printed.
    cout << findIndex7(x, 5) << endl;
    // (e) Return the upper case version of a lower case char. Here print H
    cout << toUpper('h') << endl;
    return 0;
}

Answer:

(a)

double average(int x, int y) {
    return (x + y) / 2.0;
}

(b)

int middle(int x, int y, int z) {
    if ((x - y) * (x - z) <= 0) return x;
    if ((y - x) * (y - z) <= 0) return y;
    return z;
}

(c)

int middleEntry(int x[], int c) {
    return x[(c - 1)/2];
}

(d)

int findIndex7(int array[], int cap) {
    for (int i = 0; i < cap; i++)
        if (array[i] == 7) return i;
    return -1;
}
```
Problem 40  Write a complete C++ program that does the following:
It generates 250 random numbers between 1 and 1000. For each of the 250 numbers that has not been seen before
it prints the number.
Your program should not repeat any output value, random values should be computed with the C++ random number
function  rand() . This function should be called exactly 250 times. It is likely that fewer than 250 numbers will
be printed.
Excessively long or complicated code may lose points.
Answer:

```
#include <iostream>
#include <cstdlib>
using namespace std;

int main() {
    bool seen[1001];
    for (int i = 0; i < 1001; i++) seen[i] = false;
    for (int i = 0; i < 250; i++) {
        int n = rand() % 1000 + 1;
        if (!seen[n]) {
            cout << n << endl;
            seen[n] = true;
        }
    }
    return 0;
}
```

Problem 41  Write a function called rowSums. The function has two array parameters  first  and  second  the
first is two dimensional with 5 columns and the second is one dimensional. The entries of both arrays have type  int.  
Additional parameters specify the row and column counts for  first . The function sets each entry  second[r]  to
be the sum of the entries in row  r  of  first .
For example, a program that uses the function follows.

```
int main() {
    int first[3][5] = {{9,9,8,1,0},{2,9,8,1,0},{1,1,8,1,0}};
    int second[3];
    rowSums(first, second, 3, 5);
    for (int i = 0; i < 3; i++) cout << second[i] << " "; // prints 27 20 12
    cout << endl;
    return 0;
}
```

Excessively long or complicated code may lose points.
Answer:

```
void rowSums(int first[][5], int second[], int r, int c) {
    for (int i = 0; i < r; i++) {
        second[i] = 0;
        for (int j = 0; j < c; j++)
```
second[i] += first[i][j];
}
}

Problem 42  Write a function called reverseAdd. The function has two integer parameters first and second that are positive. It returns the number obtained by attaching the reverse of second after first. For instance reverseAdd(27, 729) would return 27927. If parameters have illegal values your function can operate however you choose. Excessively long solutions that use more than 8 lines of code may lose points.

For example, a program that uses the function follows.

```c
int main() {
    cout << reverseAdd(16, 538) << endl;  // prints 16835
    cout << reverseAdd(862, 538) << endl;  // prints 862835
    return 0;
}
```

Answer:

```c
int reverseAdd(int first, int second) {
    if (second == 0) return first;
    return reverseAdd(first * 10 + second % 10, second / 10);
}
```

Problem 43  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```c
int main() {
    double dd[3] = {0, 1.1, 2.2};
    string st[3] = {"1.9", "2.3", "3.0"};

    st[0] = f2(dd[0] + dd[1], dd[0], dd[0], st[2]);  // (b)
    dd[1] = f3(st, st, 3);             // (c)
    f4(st[1], 1);                     // (d)
    char k = f4(f5(dd[1], st), dd[1]);  // (e)
    return 0;
}
```

(a) Title line for f1.
Answer:

double f1(double x, double y)

(b) Title line for f2.
Answer:

string f2(double x, double y, double z, string w)

(c) Title line for f3.
Answer:

double f3(string w[], string x[], int c)

(d) Title line for f4.
Answer:
Problem 44 Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out 123cba abcxyz ABCDEF.

```cpp
#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    cout << words[1].substr(2) << endl; // line (a)
    for (int i = 0; i <= 2; i++) cout << words[i][i]; cout << endl; // line (b)
    cout << argv[2] << endl; // line (c)
    cout << words[3].rfind("l") << endl; // line (d)
    cout << argc << endl; // line (e)
    return 0;
}
```

(a) What is the output at line (a)?
Answer:
eddy

(b) What is the output at line (b)?
Answer:
Mrc

(c) What is the output at line (c)?
Answer:
abcxyz

(d) What is the output at line (d)?
Answer:
3

(e) What is the output at line (e)?
Answer:
4

Problem 45 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function that is written only in the designated answer space.
int main() {
    int x[5] = {7, 1, 4, 7, 5};
    // (a) Return the average. Here 3.33333 is printed.
    cout << average(2, 3, 5) << endl;
    // (b) Return the smaller of 2 numbers, here 5 is printed.
    cout << smaller(5, 6) << endl;
    // (c) Return the next to last entry of an array. Here 7.
    cout << secondLastEntry(x, 5) << endl;
    // (d) Return the last index of 7 in the array or -1 if not present. Here 3 is printed.
    cout << findIndex7(x, 5) << endl;
    // (e) Return the lower case version of an upper case char. Here print h
    cout << toLower('H') << endl;
    return 0;
}

Answer:
(a)

double average(int x, int y, int z) {
    return (x + y + z) / 3.0;
}

(b)

int smaller(int x, int y) {
    if (x <= y) return x;
    return y;
}

(c)

int secondLastEntry(int x[], int c) {
    return x[c - 2];
}

(d)

int findIndex7(int array[], int cap) {
    for (int i = cap - 1; i >= 0; i--)
        if (array[i] == 7) return i;
    return -1;
}

(e)

char toLower(char x) {
    return x + 'a' - 'A';
}

Problem 46 Write a complete C++ program that does the following:
It generates 250 random numbers between 1 and 1000. For each of the 250 numbers that has been seen before it
prints the number.
Random values should be computed with the C++ random number function rand(). This function should be
called exactly 250 times. If a random number is seen more than twice, it will be printed more than once.
Excessively long or complicated code may lose points.
Answer:
```cpp
#include <iostream>
#include <cstdlib>
using namespace std;

int main() {
    bool seen[1001];
    for (int i = 0; i < 1001; i++) seen[i] = false;
    for (int i = 0; i < 250; i++) {
        int n = rand() % 1000 + 1;
        if (seen[n]) cout << n << endl;
        seen[n] = true;
    }
    return 0;
}

Problem 47   Write a function called `colSums`. The function has two array parameters `first` and `second` the first is two dimensional with 5 columns and the second is one dimensional with the same number of columns. The entries of both arrays have type `int`. Additional parameters specify the row and column counts for `first`. The function sets each entry `second[c]` to be the sum of the entries in column `c` of `first`.

For example, a program that uses the function follows.

```cpp
int main() {
    int first[3][5] = {{9,9,8,1,0},{2,9,8,1,0},{1,1,8,1,0}};
    int second[5];
    colSums(first, second, 3, 5);
    for (int i = 0; i < 5; i++) cout << second[i] << " "; // prints 12 19 24 3 0
    cout << endl;
    return 0;
}
```

Excessively long or complicated code may lose points.

Answer:

```cpp
void colSums(int first[][5], int second[], int r, int c) {
    for (int i = 0; i < c; i++) {
        second[i] = 0;
        for (int j = 0; j < r; j++)
            second[i] += first[j][i];
    }
}
```

Problem 48   Write a function called `attach`. The function has two integer parameters `first` and `second` that are positive. It returns the number obtained by attaching `second` after `first`. For instance `attach(27,927)` would return 27927, If parameters have illegal values your function can operate however you choose. Excessively long solutions that use more than 8 lines of code may lose points.

For example, a program that uses the function follows.

```cpp
int main() {
    cout << attach(16, 835) << endl; // prints 16835
    cout << attach(862, 835) << endl; // prints 862835
    return 0;
}
```

Answer:
int attach(int first, int second) {
    if (second == 0) return first;
    return attach(first, second / 10) * 10 + second % 10;
}

Problem 49  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
    int dd[3] = {0, 1, 2};
    char st[3] = {'9', '2', '3'};

    st[0] = f2(dd[0] + dd[1], dd[0], dd[0], st[2]);  // (b)
    if (f3(st, st, 3)) return 0;  // (c)
    cout << 2 + f4(st[1], 1);  // (d)
    f4(f5(dd[1], st), dd[1]);  // (e)
    return 0;
}

(a) Title line for f1.
Answer:
int f1(int x, int y)

(b) Title line for f2.
Answer:
char f2(int x, int y, int z, char w)

(c) Title line for f3.
Answer:
bool f3(char w[], char x[], int c)

(d) Title line for f4.
Answer:
int f4(char x, int y)

(e) Title line for e.
Answer:
char f5(int x, char y[])

Problem 50  Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out 123456 456789 135799.

#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    string words[4] = {"123", "987654", "9999", "77777"};
    cout << words[2].substr(2) << endl;  // line (a)
    for (int i = 1; i <= 3; i++) cout << words[i][i]; cout << endl;  // line (b)
    words[3] = argv[2];
    cout << words[3] << endl;  // line (c)
    cout << words[3].find("9") << endl;  // line (d)
    cout << argc << endl;  // line (e)
    return 0;
}
(a) What is the output at line (a)?
Answer:
99

(b) What is the output at line (b)?
Answer:
897

(c) What is the output at line (c)?
Answer:
456789

(d) What is the output at line (d)?
Answer:
5

(e) What is the output at line (e)?
Answer:
4

Problem 51 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function that is written only in the designated answer space.

```c++
int main() {
    int x[5] = {7, 1, 4, 7, 5};
    // (a) Return the average. Here 3.33333 is printed.
    cout << average(2, 3, 5) << endl;
    // (b) Return the smaller of 2 numbers, here 5 is printed.
    cout << smaller(5, 6) << endl;
    // (c) Return the next to last entry of an array. Here 7.
    cout << secondLastEntry(x, 5) << endl;
    // (d) Return the last index of 7 in the array or -1 if not present. Here 3 is printed.
    cout << findIndex7(x, 5) << endl;
    // (e) Return the lower case version of an upper case char. Here print h
    cout << toLower('H') << endl;
    return 0;
}
```

Answer:
(a)
```c++
double average(int x, int y, int z) {
    return (x + y + z) / 3.0;
}
```

(b)
```c++
int smaller(int x, int y) {
    if (x <= y) return x;
    return y;
}
```
(c)

```c
int secondLastEntry(int x[], int c) {
    return x[c - 2];
}
```

(d)

```c
int findIndex7(int array[], int cap) {
    for (int i = cap - 1; i >= 0; i--)
        if (array[i] == 7) return i;
    return -1;
}
```

(e)

```c
char toLower(char x) {
    return x + 'a' - 'A';
}
```

Problem 52

Write a complete C++ program that does the following:

It generates random numbers between 1 and 1000. As soon as it generates a number that is the sum of the two numbers right before it, it should print out this sum, report the total number of random numbers that have been generated and end.

Your program should produce output in this form:

```
626 = 154 + 472  
Generated 307 Numbers  
```

Random values should be computed with the C++ random number function `rand()`.

Excessively long or complicated code may lose points.

Answer:

```c
#include <iostream>
#include <cstdlib>
using namespace std;

int main() {
    int lastButOne = rand() % 1000 + 1;
    int last = rand() % 1000 + 1;
    int count = 2;
    while (true) {
        int n = rand() % 1000 + 1;
        count++;
        if (n == last + lastButOne) {
            cout << n << " = " << last << " + " << lastButOne << endl;
            cout << "Generated " << count << " Numbers " << endl;
            return 0;
        }
        lastButOne = last;
        last = n;
    }
    return 0;
}
```
Problem 53  Write a function called `rowPositive`. The function has two array parameters `first` and `second` the first is two dimensional with 5 columns and the second is one dimensional. The entries of `first` have type `int`. Additional parameters specify the row and column counts for `first`. The function sets each entry `second[r]` to be `true` exactly when the entries in row `r` of `first` have a positive sum.

For example, a program that uses the function follows.

```cpp
int main() {
    int first[3][5] = {{9,-9,8,1,0},{2,-9,-8,1,0},{1,-1,-8,1,0}};
    bool second[3];
    rowPositive(first, second, 3, 5);
    for (int i = 0; i < 3; i++)
        if (second[i]) cout << "Positive ";
        else cout << "Negative "; // prints Positive Negative Negative
        cout << endl;
    return 0;
}
```

Excessively long or complicated code may lose points.

Answer:

```cpp
void rowPositive(int first[][5], bool second[], int r, int c) {
    for (int i = 0; i < r; i++) {
        int sum = 0;
        for (int j = 0; j < c; j++)
            sum += first[i][j];
        second[i] = sum > 0;
    }
}
```

Problem 54  Write a function called `numberMatch`. The function has two integer parameters `first` and `second` that are positive and have the same number of digits. It returns the number of positions where their digits are equal. For instance `numberMatch(1234,1894)` would return 2, since the numbers match in their first and last digits. If parameters have illegal values your function can operate however you choose. Excessively long solutions that use more than 5 lines of code may lose points.

For example, a program that uses the function follows.

```cpp
int main() {
    cout << numberMatch(1628, 1328) << endl; // prints 3
    cout << numberMatch(862, 862) << endl;   // prints 3
    cout << numberMatch(862, 628) << endl;   // prints 0
    return 0;
}
```

Answer:

```cpp
int numberMatch(int first, int second) {
    if (second == 0) return 0;
    int ans = numberMatch(first / 10, second / 10);
    if (first % 10 == second % 10) return ans + 1;
    return ans;
}
```

Problem 55  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.
int main() {
    double rr[3] = {0, 1.1, 2.2};
    int zz[3] = {19, 23, 30};
    char ch = 'a';

    ch = a(ch, ch); // (a)
    zz[0] = b(rr[0], zz[1]); // (b)
    cout << 3 * c(a(ch, ch)); // (c)
    d(d(rr[0], rr[1]), 5); // (d)
    a(e(rr, rr[0] + rr[1], zz), ch); // (e)
    return 0;
}

(a) Title line for a.
Answer:

cchar a(char x, char y)

(b) Title line for b.
Answer:

int b(double x, int u)

(c) Title line for c.
Answer:

int c(char x)

(d) Title line for d.
Answer:

double d(double x, double y)

(e) Title line for e.
Answer:

char e(double z[], double x, int y[])

Problem 56 Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out PQRPQR PQR789.

#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    string words[4] = {"NO0", "NO0P", "OPQR", "MNOPQRS"};
    cout << words[3].substr(2) << endl; // line (a)
    for (int i = 0; i <= 3; i++) cout << words[i][i]; cout << endl; // line (b)
    words[3] = argv[2];
    cout << words[3] << endl; // line (c)
    cout << words[3].rfind("R") << endl; // line (d)
    cout << argc % argc << endl; // line (e)
    return 0;
}

(a) What is the output at line (a)?
Answer:
Problem 57  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function that is written only in the designated answer space.

```cpp
int main() {
    int x[5] = {3, 1, 4, 1, 5};
    // (a) Return the average. Here 2.5 is printed.
    cout << average(2, 3) << endl;
    // (b) Return the middle of 3 numbers, here 5 is printed.
    cout << middle(5, 6, 4) << endl;
    // (c) Return the middle entry of an array with odd capacity. Here 4.
    cout << middleEntry(x, 5) << endl;
    // (d) Return the first index of 7 in the array or -1 if not present. Here -1 is printed.
    cout << findIndex7(x, 5) << endl;
    // (e) Return the upper case version of a lower case char. Here print H
    cout << toUpper('h') << endl;
    return 0;
}
```

Answer:

(a)
```cpp
double average(int x, int y) {
    return (x + y) / 2.0;
}
```

(b)
```cpp
int middle(int x, int y, int z) {
    if ((x - y) * (x - z) <= 0) return x;
    if ((y - x) * (y - z) <= 0) return y;
    return z;
}
```
int middleEntry(int x[], int c) {
    return x[(c - 1)/2];
}

int findIndex7(int array[], int cap) {
    for (int i = 0; i < cap; i++)
        if (array[i] == 7) return i;
    return -1;
}

char toUpper(char x) {
    return x + 'A' - 'a';
}

Problem 58
Write a complete C++ program that does the following:
It generates random numbers between 1 and 1000. As soon as it generates a number that is the square root of the number right before it, it should print out these two numbers, report the total number of random numbers that have been generated and end.
Your program should produce output in this form:

19 = sqrt 361
Generated 20703 Numbers

Random values should be computed with the C++ random number function `rand()`.
Excessively long or complicated code may lose points.

Answer:

```cpp
#include <iostream>
#include <cstdlib>
using namespace std;

int main() {
    int last = rand() % 1000 + 1;
    int count = 1;
    while (true) {
        int n = rand() % 1000 + 1;
        count++;
        if (n * n == last) {
            cout << n << " = sqrt " << last << endl;
            cout << "Generated " << count << " Numbers " << endl;
            return 0;
        }
        last = n;
    }
    return 0;
}
```
Problem 59  Write a function called \texttt{colPositive}. The function has two array parameters \texttt{first} and \texttt{second} the first is two dimensional with 5 columns and the second is one dimensional with the same number of columns. The entries of \texttt{first} have type \texttt{int}. Additional parameters specify the row and column counts for \texttt{first}. The function sets each entry \texttt{second}[c] to be \texttt{true} exactly when the entries in column \texttt{c} of \texttt{first} have a positive product.

For example, a program that uses the function follows.

```cpp
int main() {
    int first[3][5] = {{9,-9,8,1,0},{2,-9,-8,1,0},{1,-1,-8,1,0}};
    bool second[5];
    colPositive(first, second, 3, 5);
    for (int i = 0; i < 5; i++)
        if (second[i]) cout << "Positive ";
        else cout << "Not "; // prints Positive Not Positive Positive Not
    cout << endl;
    return 0;
}
```

Excessively long or complicated code may lose points.

\textbf{Answer:}

```cpp
void colPositive(int first[][5], bool second[], int r, int c) {
    for (int i = 0; i < c; i++) {
        int product = 1;
        for (int j = 0; j < r; j++)
            product *= first[j][i];
        second[i] = product > 0;
    }
}
```

Problem 60  Write a function called \texttt{sumMatch}. The function has two integer parameters \texttt{first} and \texttt{second} that are positive and have the same number of digits. It returns the sum of the digits that match in the two numbers. For instance \texttt{sumMatch(1254,1451)} would return 6, since the numbers match in their first and third digits which are 1 and 5 the answer is found as 1 + 5. If parameters have illegal values your function can operate however you choose. Excessively long solutions that use more than 5 lines of code may lose points.

For example, a program that uses the function follows.

```cpp
int main() {
    cout << sumMatch(1628, 1328) << endl; // prints 11
    cout << sumMatch(862, 862) << endl; // prints 16
    cout << sumMatch(862, 628) << endl; // prints 0
    return 0;
}
```

\textbf{Answer:}

```cpp
int sumMatch(int first, int second) {
    if (second == 0) return 0;
    int ans = sumMatch(first / 10, second / 10);
    if (first % 10 == second % 10) return ans + first % 10;
    return ans;
}
```

Problem 61  Write the best title lines for the functions that are called by the following main program. \textbf{Do not} supply blocks for the functions.
int main() {
    double dd[3] = {0, 1.1, 2.2};
    string st[3] = {"1.9", "2.3", "3.0"};
    st[0] = f2(dd[0] + dd[1], dd[0], dd[0], st[2]); // (b)
    st[0][0] = f3(st, st, 3); // (c)
    f4(st[1], 1); // (d)
    f4(f5(dd[1], st), f4("hello", dd[1])); // (e)
    return 0;
}

(a) Title line for f1.
Answer:

double f1(double x, double y)

(b) Title line for f2.
Answer:

string f2(double x, double y, double z, string w)

(c) Title line for f3.
Answer:

char f3(string w[], string x[], int c)

(d) Title line for f4.
Answer:

double f4(string x, double y)

(e) Title line for f5.
Answer:

string f5(double x, string y[])

Problem 62  Consider the following C++ program. It is compiled to a.out and executed with the command
./a.out 111999 229992 999333.

#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    string words[4] = {"444", "55555", "6666", "77777"};
    cout << words[2].substr(2) << endl; // line (a)
    for (int i = 1; i <= 3; i++) cout << words[i][i]; cout << endl; // line (b)
    words[3] = argv[2];
    cout << words[3] << endl; // line (c)
    cout << words[3].rfind("9") << endl; // line (d)
    cout << argc << endl; // line (e)
    return 0;
}

(a) What is the output at line (a)?
Answer:

66
(b) What is the output at line (b)?
Answer:
567

(c) What is the output at line (c)?
Answer:
229992

(d) What is the output at line (d)?
Answer:
4

(e) What is the output at line (e)?
Answer:
4

**Problem 63** Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function that is written only in the designated answer space.

```cpp
int main() {
    string x[5] = {"CS", "111", "Queens", "College", "CUNY"};
    // (a) Return the average. Here 2.5 is printed.
    cout << average(2, 3) << endl;
    // (b) Return the middle of 3 numbers, here 5 is printed.
    cout << middle(5, 6, 4) << endl;
    // (c) Return the string formed by the first characters of the entries. Here C1QCC.
    cout << initialLetters(x, 5) << endl;
    // (d) Return the first index of an entry containing a target or -1 if not present. Here 2 is printed.
    cout << findIndexContains(x, 5, "ee") << endl;
    // (e) Return the longest entry. Here print College
    cout << longest(x, 5) << endl;
    return 0;
}
```

Answer:
(a)
```cpp
double average(int x, int y) {
    return (x + y) / 2.0;
}
```

(b)
```cpp
int middle(int x, int y, int z) {
    if ((x - y) * (x - z) <= 0) return x;
    if ((y - x) * (y - z) <= 0) return y;
    return z;
}
```

(c)
string initialLetters(string x[], int c) {
    string ans = "";
    for (int i = 0; i < c; i++) ans += x[i].substr(0, 1);
    return ans;
}

int findIndexContains(string array[], int cap, string target) {
    for (int i = 0; i < cap; i++) {
        int x = array[i].find(target);
        if (0 <= x && x < array[i].size()) return i;
    }
    return -1;
}

string longest(string x[], int cap) {
    string ans = x[0];
    for (int i = 1; i < cap; i++)
        if (x[i].size() > ans.size()) ans = x[i];
    return ans;
}

Problem 64 Write a complete C++ program that does the following:
It generates random numbers between 1 and 1000. As soon as a repeat number is generated the program stops and
reports the total number of random numbers that have been generated.
Random values should be computed with the C++ random number function `rand()`.
Excessively long or complicated code may lose points.
Answer:
#include <iostream>
#include <cstdlib>
using namespace std;

int main() {
    int count = 0;
    bool seen[1001];
    for (int i = 0; i < 1001; i++) seen[i] = false;
    while (true) {
        int n = rand() % 1000 + 1;
        count++;
        if (seen[n]) {
            cout << count << endl;
            return 0;
        }
        seen[n] = true;
    }
    return 0;
}

Problem 65 Write a function called `maxIndex`. The function has two array parameters `first` and `second` the
first is two dimensional with 4 columns and the second is one dimensional. The entries of the two dimensional array
are required to be distinct integers. The arrays have the same number of columns. Additional parameters specify the row and column counts for first. The function sets each entry second[c] to be the index of the row of first for which the entry in column c is as large as possible.

For instance if first has 3 rows and 4 columns, as follows:

```
99  95  80  16
25  98  82  17
10  11  83  15
```

Then second would be set to store 0, 1, 2, 1.

For example, a program that uses the function follows.

```cpp
int main() {
    int first[3][4] = {{99,95,80,16},{25,98,82,17},{10,11,83,15}};
    int second[4];
    maxIndex(first, second, 3, 4);
    for (int i = 0; i < 4; i++) cout << second[i] << " "; // prints 0 1 2 1
    cout << endl;
    return 0;
}
```

Excessively long or complicated code may lose points.

**Answer:**

```cpp
void maxIndex(int first[][4], int second[], int r, int c) {
    for (int i = 0; i < c; i++) {
        second[i] = 0;
        for (int j = 0; j < r; j++)
            if (first[j][i] > first[second[i]][i])
                second[i] = j;
    }
}
```

---

**Problem 66** Write a function called drop. The function has two integer parameters first and second that are positive. It returns the number obtained by dropping digits from the left of first until it has no more digits than second. For instance drop(19683,729) would drop 2 digits from the left of 19683 and return 683. If parameters have illegal values your function can operate however you choose. Excessively long solutions that use more than 8 lines of code may lose points.

For example, a program that uses the function follows.

```cpp
int main() {
    cout << drop(16, 538) << endl; // prints 16
    cout << drop(862, 538) << endl; // prints 862
    cout << drop(3862, 538) << endl; // prints 862
    cout << drop(53862, 538) << endl; // prints 862
    return 0;
}
```

**Answer:**

```cpp
int drop(int first, int second) {
    if (second == 0) return 0;
    return drop(first / 10, second / 10) * 10 + first % 10;
}
```

---

**Problem 67** Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out abcabc abc123.
```cpp
#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    string words[4] = {"A ", "very ", "easy", "question ";
    cout << words[1].substr(2) << endl; // line (a)
    for (int i = 0; i <= 2; i++) cout << words[i][i]; cout << endl; // line (b)
    words[3] = argv[1];
    cout << words[3] << endl; // line (c)
    cout << words[3].rfind("c") << endl; // line (d)
    cout << argc << endl; // line (e)
    return 0;
}

(a) What is the output at line (a)?
Answer:
ry

(b) What is the output at line (b)?
Answer:
Aes

(c) What is the output at line (c)?
Answer:
abcabc

(d) What is the output at line (d)?
Answer:
5

(e) What is the output at line (e)?
Answer:
3

Problem 68
Write C++ statements to carry out the following tasks. Do not write complete programs, just give a few lines of C++ code. Most answers need no more than two lines. No solution can use more than four lines. Assume the following variables have been declared and initialized with positive values.

```cpp
int x, y;
```
(b) Print the remainder when variable x is divided by variable y.

Answer:

    cout << x % y << endl;

(c) Print the square root of 19. Use a C++ function for the calculation.

Answer:

    cout << sqrt(19.0) << endl;

(d) Print a random number in the range 23 to 34, inclusive. Use a C++ function.

Answer:

    cout << rand() % 12 + 23 << endl;

(e) Print the digits of the variable x backwards. So if x is 25, print 52.

Answer:

    while (x > 0) {
        cout << x % 10;
        x = x / 10;
    }
    cout << endl;

Problem 69 Write a function called reverseAdd. The function has two integer parameters first and second that are positive. It returns the number obtained by attaching digits in odd positions of the reverse of second after first. For instance reverseAdd(27,78289) would return 27927, since the digits in odd positions of the reverse of second are 9, 2 and 7. If parameters have illegal values your function can operate however you choose. Excessively long solutions that use more than 8 lines of code may lose points.

For example, a program that uses the function follows.

```cpp
int main() {
    cout << reverseAdd(16, 51328) << endl; // prints 16835
    cout << reverseAdd(862, 151318) << endl; // prints 862835
    return 0;
}
```

Answer:

```cpp
int reverseAdd(int first, int second) {
    if (second == 0) return first;
    return reverseAdd(first * 10 + second % 10, second / 100);
}
```

Problem 70 Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out 123cba abcxyz ABCDEF.
#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    cout << words[1].substr(2) << endl;                      // line (a)
    for (int i = 0; i <= 2; i++) cout << words[i][i];       // line (b)
    words[3] = argv[2];
    cout << words[3] << endl;                               // line (c)
    cout << words[3].find("c") << endl;                    // line (d)
    cout << argc << endl;                                  // line (e)
    return 0;
}

(a) What is the output at line (a)?
Answer:
eddy

(b) What is the output at line (b)?
Answer:
Mrc

(c) What is the output at line (c)?
Answer:
abcxyz

(d) What is the output at line (d)?
Answer:
2

(e) What is the output at line (e)?
Answer:
4

**Problem 71** Write a function called `attach`. The function has two integer parameters `first` and `second` that are positive. It returns the number obtained by attaching to `first` alternate digits of `second` ending at the last digit. These are the rightmost digit and any others that are even number of places from the right. The order of these digits is to remain as in `second`.

For instance, `attach(27, 91217)` would return 27927, since the digits in even positions (from the right) of `second` are 9, 2 and 7. If parameters have illegal values your function can operate however you choose. Excessively long solutions that use more than 8 lines of code may lose points.

For example, a program that uses the function follows.

```cpp
int main() {
    cout << attach(16, 181315) << endl;       // prints 16835
    cout << attach(862, 81315) << endl;       // prints 862835
    return 0;
}
```

Answer:
int attach(int first, int second) {
    if (second == 0) return first;
    return attach(first, second / 100) * 10 + second % 10;
}

Problem 72 Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
    double dd[3] = {0, 1.1, 2.2};
    string st[3] = {"1.9", "2.3", "3.0"};

    st[0] = f2(dd[0] + dd[1], dd[0], dd[0], st[2]); // (b)
    st[0] = f3(st, st, 3); // (c)
    f4(st[1], 1); // (d)
    f4(f5(dd[1], st), f4("hello", dd[1])); // (e)
    return 0;
}

(a) Title line for f1.
Answer:

double f1(double x, double y)

(b) Title line for f2.
Answer:

string f2(double x, double y, double z, string w)

(c) Title line for f3.
Answer:

string f3(string w[], string x[], int c)

(d) Title line for f4.
Answer:

double f4(string x, double y)

(e) Title line for f5.
Answer:

string f5(double x, string y[])

Problem 73 Consider the following C++ program.

#include <iostream>
using namespace std;

double fun(int x[], int cap, int gap) {
    double ans = 0.0;
    for (int i = cap - 1; i >= 0; i-= gap)
        ans += x[i];
    return ans / 100;
}
int main() {
    int x[6] = {3, 1, 4, 1, 5, 9};
    cout << x[2] << endl;  // line (a)
    cout << x[5/3] << endl; // line (b)
    cout << x[2 * x[3]] << endl; // line (c)
    cout << fun(x, 6, 2) << endl; // line (d)
    cout << fun(x, 4, 3) << endl; // line (e)
}

(a) What is the output at line (a)?
Answer:
4

(b) What is the output at line (b)?
Answer:
1

(c) What is the output at line (c)?
Answer:
4

(d) What is the output at line (d)?
Answer:
0.11

(e) What is the output at line (e)?
Answer:
0.04

Problem 74
Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function that is written only in the designated answer space.

int main() {
    string x[5] = {"CS", "111", "Queens", "College", "CUNY"};
    // (a) Return the average. Here 2.5 is printed.
    cout << average(2, 3) << endl;
    // (b) Return the middle of 3 numbers, here 5 is printed.
    cout << middle(5, 6, 4) << endl;
    // (c) Return the string formed by the first characters of the entries. Here C1QCC.
    cout << initialLetters(x, 5) << endl;
    // (d) Return the first index of an entry containing a target or -1 if not present. Here 2 is printed.
    cout << findIndexContains(x, 5, "ee") << endl;
    // (e) Return the shortest entry. Here print CS
    cout << shortest(x, 5) << endl;
    return 0;
}

Answer:
(a)
double average(int x, int y) {
    return (x + y) / 2.0;
}

(b)

int middle(int x, int y, int z) {
    if (x <= y && y <= z) return y;
    if (y <= z && z <= x) return z;
    return x;
}

(c)

string initialLetters(string x[], int c) {
    string ans = "";
    for (int i = 0; i < c; i++) ans += x[i].substr(0, 1);
    return ans;
}

(d)

int findIndexContains(string array[], int cap, string target) {
    for (int i = 0; i < cap; i++) {
        int x = array[i].find(target);
        if (0 <= x && x < array[i].size()) return i;
    }
    return -1;
}

(e)

string shortest(string x[], int cap) {
    string ans = x[0];
    for (int i = 1; i < cap; i++)
        if (x[i].size() < ans.size()) ans = x[i];
    return ans;
}

Problem 75    Write a complete C++ program that does the following:
It generates random numbers between 1 and 1000. As soon as it generates a number that is larger than the number
right before it, it should print out these two numbers, report the total number of random numbers that have been
generated and end.
Your program should produce output in this form:

530 > 263
Generated 4 Numbers

Random values should be computed with the C++ random number function  rand() .
Excessively long or complicated code may lose points.

Answer:
```cpp
#include <iostream>
#include <cstdlib>
using namespace std;

int main() {
    int last = rand() % 1000 + 1;
    int count = 1;
    while (true) {
        int n = rand() % 1000 + 1;
        count++;
        if (n > last) {
            cout << n << " > " << last << endl;
            cout << "Generated " << count << " Numbers " << endl;
            return 0;
        }
        last = n;
    }
    return 0;
}

Problem 76  Write a function called maxIndex. The function has two array parameters first and second the first is two dimensional with 4 columns and the second is one dimensional. The entries of the two dimensional array are required to be distinct integers. The number of columns in the second array is the number of rows in the first. Additional parameters specify the row and column counts for first. The function sets each entry second[r] to be the index of the column of first for which the entry in row r is biggest.

For instance if first has 3 rows and 4 columns, as follows:

```
99 94 80 16
25 98 82 17
10 11 83 95
```

Then second would be set to store 0, 1, 3. Because the biggest entries in rows 0, 1 and 2 of the table appear in columns 0, 1 and 3.

For example, a program that uses the function follows.

```cpp
int main() {
    int first[3][4] = {{99,94,80,16},{25,98,82,17},{10,11,83,95}};
    int second[3];
    maxIndex(first, second, 3, 4);
    for (int i = 0; i < 3; i++) cout << second[i] << " ";  // prints 0 1 3
    cout << endl;
    return 0;
}
```

Excessively long or complicated code may lose points.

Answer:

```cpp
void maxIndex(int first[][4], int second[], int r, int c) {
    for (int i = 0; i < r; i++) {
        second[i] = 0;
        for (int j = 0; j < c; j++)
            if (first[i][j] > first[i][second[i]])
                second[i] = j;
    }
}
```
Problem 77  Write a function called drop. The function has two integer parameters target that is between 0 and 9 and number that is positive. It returns the number obtained by dropping all copies of the target digit from the number. drop(9, 74949) would drop the two 9 digits and return 744. If parameters have illegal values your function can operate however you choose. Excessively long solutions that use more than 8 lines of code may lose points.

For example, a program that uses the function follows.

```cpp
int main() {
    cout << drop(9, 74949) << endl; // prints 744
    cout << drop(4, drop(9, 74949)) << endl; // prints 7
    cout << drop(4, 444) << endl; // prints 0
    return 0;
}
```

Answer:

```cpp
int drop(int target, int number) {
    if (number == 0) return 0;
    if (number % 10 == target) return drop(target, number / 10);
    return drop(target, number / 10) * 10 + number % 10;
}
```

Problem 78  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```cpp
int main() {
    int x = 0, y = 1, z = 2;
    double w[3] = {1.9, 2.3, 3.0};

    x = a(x + y, z); // (a) sets x as the smaller of two values
    w[0] = b(x, y, y, w[2]); // (b) sets w[0] as the largest of four values
    c(w, y, x); // (c) print the values of w indexed by x and y
    d(w[1], y); // (d) increase y by the nearest integer to w[1]
    d(e(y, z), y); // (e) applies e and then d
    return 0;
}
```

(a) Title line for a.

Answer:

```cpp
int a(int x, int y)
```

(b) Title line for b.

Answer:

```cpp
double b(int x, int y, int z, double w)
```

(c) Title line for c.

Answer:

```cpp
void c(double w[], int x, int y)
```

(d) Title line for d.

Answer:

```cpp
void d(double x, int &y)
```
Problem 79  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
    double x = 0, y = 1, z = 2;
    double w[3] = {1.9, 2.3, 3.0};

    x = f1(x + y, z);  // (a) sets x as the smaller of two values
    w[0] = f2(x, y, y, w[2]);  // (b) sets w[0] as the largest of four values
    f3(w, 3);  // (c) print all values in w
    f4(w[1], y);  // (d) decrease y by w[1]
    f4(f5(y, z), y);  // (e) applies f5 and then f4
    return 0;
}

(a) Title line for f1.
Answer:

double f1(double x, double y)

(b) Title line for f2.
Answer:

double f2(double x, double y, double z, double w)

(c) Title line for f3.
Answer:

void f3(double w[], int c)

(d) Title line for f4.
Answer:

void f4(double x, double &y)

(e) Title line for f5.
Answer:

double f5(double x, double y)

Problem 80  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
    char x = '0', y = '1', z = '2';
    string w[3] = {"1.9", "2.3", "3.0"};

    x = a(x, z);  // (a) sets x as the smaller of two characters
    w[0] = b(x, y, y, w[2]);  // (b) sets w[0] as the concatenation
    c(w, 0, 1);  // (c) prints the concatenation of w[0] and w[1]
    d(w[1], y);  // (d) change y to the first character of w[1]
    d(e(y, z), y);  // (e) applies e and then d
    return 0;
}

(c) Title line for e.
Answer:

double e(int x, int y)
Problem 81  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```c
int main() {
    double x = 0, y = 1, z = 2;
    string w[3] = {"1.9", "2.3", "3.0"};

    x = f1(x + y, z);  // (a) sets x as the smaller of two values
    w[0] = f2(x, y, y, w[2]);  // (b) sets w[0] using the four values
    f3(w, 3);  // (c) print all values in w
    f4(w[1], y);  // (d) decrease y by the numerical value of w[1]
    f4(f5(y, z), y);  // (e) applies f5 and then f4
    return 0;
}
```

(a) Title line for f1.
Answer:

```c
double f1(double x, double y)
```

(b) Title line for f2.
Answer:

```c
string f2(double x, double y, double z, string w)
```

(c) Title line for f3.
Answer:

```c
void f3(string w[], int c)
```

(d) Title line for f4.
Answer:
Problem 82    Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```cpp
int main() {
    int i = 7, j = 8, k = 9;
    double a[3] = {1.1, 1.2, 1.3};
    double b[5] = {1.1, 9.1, 6.1, 8.1, 3.1};
    bool x[2][2] = {{true, true}, {false, true}};
    cout << min(i, j, k) << endl;       // (a) prints: 7
    printMax(b, 5);                     // (b) prints: 9.1
    cout << countFalse2d(x, 2, 2) << endl; // (c) prints: 1 false entry
    swap (i, j);                        // (d) swaps i and j
    swapArrays (a, b, 2);               // (e) swaps first 2 elements of arrays a and b
    return 0;
}
```

(a) Title line for min.
Answer:

```cpp
int min(int x, int y, int z)
```

(b) Title line for printMax.
Answer:

```cpp
void printMax(double x[], int capacity)
```

(c) Title line for countFalse2d.
Answer:

```cpp
string countFalse2d(bool x[][2], int r, int c)
```

(d) Title line for swap.
Answer:

```cpp
void swap(int &x, int &y)
```

(e) Title line for swapArrays.
Answer:

```cpp
void swapArrays(double x[], double y[], int number)
```

Problem 83    Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

int fun(int x) {
    int ans = 23456;
    if (x <= 0) return -1;
```
if ((x >= 5) && (x < 10)) return ans % 1000;
if (x >= 7) return -2;
cout << x / 2;
return fun(x + 1);
}

int main() {
    cout << fun(0) << endl;  // line (a)
    cout << fun(6) << endl;  // line (b)
    cout << fun(7) << endl;  // line (c)
    cout << fun(17) << endl; // line (d)
    cout << fun(3) << endl;  // line (e)
}

(a) What is the output at line (a)?
Answer:
-1

(b) What is the output at line (b)?
Answer:
456

(c) What is the output at line (c)?
Answer:
456

(d) What is the output at line (d)?
Answer:
-2

(e) What is the output at line (e)?
Answer:
12456

Problem 84  Consider the following C++ program.

#include <iostream>
using namespace std;

int fun(int x) {
    int ans = 2345;
    if (x <= 0) return -2;
    if ((x >= 6) && (x < 10)) return ans % 100;
    if (x >= 8) return -5;
    cout << x / 3;
    return fun(x - 1);
}

int main() {
    cout << fun(0) << endl;  // line (a)
    cout << fun(6) << endl;  // line (b)
    cout << fun(7) << endl;  // line (c)
    cout << fun(17) << endl; // line (d)
    cout << fun(3) << endl;  // line (e)
}
Problem 85  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

int fun(int x) {
    int ans = 34567;
    if (x <= 0) return 0;
    if ((x >= 6) && (x < 10)) return ans % 1000;
    if (x >= 8) return -1;
    cout << x % 2;
    return fun(x + 2);
}

int main() {
    cout << fun(0) << endl; // line (a)
    cout << fun(6) << endl; // line (b)
    cout << fun(7) << endl; // line (c)
    cout << fun(17) << endl; // line (d)
    cout << fun(3) << endl; // line (e)
}
```

(a) What is the output at line (a)?

**Answer:**

0

(b) What is the output at line (b)?

**Answer:**

45

(c) What is the output at line (c)?

**Answer:**

45

(d) What is the output at line (d)?

**Answer:**

-5

(e) What is the output at line (e)?

**Answer:**

100-2
(c) What is the output at line (c)?
Answer:
567

(d) What is the output at line (d)?
Answer:
-1

(e) What is the output at line (e)?
Answer:
11567

Problem 86    Consider the following C++ program.

#include <iostream>
using namespace std;

int fun(int x) {
    int ans = 5432;
    if (x <= 0) return -1;
    if ((x >= 8) && (x < 13)) return ans % 100;
    if (x >= 10) return -5;
    cout << x % 3;
    return fun(x + 2);
}

int main() {
    cout << fun(0) << endl;    // line (a)
    cout << fun(6) << endl;    // line (b)
    cout << fun(7) << endl;    // line (c)
    cout << fun(17) << endl;   // line (d)
    cout << fun(3) << endl;    // line (e)
}

(a) What is the output at line (a)?
Answer:
-1

(b) What is the output at line (b)?
Answer:
032

(c) What is the output at line (c)?
Answer:
132

(d) What is the output at line (d)?
Answer:
-5
Problem 87  The following C++ program has errors at the lines marked a,b,c,d, and e. For each answer write a single line of C++ that fixes all errors in the corresponding line. Do not change anything that is correct.

// Program reads integers x and y from an input file called inputFile.txt
// If they are equal, it prints Equal
// Otherwise it prints the smaller one
#include <iostream>
#include <fstream>
using namespace std;

int main() {
    int x, y;
    ifstream f;
    f.open(inputFile.txt); // line a
    f >> x, y; // line b
    if (x = y) cout << "Equal"; // line c
    else if (x < y) cout << x else cout << y; // line d
    cout endl; return; // line e
}

(a) Correct line (a):
Answer:
    f.open("inputFile.txt"); // line a

(b) Correct line (b):
Answer:
    f >> x >> y; // line b

(c) Correct line (c):
Answer:
    if (x == y) cout << "Equal"; // line c

(d) Correct line (d):
Answer:
    else if (x < y) cout << x else cout << y; // line d

(e) Correct line (e):
Answer:
    cout << endl; return 0; // line e
Problem 88  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    int i = 2;
    int x[5] = {3, 1, 4, 1, 5};
    // (a) Return the absolute value (ignoring a minus sign). Here 2 is printed.
    cout << absVal(-2) << endl;
    // (b) Return number of even entries, here 1 is printed.
    cout << numEven(x, 5) << endl;
    // (c) Cube i. Here 8 is printed.
    cubeIt(i); cout << i << endl;
    // (d) Find the (last) index of the smallest entry. Here 3 is printed.
    cout << findIndexMin(x, 5) << endl;
    // (e) Is it a digit? Here print nothing.
    if (isDigit('h')) cout << "Digit" << endl;
    return 0;
}

Answer:
(a)
int absVal(int x) {
    if (x < 0) return -x;
    return x;
}

(b)
int numEven(int array[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (array[i] % 2 == 0) ans++;
    return ans;
}

(c)
void cubeIt(int &x) {
    x = x * x * x;
}

(d)
int findIndexMin(int array[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (array[i] <= array[ans]) ans = i;
    return ans;
}

(e)
bool isDigit(char x) {
    return '0' <= x && x <= '9';
}
Problem 89  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```c++
int main() {
    int i = 2;
    int x[7] = {3, 1, 4, 1, 5, 9, 2};
    // (a) Return the exact quotient. Here 0.4 is printed.
    cout << divide(i, 5) << endl;
    // (b) Return number of odd entries. Here 5 is printed.
    cout << numOdd(x, 7) << endl;
    // (c) Make a number from two copies of a (single) digit. Here 22 is printed.
    cout << doubleIt(2) << endl;
    // (d) Find the last index of the largest entry. Here 5 is printed.
    cout << findIndexMax(x, 7) << endl;
    // (e) Is it a lower case character? Here L is printed.
    if (isLowerCase('h')) cout << "L" << endl;
    return 0;
}

Answer:
(a)

double divide(int x, int y) {
    return x / ((double) y);
}

(b)

int numOdd(int array[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (array[i] % 2 != 0) ans++;
    return ans;
}

(c)

int doubleIt(int x) {
    return 11 * x;
}

(d)

int findIndexMax(int array[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (array[i] >= array[ans]) ans = i;
    return ans;
}

(e)

bool isLowerCase(char x) {
    return 'a' <= x && x <= 'z';
}
```
Problem 90  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    int a = 123, b = 3;
    ifstream f;
    string s = "HELLO";
    f.open("testFile.txt");
    // (a) Tests whether a number has 3 digits, here Yes!
    if (is3digit(a)) cout << "Yes!" " endl;
    // (b) Doubles a string, here HELLOHELLO
    cout << doubleIt(s) " endl;
    // (c) Returns the number of words found in the input file before eof() is true
    cout << countWords(f) " endl;
    // (d) Print middle character of a string that has odd length here L, ignore even lengths
    cout << midChar(s) " endl;
    // (e) swap a and b so that 3,123 is printed
    swap(a, b);
    cout " a " " b " endl;
    return 0;
}

Answer:
(a)
bool is3digit(int x) {
    return (x > 99) && (x < 1000);
}

(b)
string doubleIt(string x) {
    return x + x;
}

(c)
int countWords(ifstream &file) {
    string x; int count = 0;
    while (!file.eof()) {
        file >> x; count++;
    }
    return count;
}

(d)
char midChar(string x) {
    return x[x.length()/2];
}

(e)
void swap(int &x, int &y) {
    int temp = x;
    x = y; y = temp;
}
Problem 91  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    int a = 2, b = 3, c = 4;
    ifstream f;
    string s = "HELLO";
    f.open("testFile.txt");
    // (a) Tests whether a number is even, here Even!
    if (even(c)) cout << "Even!" << endl;
    // (b) Removes first character from a string, here ELLO
    cout << removeFirst(s) << endl;
    // (c) Returns first word read from the input file
    cout << firstWord(f) << endl;
    // (d) Returns last character of a string, here O
    cout << lastChar(s) << endl;
    // (e) Change a,b,c to be c, a, b so here it prints 423
    rotate(a, b, c);
    cout << a << b << c << endl;
    return 0;
}

Answer:
(a)
bool even(int x) {
    return x % 2 == 0;
}

(b)
string removeFirst(string x) {
    return x.substr(1);
}

(c)
string firstWord(ifstream &file) {
    string x;
    file >> x;
    return x;
}

(d)
char lastChar(string x) {
    return x[x.length() - 1];
}

(e)
void rotate(int &x, int &y, int &z) {
    int temp = x;
    x = z;
    z = y;
    y = temp;
}
```
Problem 92  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string fun(int x) {
    string ans = "56789";
    if (x <= 0) return "0";
    if ((x >= 5) && (x < 10)) return ans.substr(x - 3);
    if (x >= 7) return "Error\nError";
    cout << x;
    return fun(x + 1);
}

int main() {
    cout << fun(0) << endl; // line (a)
    cout << fun(6) << endl; // line (b)
    cout << fun(7) << endl; // line (c)
    cout << fun(17) << endl; // line (d)
    cout << fun(3) << endl; // line (e)
}
```

(a) What is the output at line (a)?
Answer:
0

(b) What is the output at line (b)?
Answer:
89

(c) What is the output at line (c)?
Answer:
9

(d) What is the output at line (d)?
Answer:
Error
Error

(e) What is the output at line (e)?
Answer:
34789

Problem 93  Write a complete C++ program that does the following:
1. Asks the user to enter 2 positive integers, \( x \) and \( y \). If either is illegal then the program terminates.
2. Prints all integers \( n \) with \( x \leq n \leq x^2 \) for which the sum of the digits of \( n \) is exactly equal to \( y \).
The numbers printed should appear on separate lines of output. Excessively long solutions (with more than 25 lines of code) may lose points.

For example, the following represents one run of the program:
#include <iostream>
using namespace std;

int main() {
    int x, y;
    cout << "Enter 2 integers : ";
    cin >> x >> y;
    if (x <= 0 || y <= 0) return 0;
    for (int n = x; n <= x * x; n++) {
        int sum = 0, copy = n;
        while (copy > 0) {
            sum += copy % 10;
            copy /= 10;
        }
        if (sum == y) cout << n << endl;
    }
    return 0;
}

Problem 94  Write a complete C++ program that does the following:
1. Asks the user to enter 2 positive integers, x and y. If either is illegal then the program repeatedly asks the user to retype x and y until legal values are given.
2. Prints all integers n with 1 ≤ n ≤ x for which the product of the digits of n is exactly equal to y.
The numbers printed should appear on separate lines of output. Excessively long solutions (with more than 25 lines of code) may lose points.
For example, the following represents one run of the program:
Enter 2 integers : 35 6
6
16
23
32

Answer:

#include <iostream>
using namespace std;

int main() {
    int x, y;
    cout << "Enter 2 integers : ";
    cin >> x >> y;
    while (x <= 0 || y <= 0) {
        cout << "Illegal. Enter 2 positive integers: ";
        cin >> x >> y;
    }
    for (int n = 1; n <= x; n++) {
        int product = 1, copy = n;
        while (copy > 0) {
            product *= copy % 10;
            copy /= 10;
        }
        if (product == y) cout << n << endl;
    }
}
Problem 95  Write a complete C++ program that does the following:
1. Asks the user to enter 2 positive integers, \( x \) and \( y \) for which \( 0 < y \leq 9 \). If either is illegal then the program terminates.
2. Prints all integers \( n \) with \( x \leq n < x^2 \) such that one of the digits of \( n \) is equal to \( y \).
The numbers printed should appear on separate lines of output. Excessively long solutions (with more than 25 lines of code) may lose points.
For example, the following represents one run of the program:

```
Enter 2 integers : 5 2
12
20
21
22
23
24
```

Answer:
```
#include <iostream>
using namespace std;
int main() {
    int x, y;
    cout << "Enter 2 integers : ";
    cin >> x >> y;
    if (x <= 0 || y <= 0 || y > 9) return 0;
    for (int n = x; n < x * x; n++) {
        int count = 0, copy = n;
        while (copy > 0) {
            if (copy % 10 == y) count++;
            copy /= 10;
        }
        if (count > 0) cout << n << endl;
    }
    return 0;
}
```

Problem 96  Write a complete C++ program that does the following:
1. Asks the user to enter 2 positive integers, \( x \) and \( y \) for which \( 0 < y \leq 9 \). If either is illegal then the program should repeatedly as the user to re-enter \( x \) and \( y \).
2. Prints all integers \( n \) with \( 1 \leq n \leq x \) such that all of the digits of \( n \) are at least as large as \( y \).
The numbers printed should appear on separate lines of output. Excessively long solutions (with more than 25 lines of code) may lose points.
For example, the following represents one run of the program:

```
Enter 2 integers : 100 8
8
9
88
89
98
99
```
```cpp
#include <iostream>
using namespace std;

int main() {
    int x, y;
    cout << "Enter 2 integers : ";
    cin >> x >> y;
    while (x <= 0 || y <= 0 || y > 9) {
        cout << "Illegal. try again: ";
        cin >> x >> y;
    }
    for (int n = 1; n <= x; n++) {
        int copy = n;
        bool ok = true;
        while (copy > 0) {
            if (copy % 10 < y) ok = false;
            copy /= 10;
        }
        if (ok) cout << n << endl;
    }
    return 0;
}

Problem 97  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

int main() {
    double a[4] = {1.0, 2.0, -3.0, -4.0};
    double b[4] = {0.5, 1.5, 2.5, 3.5};
    // (a) Return the last digit. Here 7 is printed.
    cout << lastDigit(17) << endl;
    // (b) Return whether "Positive", "Negative" or "Zero". Here Negative is printed.
    cout << positiveOrNegative(-77) << endl;
    // (c) Return the greatest factor. (Assume input at least 2, return 1 for primes.) Here 7 is printed.
    cout << greatestFactor(35) << endl;
    // (d) Test whether all array entries are positive. Here: Not all positive
    if (!allPositive(a, 4)) cout << "Not all positive\n";
    // (e) Swap entries of the two arrays.
    swapArrays(a, b, 4);
    return 0;
}

Answer:

(a)

int lastDigit(int x) {
    return x % 10;
}

(b)

string positiveOrNegative(int x) {
    if (x > 0) return "Positive";
    if (x < 0) return "Negative";
    return "Zero";
}
int greatestFactor(int x) {
    int ans = x - 1;
    while (x % ans != 0) ans--;
    return ans;
}

bool allPositive(double x[], int capacity) {
    for (int i = 0; i < capacity; i++)
        if (x[i] <= 0) return false;
    return true;
}

void swapArrays(double x[], double y[], int capacity) {
    for (int i = 0; i < capacity; i++) {
        double temp = x[i];
        x[i] = y[i];
        y[i] = temp;
    }
}

Problem 98 Write a function called firstDuplicate that reports the first duplicate that it finds in an array of characters. If there is no duplicate your function should return '?' as its answer. Your solution should use no more than 15 lines of code.

For example, a program that uses the function firstDuplicate follows.

int main() {
    char x[7] = {'Q', 'u', 'e', 'e', 'n', 's', 'Q'};
    cout << firstDuplicate(x, 7) << endl; // prints e
    return 0;
}

In this example, the second letter e is the first duplicate found in the array. The duplicate letter Q comes later.

Answer:

char firstDuplicate(char x[], int c) {
    for (int i = 1; i < c; i++)
        for (int j = 0; j < i; j++)
            if (x[i] == x[j]) return x[i];
    return '?';
}

Problem 99 Write a function called firstUnique that reports the first entry that has no duplicate in an array of integers. If there is no such entry your function should return -1 as its answer. Your solution should use no more than 15 lines of code.

For example, a program that uses the function firstUnique follows.
int main() {
    int x[10] = {3, 1, 4, 1, 5, 9, 2, 6, 5, 3};
    cout << firstUnique(x, 10) << endl; // prints 4
    return 0;
}

In this example, first two entries of 3 and 1 have later duplicates, so the result is given by the third entry of 4.
Answer:

int firstUnique(int x[], int c) {
    for (int i = 0; i < c; i++) {
        int count = 0;
        for (int j = 0; j < c; j++)
            if (x[i] == x[j]) count++;
        if (count == 1) return x[i];
    }
    return -1;
}

Problem 100 Write a function called firstUniqueIndex that reports the index of the first entry that has no duplicate in an array of integers. If there is no such entry your function should return -1 as its answer. Your solution should use no more than 15 lines of code.
For example, a program that uses the function firstUniqueIndex follows.

int main() {
    int x[10] = {3, 1, 4, 1, 5, 9, 2, 6, 5, 3};
    cout << firstUniqueIndex(x, 10) << endl; // prints 2
    return 0;
}

In this example, indices 0 and 1 give entries of 3 and 1 that have later duplicates, so the result is the index 2.
Answer:

int firstUniqueIndex(int x[], int c) {
    for (int i = 0; i < c; i++) {
        int count = 0;
        for (int j = 0; j < c; j++)
            if (x[i] == x[j]) count++;
        if (count == 1) return i;
    }
    return -1;
}

Problem 101 Write a function called firstDuplicateIndex that reports the first index that contains a duplicate of an earlier entry in an array of characters. If there is no duplicate your function should return -1 as its answer. Your solution should use no more than 15 lines of code.
For example, a program that uses the function firstDuplicateIndex follows.

int main() {
    char x[7] = {'Q', 'u', 'e', 'e', 'n', 's', 'Q'};
    cout << firstDuplicateIndex(x, 7) << endl; // prints 3
    return 0;
}
In this example, the letter at index $e$ which duplicates the earlier $e$ at index 2.

Answer:

```c
int firstDuplicateIndex(char x[], int c) {
    for (int i = 1; i < c; i++)
        for (int j = 0; j < i; j++)
            if (x[i] == x[j]) return i;
    return -1;
}
```

**Problem 102**  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer $n$ that is between 1 and 18.
2. It repeatedly reads $n$ from the user until the supplied value of $n$ is legal.
3. It prints out a triangular picture (as shown in the diagram, but with $n$ characters in the top row). Along each row the characters to be used is the sequence of uppercase letters $A$, $B$, $C$, $\ldots$, and so on.

Here is an example of how the program should work:

```
Give me an integer between 1 and 18: 5
ABCDE
ABCD
ABC
AB
A
```

Answer:

```c
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 18:";
    cin >> n;
    while (n < 1 || n > 18) {
        cout << "Illegal. Try again: ";
        cin >> n;
    }
    for (int r = n; r >= 1; r--) {
        char out = 'A';
        for (int c = 0; c < r; c++) {
            cout << out;
            out++;
        }
        cout << endl;
    }
}
```

**Problem 103**  Write a function called `biggerDigits` that uses two positive integer parameters with the same number of digits and returns a result of `true` if every digit in the first parameter is bigger than the corresponding digit in the second parameter. Otherwise it returns `false`. If a negative parameter is given, or if parameters with unequal numbers of digits are given your function can return any result of your choosing. Excessively long solutions that use more than 6 lines of code may lose points.

For example, a program that uses the function `biggerDigits` follows.
int main() {
    cout << biggerDigits(987, 123) << endl;       // prints true
    cout << biggerDigits(123, 987) << endl;       // prints false
    cout << biggerDigits(98765, 12345) << endl;  // prints false
    // because the last digit isn’t bigger
    if (biggerDigits(76, 91)) cout << "Hello";    // doesn’t print
    return 0;
}

Answer:

bool biggerDigits(int x, int y) {
    if (x == 0) return true;
    if ((x % 10) <= (y % 10)) return false;
    return biggerDigits(x/10, y/10);
}

Problem 104 Write a function called sameEvens that uses two positive integer parameters with the same number of digits and returns a result of true if the positions of the even digits in the two parameters are identical. Otherwise it returns false. For example, the even digits in both of the numbers 12345 and 98765 occupy the 2\textsuperscript{nd} and 4\textsuperscript{th} positions so that sameEvens(12345, 98765) would return true.

If a negative parameter is given, or if parameters with unequal numbers of digits are given your function can return any result of your choosing. Excessively long solutions that use more than 6 lines of code may lose points.

For example, a program that uses the function sameEvens follows.

int main() {
    cout << sameEvens(987, 123) << endl;       // prints true
    cout << sameEvens(123, 223) << endl;       // prints false
    cout << sameEvens(98765, 12345) << endl;  // prints true
    if (sameEvens(76, 91)) cout << "Hello";    // doesn’t print
    return 0;
}

Answer:

bool sameEvens(int x, int y) {
    if (x == 0) return true;
    if ((x % 2) != (y % 2)) return false;
    return sameEvens(x/10, y/10);
}

Problem 105 Write a function called sumGaps that uses two positive integer parameters with the same number of digits and returns the sum of the gaps between their corresponding digits. For example if the numbers are 646 and 920 the gaps between their digits are 3 (between 6 and 9), 2 (between 4 and 2) and 6 (between 6 and 0).

If a negative parameter is given, or if parameters with unequal numbers of digits are given your function can return any result of your choosing. Excessively long solutions that use more than 6 lines of code may lose points.

For example, a program that uses the function sumGaps follows.

int main() {
    cout << sumGaps(9, 1) << endl;         // prints 8
    cout << sumGaps(123, 987) << endl;    // prints 18
    cout << sumGaps(91, 19) << endl;      // prints 16
    return 0;
}

Answer:
int sumGaps(int x, int y) {
    if (x == 0) return 0;
    if ((x % 10) > (y % 10)) return x % 10 - y % 10 + sumGaps(x/10, y/10);
    return y%10 - x % 10 + sumGaps(x/10, y/10);
}

Problem 106 Write a function called productGaps that uses two positive integer parameters with the same number of digits and returns the product of the gaps between their corresponding digits. For example if the numbers are 646 and 920 the gaps between their digits are 3 (between 6 and 9), 2 (between 4 and 2) and 6 (between 6 and 0).

If a negative parameter is given, or if parameters with unequal numbers of digits are given your function can return any result of your choosing. Excessively long solutions that use more than 6 lines of code may lose points.

For example, a program that uses the function productGaps follows.

int main() {
    cout << productGaps(9, 1) << endl; // prints 8
    cout << productGaps(678, 987) << endl; // prints 3
    cout << productGaps(91, 19) << endl; // prints 64
    return 0;
}

Answer:

int productGaps(int x, int y) {
    if (x == 0) return 1;
    if ((x % 10) > (y % 10)) return (x % 10 - y % 10) * productGaps(x/10, y/10);
    return (y%10 - x % 10) * productGaps(x/10, y/10);
}

Problem 107 Write a function called digitMatch that uses two positive integer parameters with the same number of digits and returns the number of positions where the two parameters have the same digit. If a negative parameter is given, or if parameters with unequal numbers of digits are given your function can return any result of your choosing. Excessively long solutions that use more than 10 lines of code may lose points.

For example, a program that uses the function digitMatch follows.

int main() {
    cout << digitMatch(111, 222) << endl; // prints 0
    cout << digitMatch(111, 212) << endl; // prints 1
    cout << digitMatch(12345, 11335) << endl; // prints 3
    cout << digitMatch(12345, 54321) << endl; // prints 1
    return 0;
}

Answer:

int digitMatch(int x, int y) {
    if (x == 0) return 0;
    int ans = digitMatch(x/10, y/10);
    if (x % 10 == y % 10) return ans + 1;
    return ans;
}

Problem 108 Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.
Problem 109     Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
    int arr1[3] = {1, 2, 3}, arr2[2][2] = {{1, 0}, {2, 4}};
    double d1 = 1.23, d2 = 12.3;
    printLine(arr2, 2, 2);     // (a) prints: 1 0 2 4
    printFancy(arr1, 3);       // (b) prints: 1 * 2 ** 3 ***
    cout << doNothing(i, (int)d1);    // (c) prints: This is a useless function
    switchValues(d1, d2);       // (d) switches the values: now, d1 = 12.3 and d2 = 1.23
    cout << goodDayWishes();    // (e) prints: Have a good day
    return 0;
}

(a) Title line for printLine.
Answer:

```
void printLine(int x[][2], int r, int c)
```

(b) Title line for printFancy.
Answer:

```
void printFancy(int a[], int cap)
```

(c) Title line for doNothing.
Answer:

```
string doNothing(int a, int b)
```

(d) Title line for switchValues.
Answer:

```
void switchValues(double &x, double &y)
```

(e) Title line for goodDayWishes.
Answer:

```
string goodDayWishes()
```
(b) Title line for printMax.
Answer:
void printMax(int a[], int cap)

(c) Title line for firstOne.
Answer:
string firstOne(string a, string b)

(d) Title line for switchValues.
Answer:
void switchValues(string &x, string &y)

(e) Title line for goodDayWishes.
Answer:
void goodDayWishes(int x, int y)

Problem 110 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    string s = "Final", t = "Exam";
    // (a) Prints the array.
    printArray(a, 5); // output: 3 1 4 1 5
    // (b) Finds index of max entry.
    cout << maxIndex(a, 5) << endl; // output: 4
    // (c) Swaps array entries
    swapArrays(a, b, 5); // output: 2 7 1 8 2
    // (d) find piece of t starting at: a (assume a is present).
    cout << cutFrom(t, "a") << endl; // output: am
    // (e) determine whether s or t has more characters
    if (hasMore(s,t)) cout << "s is longer\n";
    return 0;
}
```

Answer:
(a)

```cpp
void printArray(int x[], int c) {
    for (int i = 0; i < c; i++) cout << x[i] << " ";
    cout << endl;
}
```

(b)

```cpp
int maxIndex(int x[], int c) {
    int ans = 0;
    for (int i = 1; i < c; i++)
        if (x[i] > x[ans]) ans = i;
    return ans;
}
```
void swapArrays(int x[], int y[], int c) {
    for (int i = 0; i < c; i++) {
        int temp = x[i];
        x[i] = y[i];
        y[i] = temp;
    }
}

string cutFrom(string x, string target) {
    return x.substr(x.find(target));
}

bool hasMore(string x, string y) {
    return x.length() > y.length();
}

Problem 111 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

int main() {
    int i = 12;
    int x[5] = {3, 1, 4, 1, 5};
    // (a) Return the largest odd factor.
    cout << oddFactor(i) << endl; // output: 3
    // (b) Return the sum of even entries.
    cout << sumEven(x, 5) << endl; // output: 4
    // (c) last digit of i.
    cout << lastDigit(i) << endl; // output: 2
    // (d) Find the (last) index of the smallest entry.
    cout << findIndexMin(x, 5) << endl; // output: 3
    // (e) Is it upper case?
    if (isUpper('h')) cout << "Digit" << endl; // No output here.
    return 0;
}

Answer:
(a)

int oddFactor(int x) {
    if (x % 2 != 0) return x;
    return oddFactor(x / 2);
}

(b)

int sumEven(int array[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (array[i] % 2 == 0) ans += array[i];
    return ans;
}
Problem 112  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

int lastDigit(int x) {
    return x % 10;
}

int findIndexMin(int array[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (array[i] <= array[ans]) ans = i;
    return ans;
}

bool isUpper(char x) {
    return 'A' <= x && x <= 'Z';
}

int func1(double &d, string s) {
    s = "Final Exam";
    d = 13.14 - 3.14;
    cout << "s" << endl;
    return 13 + 1;
}

int func2(int &a, int &b, int c) {
    a = b + c;
    b = 1;
    return c;
}

int main() {
    double piDoubled = 3.14 + 3.14;
    string str = " CSCI ";
    func1(piDoubled, str); // line (a)
    cout << func1(piDoubled , str) << endl; // line (b)
    cout << piDoubled << piDoubled << endl; // line (c)
    int x = 1 , y = 11 ;
    cout << 2 * (func2(x, y, x)) << endl; // line (d)
    cout << x << y << endl; // line (e)
    return 0;
}
```

(a) What is the output at line (a)?

Answer:

```
s
```
Problem 113  Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out 007.

```cpp
#include <iostream>
using namespace std;

int fun(int &x, int y, int &z) {
    y = x;
    x = z;
    z = y;
    cout << z;
    return x;
}

int main(int argc, char *argv[]) {
    int x = 3, y = 1, z = 4;
    fun(x, y, z); cout << endl; // line (a)
    cout << x << y << z << endl; // line (b)
    cout << fun(x, y, z) << endl; // line (c)
    cout << argc << endl; // line (d)
    cout << argv[1] << endl; // line (e)
    return 0;
}
```

(a) What is the output at line (a)?
Answer: 3

(b) What is the output at line (b)?
Answer: 413
(c) What is the output at line (c)?

**Answer:**

43

(d) What is the output at line (d)?

**Answer:**

2

(e) What is the output at line (e)?

**Answer:**

007

**Problem 114** Write a function called *triPrint* that uses the entries of an array of characters to print a triangle. The first row of the triangle has the first entry, the second row the first two entries and so on. Your solution should use no more than 6 lines of code.

For example, a program that uses the function *triPrint* follows.

```cpp
int main() {
    char x[7] = {'c', 's', 'c', 'i', '1', '1', '1'};
    triPrint(x, 7);
    return 0;
}
```

The output from this program would be:

```none
c
cs
csc
csci
csci1
csci11
csci111
```

**Answer:**

```cpp
void triPrint(char x[], int c) {
    for (int r = 1; r <= c; r++) {
        for (int c = 0; c < r; c++) cout << x[c];
        cout << endl;
    }
}
```

**Problem 115** Write a function called *sums* that replaces each entry in an array of integers by the sum of that entry and all earlier entries in the original input array. Your solution should use no more than 6 lines of code.

For example, a program that uses the function *sums* follows.

```cpp
int main() {
    int x[6] = {3, 1, 4, 1, 5, 9};
    sums(x, 6);
    for (int i = 0; i < 6; i++) cout << x[i] << " ";
    cout << endl;
    return 0;
}
```
The output from this program would be:

3 4 8 9 14 23

because, for example 3 + 1 + 4 + 1 + 5 = 14 and 3 + 1 + 4 + 1 + 5 + 9 = 23.

Answer:

```c
void sums(int x[], int c) {
    if (c <= 1) return;
    sums(x, c - 1);
    x[c - 1] += x[c - 2];
}
```

Problem 116 Write a function called swapTwo that has an integer parameter that is at least 10. It returns an integer obtained by swapping the first two digits in the input number. If an argument less than 10 is given your function can return any result of your choosing.

Your function need not use more than 2 instructions. Excessively complicated long solutions that use more than 6 lines of code may lose points.

For example, a program that uses the function swapTwo follows.

```c
int main() {
    cout << swapTwo(19683) << endl; // prints 91683
    cout << swapTwo(10) << endl; // prints 1
    cout << swapTwo(swapTwo(19683)) << endl; // prints 19683
    return 0;
}
```

Answer:

```c
int swapTwo(int x) {
    if (x < 100) return x / 10 + 10 * (x % 10);
    return 10 * swapTwo(x/10) + x % 10;
}
```

Problem 117 Write a function called bigGap that has an integer parameter that is at least 10. It returns an integer that gives the biggest gap between adjacent digits in the input number. If an argument less than 10 is given your function can return any result of your choosing.

Your function need not use more than 6 instructions. Excessively complicated long solutions that use more than 12 lines of code may lose points.

For example, a program that uses the function bigGap follows.

```c
int main() {
    cout << bigGap(19683) << endl; // prints 8 found as the gap in 19
    cout << bigGap(38691) << endl; // prints 8 found as the gap in 91
    return 0;
}
```

Answer:

```c
int bigGap(int x) {
    int lastGap = (x / 10) % 10 - x % 10;
    if (lastGap < 0) lastGap = -lastGap;
    if (x < 100) return lastGap;
    int earlierGap = bigGap(x / 10);
    if (earlierGap > lastGap) return earlierGap;
    return lastGap;
}
```
Problem 118  Write a complete C++ program that does the following:
1. Asks the user to enter 2 integers, \( x \) and \( y \). Both should be between 2 and 10 (inclusive), and if either is illegal then the program terminates.
2. Fills a table (as part of a 2d-array) with characters entered by the user. The table should have as many rows as \( x \) and as many columns as the double of \( y \). The user should enter the characters separated by spaces.
3. Prints the characters in the last column in reverse order without spaces.

For example, the following represents one run of the program:
Enter 2 integers : 3 2
Enter 12 characters : a b c d e f g h i j k l
The characters in the last column (reversed): lhd

Answer:
```c++
#include <iostream>
using namespace std;

int main() {
    int x, y, r, c;
    char table[10][20];
    cout << "Enter 2 integers: ";
    cin >> x >> y;
    if (x < 2 || x > 10 || y < 2 || y > 10) return 0;
    cout << "Enter " << 2 * x * y << " characters: ";
    for (r = 0; r < x; r++)
        for (c = 0; c < 2 * y; c++)
            cin >> table[r][c];
    cout << "The characters in the last column (reversed): ";
    for (r = x - 1; r >= 0; r--)
        cout << table[r][2*y - 1];
    cout << endl;
    return 0;
}
```

Problem 119  Write a complete C++ program that does the following:
1. Asks the user to enter an integer \( x \). It should be between 2 and 10 (inclusive), and if it is illegal then the program terminates.
2. Makes the user to enter \( x \) words (strings) of text, each of which should have at least 4 characters. Any word with fewer characters is replaced by the string "Error".
3. Prints the third character from each word, beginning with the last word and ending with the first.

For example, the following represents one run of the program:
Enter an integer : 3
Enter 3 words: Final Exam CSCI111
The third characters in reverse order: Can

Answer:
```c++
#include <iostream>
using namespace std;

int main() {
    int x, r;
    string words[10];
    cout << "Enter an integer: ";
    cin >> x;
    if (x < 2 || x > 10) return 0;
    cout << "Enter " << x << " words: ";
    for (r = 0; r < x; r++)
        cin >> words[r];
    for (r = x - 1; r >= 0; r--)
        cout << words[r][2];
    cout << endl;
    return 0;
}
cout << "The third characters in reverse order: ";
for (r = x - 1; r >= 0; r--)
    cout << words[r][2];
cout << endl;
return 0;
}

Problem 120 Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
    int x = 2, y = 3, z[4];
    bool a = true, b = false, c[4];
    string s = "Hello", t = "goodbye", u[4][5];
    for (int i = 0; i < 4; i++) c[i] = data(x, y, 2.5); // (a)
setToFive(z, c, 4); cout << z[1] << endl; // (b) prints 5
y = speedLimit(x, z[1]); cout << x << y << endl; // (c) prints 55
cout << numberStrings(4, u, 5) << endl; // (d) prints 20
f(numberStrings(0, u, 0), data(y, x, f(20, a || b))); // (e)
return 0;
}

(a) Title line for data.
Answer:
bool data(int x, int y, double z)

(b) Title line for setToFive.
Answer:
void setToFive(int a[], bool b[], int cap)

(c) Title line for speedLimit.
Answer:
int speedLimit(int &a, int b)

(d) Title line for numberStrings.
Answer:
int numberStrings(int a, string b[][5], int c)

(e) Title line for f.
Answer:
double f(int a, bool b)

Problem 121 Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
    int a = 2, b = 3, c[4];
    bool s = true, t = false, u[4];
    string x = "Hello", y = "goodbye", z[4][5];
    for (int i = 0; i < 4; i++) c[i] = data(x, y, 2.5); // (a)
setToFive(z, c, 4); cout << z[1][1] << endl; // (b) prints 5
y = speedLimit(x, z[1][1]); cout << x << y << endl; // (c) prints 55
cout << numberStrings(s, t, b, u) << endl; // (d) prints 20
numberStrings(f(a), f(a), a, u); // (e)
return 0;
}
Problem 122  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```cpp
int main() {
    int x = 2, z[3] = {3, 1, 4};
    bool a = true, c[5];
    string s = "Hello", u[7][9];
    for (int i = 0; i < 4; i++) c[i] = A(x, x, 2.5);  // (a)
    cout << B(c, c, u);  // (b) prints: part B
    x = C(x, u[1][1]); cout << x << endl;  // (c) prints 55
    D(4, z, 5); cout << z[1] << endl;  // (d) prints 3
    E(E(a, s), s); cout << endl;  // (e) prints 33
    return 0;
}
```

(a) Title line for A.
Answer:

```
bool A(int x, int y, double z)
```

(b) Title line for B.
Answer:

```
string B(bool a[], bool b[], string[][9])
```

(c) Title line for C.
Answer:

```
int C(int a, string b)
```

(d) Title line for D.
Answer:
void D(int a, int b[], int c)

(c) Title line for E.

Answer:

bool E(bool a, string b)

**Problem 123** Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```cpp
int main() {
    int a = 2, c[3] = {3, 1, 4};
    bool s = true, u[5];
    string x = "Hello", z[7][9];
    for (int i = 0; i < 4; i++) c[i] = A(x, x, 2.5); // (a)
    cout << B(c, c, u); // (b) prints: part B
    x = C(x, u[1]); cout << x << endl; // (c) prints 55
    D(4, z, 5); cout << z[1][1] << endl; // (d) prints 3
    E(E(a, s), s); cout << endl; // (e) prints 33
    return 0;
}
```

(a) Title line for A.

Answer:

```cpp
int A(string x, string y, double z)
```

(b) Title line for B.

Answer:

```cpp
string B(int a[], int b[], bool[])
```

(c) Title line for C.

Answer:

```cpp
string C(string a, bool b)
```

(d) Title line for D.

Answer:

```cpp
void D(int a, string b[][9], int c)
```

(e) Title line for E.

Answer:

```cpp
int E(int a, bool b)
```

**Problem 124** Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

int F(int x[], int c) {
    if (c < 3) return 0;
    return x[c - 1] + F(x, c - 1);
}
```
int G(int a, int &b) {
    b = b - a;
    a = b + a;
    return a;
}

int main() {
    int a = 4, b = 1;
    int x[5] = {3, 1, 4, 1, 5};
    string s = "Problem Number 2";
    cout << x[2 + 2] + x[2] << endl; // line (a)
    cout << s.substr(2, 3) << endl; // line (b)
    cout << s.substr(s.find("b")) << endl; // line (c)
    cout << G(b, a); cout << a << b << endl; // line (d)
    cout << F(x, 5) << endl; // line (e)
    return 0;
}

(a) What is the output at line (a)?
Answer:
9
(b) What is the output at line (b)?
Answer:
obl
(c) What is the output at line (c)?
Answer:
bblem Number 2
(d) What is the output at line (d)?
Answer:
431
(e) What is the output at line (e)?
Answer:
10

Problem 125  Consider the following C++ program.

#include <iostream>
using namespace std;

int F(int x[], int c) {
    if (c < 1) return 0;
    return x[c - 1] + F(x, c - 1);
}

int G(int &a, int b) {
    b = b - a;
    a = b + a;
int main() {
    int a = 7, b = 5;
    int x[5] = {3, 1, 4, 1, 5};
    string s = "String Question";
    cout << x[2 / 2] * x[2] << endl;  // line (a)
    cout << s.substr(2, 3) << endl;    // line (b)
    cout << s.substr(s.rfind("s")) << endl; // line (c)
    cout << G(b, a); cout << a << b << endl; // line (d)
    cout << F(x, 4) << endl;          // line (e)
    return 0;
}

(a) What is the output at line (a)?
Answer:
4

(b) What is the output at line (b)?
Answer:
rin

(c) What is the output at line (c)?
Answer:
ston

(d) What is the output at line (d)?
Answer:
777

(e) What is the output at line (e)?
Answer:
9

Problem 126  Consider the following C++ program.

#include <iostream>
using namespace std;

int F(int a, int &b) {
    b = b - a;
    a = b + a;
    return a;
}

int G(int x[], int c) {
    if (c < 3) return 0;
    return x[c - 1] + G(x, c - 1);
}
int main() {
    int a = 5, b = 3;
    int x[5] = {2, 7, 1, 8, 2};
    string s = "Final Exam";
    cout << x[2 + 2] + x[2] << endl; // line (a)
    cout << s.substr(2, 3) << endl; // line (b)
    cout << s.substr(s.find("a")) << endl; // line (c)
    cout << F(b, a); cout << a << b << endl; // line (d)
    cout << G(x, 5) << endl; // line (e)
    return 0;
}

(a) What is the output at line (a)?
Answer:
3

(b) What is the output at line (b)?
Answer:
 nal

(c) What is the output at line (c)?
Answer:
al Exam

(d) What is the output at line (d)?
Answer:
523

(e) What is the output at line (e)?
Answer:
11

Problem 127 Consider the following C++ program.

#include <iostream>
using namespace std;

int F(int &a, int b) {
    b = b - a;
    a = b + a;
    return a;
}

int G(int x[], int c) {
    if (c < 1) return 0;
    return x[c - 1] + G(x, c - 1);
}

int main() {
    int a = 6, b = 4;
    int x[5] = {2, 7, 1, 8, 2};
Problem 128  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    int a[2][4] = {{1, 2, 3, 4}, {0, 1, 2, 3}};
    int b[4] = {3, 1, 4, 1};
    int x = 1, y = 2;
    string s = "hello";
    // (a) Return true if at least one of x and y is positive. Here Yes is printed
    if (positive(x, y)) cout << "Yes" << endl;
    // (b) Return the sum of the first row. Here 10 is printed.
    cout << rowSum(a, 2, 4) << endl;
    // (c) Return the smallest element. Here 1 is printed.
    cout << smallest(b, 4) << endl;
    // (d) Remove the first letter. Here ello is printed.
    cout << removeFirst(s) << endl;
    // (e) Insert an X at the specified position. Here heXllo is printed.
    addX(s, 2);
    cout << s << endl;
    return 0;
}
```
Answer:

(a)

```cpp
bool positive(int x, int y) {
    return x > 0 || y > 0;
}
```

(b)

```cpp
int rowSum(int a[][4], int r, int c) {
    int ans = 0;
    for (int j = 0; j < c; j++)
        ans += a[0][j];
    return ans;
}
```

(c)

```cpp
int smallest(int x[], int c) {
    int ans = x[0];
    for (int i = 0; i < c; i++)
        if (x[i] < ans) ans = x[i];
    return ans;
}
```

(d)

```cpp
string removeFirst(string s) {
    return s.substr(1);
}
```

(e)

```cpp
void addX(string &s, int y) {
    s.insert(y, "X");
}
```

Problem 129

Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    int a[2][4] = {{1, 2, 3, 4}, {0, 1, 2, 3}};
    int b[4] = {3, 1, 4, 1};
    int x = 1, y = 2;
    string s = "hello";
    // (a) Return true if both of x and y are positive. Here Yes is printed
    if (positive(x, y)) cout << "Yes" << endl;
    // (b) Return the sum of the second row. Here 6 is printed.
    cout << rowSum(a, 2, 4) << endl;
    // (c) Return the largest element. Here 4 is printed.
    cout << largest(b, 4) << endl;
    // (d) Return the first two letters. Here he is printed.
    cout << firstTwo(s) << endl;
    // (e) Insert a specified number of X’s at the end. Here helloXX is printed.
```
addX(s, 2);
cout << s << endl;
return 0;
}

Answer:
(a)

bool positive(int x, int y) {
    return x > 0 && y > 0;
}

(b)

int rowSum(int a[][4], int r, int c) {
    int ans = 0;
    for (int j = 0; j < c; j++)
        ans += a[1][j];
    return ans;
}

(c)

int largest(int x[], int c) {
    int ans = x[0];
    for (int i = 0; i < c; i++)
        if (x[i] > ans) ans = x[i];
    return ans;
}

(d)

string firstTwo(string s) {
    return s.substr(0, 2);
}

(e)

void addX(string &s, int y) {
    for (int i = 0; i < y; i++) s = s + "X";
}

Problem 130 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

int main() {
    int x = 1, y = 2;
    string a[2][3] = {"CS", "111", "Final"}, {"Question", "number", "3"};
    // (a) Return true if at least one of x and y is negative. Here nothing is printed
    if (negative(x, y)) cout << "Yes" << endl;
    // (b) Return the first entry in the first row. Here CS is printed.
    cout << firstEntry(a, 2, 3) << endl;
    // (c) Return the longest element. Here Problem is printed.
cout << longest(b, 3) << endl;  // (d) Remove the first letter. Here number is printed.
cout << removeFirst(a[1][1]) << endl;  // (e) Insert a Q at the specified position of a string. Here CQS is printed.
addQ(a[0][0], 1);
cout << a[0][0] << endl;
return 0;
}

Answer:
(a)

bool negative(int x, int y) {
    return x < 0 || y < 0;
}

(b)

string firstEntry(string a[], int r, int c) {
    return a[0][0];
}

(c)

string longest(string x[], int c) {
    string ans = x[0];
    for (int i = 0; i < c; i++)
        if (x[i].length() > ans.length()) ans = x[i];
    return ans;
}

(d)

string removeFirst(string s) {
    return s.substr(1);
}

(e)

void addQ(string &s, int y) {
    s.insert(y, "Q");
}

Problem 131 Write blocks of code to perform the functions used in the following main program. Your blocks
must match the given title lines. Each block should be a short function of only a few lines.

int main() {
    int x = 1, y = 2;
    string a[2][3] = {"CS", "111", "Final"}, {"Question", "number", "3"};
    // (a) Return true if both of x and y are negative. Here nothing is printed
    if (negative(x, y)) cout << "Yes" << endl;
    // (b) Return the first entry in the second column. Here 111 is printed.
cout << firstEntry(a, 2, 3) << endl;
}
// (c) Return the shortest element. Here An is printed.
    cout << shortest(b, 3) << endl;
// (d) Return the first two letters. Here Fi is printed.
    cout << firstTwo(a[0][2]) << endl;
// (e) Insert the specified number of Qs at the start of a string. Here QQCS is printed.
    addQ(a[0][0], 2);
    cout << a[0][0] << endl;
    return 0;
}

Answer:
(a)

    bool negative(int x, int y) {
        return x < 0 && y < 0;
    }

(b)

    string firstEntry(string a[][3], int r, int c) {
        return a[0][1];
    }

(c)

    string shortest(string x[], int c) {
        string ans = x[0];
        for (int i = 0; i < c; i++)
            if (x[i].length() < ans.length()) ans = x[i];
        return ans;
    }

(d)

    string firstTwo(string s) {
        return s.substr(0, 2);
    }

(e)

    void addQ(string &s, int y) {
        for (int i = 0; i < y; i++)
            s = "Q" + s;
    }

Problem 132 Write a function called randFill that fills the entries of an array with random integers in the range from 10 to 99 (inclusive). (You should use the rand function to generate the values. You do not need to call srand. Your solution should use no more than 6 lines of code.)
For example, a program that uses the function randFill follows.

    int main() {
        int x[5];
randFill(x, 5);
for (int i = 0; i < 5; i++)
    cout << x[i] << " "; // prints 5 random numbers
    cout << endl; // such as 93 73 12 69 40
return 0;
}

Problem 133 Write a function called randAdd that changes each entry of an array by generating a random integer between 1 and 10 and adding it to the entry. (You should use the rand function to generate the values. You do not need to call srand. Your solution should use no more than 6 lines of code.)
For example, a program that uses the function randAdd follows.

int main()
{
    int x[5] = {3, 1, 4, 1, 5};
rndAdd(x, 5);
for (int i = 0; i < 5; i++)
    cout << x[i] << " "; // prints 5 randomly adjusted entries
    cout << endl; // such as 93 73 12 69 40
return 0;
}

Answer:
#include <cstdlib>

void randAdd(int x[], int cap) {
    for (int i = 0; i < cap; i++)
        x[i] += rand() % 10 + 1;
}

Problem 134 Write a function called maxIndex that reports the index of a row that contains the largest entry in a 2-dimensional array of integers (with 3 columns).
For example, a program that uses the function maxIndex follows.

int maxIndex(int x[][3], int r, int c) {
int a = 0, b = 0;
for (int i = 0; i < r; i++)
    if (x[i][2] > x[b][2])
        b = i;
return b;
}
for (int i = 0; i < r; i++)
  for (int j = 0; j < c; j++)
    if (x[i][j] > x[a][b]) {
      a = i;
      b = j;
    }
  return a;
}

Problem 135     Write a function called maxIndex that reports the index of a column that contains the largest entry in a 2-dimensional array of integers (with 3 columns).
For example, a program that uses the function maxIndex follows.

int main() {
  int x[3][3] = {{3,1,4},{1,5,9}, {2,6,5}};
  cout << maxIndex(x, 3, 3) << endl; // prints 2
     // because the entry 9 is in column 2
  return 0;
}

Answer:

int maxIndex(int x[][3], int r, int c) {
  int a = 0, b = 0;
  for (int i = 0; i < r; i++)
    for (int j = 0; j < c; j++)
      if (x[i][j] > x[a][b]) {
        a = i;
        b = j;
      }
  return b;
}

Problem 136     Write a function called evenUp that returns the result of increasing the first even digit in a positive integer parameter by 1. (Your solution should use no more than 10 lines of code. Your function can return any convenient value of your choice if the parameter is not positive.)
For example, a program that uses the function evenUp follows.

int main() {
  cout << evenUp(1232) << endl; // prints 1332 only the first even 2 changes
  cout << evenUp(1332) << endl; // prints 1333
  cout << evenUp(1333) << endl; // prints 1333 no even digit to change
  cout << evenUp(22) << endl;   // prints 32
  cout << evenUp(2) << endl;    // prints 3
  return 0;
}

Answer:

int evenUp(int x) {
  if (x <= 0) return 0;
  int y = evenUp(x / 10);
  if (x % 2 == 1) return 10 * y + x % 10;
  if (y > x / 10) return 10 * y + x % 10;
  return x + 1;
}
Problem 137  Write a function called \textit{oddDown} that returns the result of decreasing the first odd digit in a positive integer parameter by 1. (Your solution should use no more than 10 lines of code. Your function can return any convenient value of your choice if the parameter is not positive.)

For example, a program that uses the function \textit{oddDown} follows.


text

int main() {
    cout << oddDown(321) << endl;  // prints 221 only the first odd digit changes
    cout << oddDown(221) << endl;  // prints 220
    cout << oddDown(220) << endl;  // prints 220 because no odd digit to decrease
    cout << oddDown(7) << endl;    // prints 6
    cout << oddDown(6) << endl;    // prints 6
    return 0;
}

Answer:

int oddDown(int x) {
    if (x <= 0) return 0;
    int y = oddDown(x / 10);
    if (x % 2 == 0) return 10 * y + x % 10;
    if (y < x / 10) return 10 * y + x % 10;
    return x - 1;
}

Problem 138  Write a function called \textit{evenUp} that returns the result of increasing the last even digit in a positive integer parameter by 1. (Your solution should use no more than 5 lines of code. Your function can return any convenient value of your choice if the parameter is not positive.)

For example, a program that uses the function \textit{evenUp} follows.


text

int main() {
    cout << evenUp(1234) << endl;  // prints 1235
    cout << evenUp(1335) << endl;  // prints 1335
    cout << evenUp(2) << endl;     // prints 3
    cout << evenUp(3) << endl;     // prints 3
    return 0;
}

Answer:

int evenUp(int x) {
    if (x % 2 == 0) return x + 1;
    if (x < 10) return x;
    return 10 * evenUp(x / 10) + x % 10;
}

Problem 139  Write a function called \textit{oddDown} that returns the result of decreasing the last odd digit in a positive integer parameter by 1. (Your solution should use no more than 5 lines of code. Your function can return any convenient value of your choice if the parameter is not positive.)

For example, a program that uses the function \textit{oddDown} follows.


text

int main() {
    cout << oddDown(3234) << endl;  // prints 3224
    cout << oddDown(3224) << endl;  // prints 2224
}
cout << oddDown(1214) << endl;  // prints 1204
cout << oddDown(1204) << endl;  // prints 204
cout << oddDown(2) << endl;    // prints 2
cout << oddDown(1) << endl;    // prints 0
return 0;
}

Answer:

int oddDown(int x) {
    if (x % 2 == 1) return x - 1;
    if (x < 10) return x;
    return 10 * oddDown(x / 10) + x % 10;
}

Problem 140  Write a complete C++ program that is to be used for a psychology study into random number choices by a human volunteer. Your program is to operate as follows. (Programs that correctly carry out some of the tasks will receive partial credit. Your program should not be more than 30 lines long.)
Ask the user (the volunteer) to repeatedly type 2 digit numbers onto the screen.
Read the user input and discard any number that is less than 10 or greater than 99, but keep track of numbers within this range.
When the total of the legal numbers typed exceeds 100000 the experiment ends and the program prints a summary with the following form (with one line of output for each of the numbers from 10 to 99):

User chose 99 for 2.1% of choices.
User chose 98 for 0.7% of choices.
User chose 97 for ...

Answer:

#include <iostream>
using namespace std;

int main() {
    int n = 0, total = 0, x;
    int counts[100];
    for (int i = 0; i < 100; i++)
        counts[i] = 0;
    while (total <= 100000) {
        cout << "Enter a 2 digit number: ";
        cin >> x;
        if (10 <= x && x <= 99) {
            counts[x]++;
            total += x;
            n++;
        }
    }
    for (x = 99; x >= 10; x--)
        cout << "User chose " << x << " for " << 100.0 * counts[x] / n << "% of choices.\n";
}

Problem 141  Write a complete C++ program that is to be used for a psychology study into random number choices by a human volunteer. Your program is to operate as follows. (Programs that correctly carry out some of the tasks will receive partial credit. Your program should not be more than 30 lines long.)
Ask the user (the volunteer) to repeatedly type single digit numbers onto the screen.
Read the user input and discard any number that is less than 1 or greater than 9, but keep track of numbers within this range.

When the total of the legal numbers typed exceeds 10000 the experiment ends and the program prints a list of the most frequent choice (or choices if two or more numbers are tied).

Output should appear as:

The most frequent choice(s): 3 7

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int total = 0, x, max = 0;
    int counts[10];
    for (int i = 0; i < 10; i++)
        counts[i] = 0;
    while (total <= 10000) {
        cout << "Enter a single digit number: ";
        cin >> x;
        if (1 <= x && x <= 9) {
            counts[x]++;
            total += x;
        }
    }
    for (x = 1; x <= 10; x++)
        if (counts[x] > max) max = counts[x];
    cout << "The most frequent choice(s): ";
    for (x = 1; x <= 10; x++)
        if (counts[x] == max) cout << x << " ";
    cout << endl;
}
```

Problem 142 Write a complete C++ program that is to be used for a marketing study into cent values that appear in gas prices. Your program is to operate as follows. (Programs that correctly carry out some of the tasks will receive partial credit. Your program should not be more than 30 lines long.)

Ask the user to repeatedly type numbers in the range 0 to 99 (representing cents in prices observed) onto the screen.

Read the user input and discard any number that is out of range. As soon as every possible cent value has been seen at least once, the program ends by printing a summary with the following form (with one line of output for each of the numbers from 0 to 99):

99 cents for 12.1% of prices.
98 cents for 0.7% of prices.
97 cents for 0.35% of ...

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int numberOfValues = 0, total = 0, x;
    int counts[100];
    for (int i = 0; i < 100; i++)
        counts[i] = 0;
    while (numberOfValues < 100) {
```
Problem 143 Write a complete C++ program that is to be used for an economics study into mortgage interest rates. Your program is to operate as follows. (Programs that correctly carry out some of the tasks will receive partial credit. Your program should not be more than 30 lines long.)

Ask the user to repeatedly type integers in the range 0 to 8 (representing interest rates observed) onto the screen. Read the user input and discard any number that is out of range. As soon as every possible input value has been seen at least once, the program ends by showing the most frequent rate (or rates in case of a tie). For example, output might be:

Most common rate(s): 3 4

Answer:

```
#include <iostream>
using namespace std;

int main() {
    int numberOfValues = 0, x, max = 0;
    int counts[9];
    for (int i = 0; i < 9; i++)
        counts[i] = 0;
    while (numberOfValues < 9) {
        cout << "Enter a number between 0 and 8: ";
        cin >> x;
        if (0 <= x && x <= 8) {
            if (counts[x] == 0) numberOfValues++;
            counts[x]++;
        }
    }
    for (x = 0; x < 9; x++)
        if (counts[x] > max) max = counts[x];
    cout << "Most common rate(s): ";
    for (x = 0; x < 9; x++)
        if (counts[x] == max)
            cout << x << " ";
    cout << endl;
}
```

Problem 144 Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```
int main() {
    double x = 0.0, y = 3.1, z = 2.5;
    int array[5] = {3,1,4,1,5};
    string s;
```
Problem 145 Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
    int x = 0, y = 3, z = 2;
    char array[5] = {'a','b','c','d','e'};
    string s;

    cout << biggest(x, y, z) << endl; // (a) prints biggest: 3
    x = increase(x); cout << x << endl; // (b) prints 1
    s = printBoth(y, z); cout << s << endl; // (c) prints 3 2
    allOf(array, 5); // (d) prints a b c d e
    upper(array, 5); allOf(array, 5); // (e) prints A B C D E
    return 0;
}

(a) Title line for biggest.
Answer:

int biggest(int a, int b, int c)

(b) Title line for increase.
Answer:

void increase(double &x)
int increase(int x)

(c) Title line for printBoth.
Answer:

string printBoth(int a, int b)

(d) Title line for allOf.
Answer:

void allOf(char a[], int cap)

(e) Title line for upper.
Answer:

void upper(char x[], int cap)

Problem 146  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
    int x = 0, y = 3, z = 2;
    string array[5] = {"A","B","C","D","E"};
    string s;

    cout << least(x, y, z) << endl;       // (a) prints least: 0
    x = decrease(y); cout << x << " " << y << endl;   // (b) prints 2 2
    s = printBoth(z, z); cout << s << endl;          // (c) prints 2 2
    allOf(array, 5);                           // (d) prints A B C D E
    lower(array, 5); allOf(array,5);            // (e) prints a b c d e
    return 0;
}

(a) Title line for least.
Answer:

int least(int a, int b, int c)

(b) Title line for decrease.
Answer:

int decrease(int &x)

(c) Title line for printBoth.
Answer:

string printBoth(int a, int b)

(d) Title line for allOf.
Answer:

void allOf(string a[], int cap)

(e) Title line for lower.
Answer:

void lower(string x[], int cap)
Problem 147 Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```cpp
int main() {
    double x = 0.0, y = 3.1, z = 2.5;
    int array[5] = {3,1,4,1,5};
    string s;

cout << second(x, x, z) << endl;                   // (a) prints second value 0.0
increase(x); cout << x << endl;                   // (b) prints 1.0
printBoth(y, z);                                  // (c) prints 3.1 2.5
s = allOf(array, 5); cout << s << endl;           // (d) prints 3 1 4 1 5
rotate(array, 5); cout << allOf(array, 5) << endl; // (e) prints 1 4 1 5 3
return 0;
}
```

(a) Title line for `second`.

**Answer:**

double second(double a, double b, double c)

(b) Title line for `increase`.

**Answer:**

void increase(double &x)

(c) Title line for `printBoth`.

**Answer:**

void printBoth(double a, double b)

(d) Title line for `allOf`.

**Answer:**

string allOf(int a[], int cap)

(e) Title line for `rotate`.

**Answer:**

void rotate(int x[], int cap)

Problem 148 Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string fun(string x) {
    if (x.length() <= 4) {
        return "00";
    }
    return fun(x.substr(4)) + x.substr(4);
}

int main() {
    int x = 43;
    int y = x / 10;
    cout << x / 10 + x % 10 << endl;                   // line (a)
    if (((x > 40) || (x < 50)) && ((y > 4) || (y < 5)))
```
Problem 149  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string fun(string x) {
    if (x.length() <= 4) {
        return "XX";
    }
    return fun(x.substr(3)) + x.substr(4);
}

int main() {
    int x = 34;
    int y = x / 10;
    cout << x % y << endl;  // line (b)
    cout << fun("Easy") << endl;  // line (c)
    cout << fun("12345") << endl;  // line (d)
    cout << fun("123456789") << endl;  // line (e)
    cout << x / 10 + x % 10 << endl;  // line (a)
    if (((x > 30) && (x < 50)) || ((y > 3) && (y < 5)))
        cout << x % y << endl;  // line (b)
    cout << fun("Easy") << endl;  // line (c)
    cout << fun("ABCDE") << endl;  // line (d)
    cout << fun("ABCDEF") << endl;  // line (e)
}
```

(a) What is the output at line (a)?

Answer:

7

(b) What is the output at line (b)?

Answer:

3

(c) What is the output at line (c)?

Answer:

00

(d) What is the output at line (d)?

Answer:

005

(e) What is the output at line (e)?

Answer:

00956789
(b) What is the output at line (b)?
**Answer:**
1

(c) What is the output at line (c)?
**Answer:**
XX

(d) What is the output at line (d)?
**Answer:**
XXE

(e) What is the output at line (e)?
**Answer:**
XXEFG

**Problem 150**   Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string fun(string x) {
    if (x.length() <= 5) {
        return "00";
    }
    return fun(x.substr(5, 1)) + x.substr(5, 1);
}

int main() {
    int x = 78;
    string y = "Hello";
    cout << x / 10 + x % 10 << endl; // line (a)
    cout << y.find("l") << endl; // line (b)
    cout << fun("Easy") << endl; // line (c)
    cout << fun("234567") << endl; // line (d)
    cout << fun("23456789") << endl; // line (e)
}
```

(a) What is the output at line (a)?
**Answer:**
15

(b) What is the output at line (b)?
**Answer:**
2

(c) What is the output at line (c)?
**Answer:**
XX

(d) What is the output at line (d)?
**Answer:**
XXE

(e) What is the output at line (e)?
**Answer:**
XXEFG
(d) What is the output at line (d)?
Answer:

XX

(e) What is the output at line (e)?
Answer:

XXas
Problem 152 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    int a[4] = {1, 2, -3, -4};
    int x = 5, y = 6;
    // (a) Return the cube. Here 8 is printed.
    cout << cube(2) << endl;
    // (b) Return the larger number. Here 6 is printed.
    cout << larger(x, y) << endl;
    // (c) Return the largest element. Here 2 is printed.
    cout << largest(a, 4) << endl;
    // (d) Test whether all array entries are positive. Here: Not all positive
    if (!allPositive(a, 4)) cout << "Not all positive\n";
    // (e) Swap values. Here -3 is printed.
    swap(a[2], x);
    cout << x << endl;
    return 0;
}
```

Answer:

(a)

```cpp
int cube(int x) {
    return x * x * x;
}
```

(b)

```cpp
int larger(int x, int y) {
    if (x > y) return x;
    return y;
}
```

(c)

```cpp
int largest(int x[], int cap) {
    int ans = x[0];
    for (int i = 0; i < cap; i++)
        if (x[i] > ans) ans = x[i];
    return ans;
}
```

(d)

```cpp
bool allPositive(int x[], int capacity) {
    for (int i = 0; i < capacity; i++)
        if (x[i] <= 0) return false;
    return true;
}
```

(e)
Problem 153  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```c
int main() {
    int a[4] = {1, 2, -3, -4};
    int x = 5, y = 6;
    // (a) Return the cube. Here 8.0 is printed.
    cout << cube(2.0) << endl;
    // (b) Print the larger number. Here 6 is printed.
    larger(x, y);
    // (c) Return the first negative element, or 0 if there is none. Here -3 is printed.
    cout << firstNegative(a, 4) << endl;
    // (d) Test whether array entries increase in size. Here: Not increasing
    if (!increasing(a, 4)) cout << "Not increasing\n";
    // (e) Swap values. Here 6 is printed.
    swap(y, x);
    cout << x << endl;
    return 0;
}
```

Answer:

(a)

```c
double cube(double x) {
    return x * x * x;
}
```

(b)

```c
void larger(int x, int y) {
    if (x > y) cout << x << endl;
    else cout << y << endl;
}
```

(c)

```c
int firstNegative(int x[], int cap) {
    for (int i = 0; i < cap; i++)
        if (x[i] < 0) return x[i];
    return 0;
}
```

(d)

```c
bool increasing(int x[], int capacity) {
    for (int i = 1; i < capacity; i++)
        if (x[i - 1] >= x[i]) return false;
    return true;
}
```
Problem 154  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```c
int main() {
    int a[4] = {3, 2, -3, -4};
    double x = 5.0, y = 6.0;
    // (a) Return the cube. Here 8.0 is printed.
    cout << cube(2.0) << endl;
    // (b) Print the larger number. Here 6.0 is printed.
    larger(x, y);
    // (c) Return the last positive element, or 0 if there is none. Here 2 is printed.
    cout << lastPositive(a, 4) << endl;
    // (d) Test whether array entries decrease in size. Here: decreasing
    if (decreasing(a, 4)) cout << "Decreasing\n";
    // (e) Swap values. Here 2 is printed.
    swap(a[0], a[1]);
    cout << a[0] << endl;
    return 0;
}
```

Answer:

(a)

```c
double cube(double x) {
    return x * x * x;
}
```

(b)

```c
void larger(double x, double y) {
    if (x > y) cout << x << endl;
    else cout << y << endl;
}
```

(c)

```c
int lastPositive(int x[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (x[i] > 0) ans = x[i];
    return ans;
}
```

(d)

```c
bool decreasing(int x[], int capacity) {
```
for (int i = 1; i < capacity; i++)
    if (x[i - 1] <= x[i]) return false;
return true;
}

void swap(int &x, int &y) {
    int temp = x;
    x = y;
    y = temp;
}

Problem 155  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

int main() {
    int a[4] = {3, 2, -3, -4};
    int x = 7, y = 6;
    // (a) Return the cube. Here 8 is printed.
    cout << cube(2) << endl;
    // (b) Is x larger than y?. Here YES is printed.
    if (larger(x, y)) cout << "YES" << endl;
    // (c) Return the smallest element. Here -4 is printed.
    cout << smallest(a, 4) << endl;
    // (d) Test whether all array entries are negative. Here: Not all negative
    if (!allNegative(a, 4)) cout << "Not all negative\n";
    // (e) Swap values. Here -3 is printed.
    swap(a[2], x);
    cout << x << endl;
    return 0;
}

Answer:
(a)
int cube(int x) {
    return x * x * x;
}

(b)
bool larger(int x, int y) {
    return x > y;
}

(c)
int smallest(int x[], int cap) {
    int ans = x[0];
    for (int i = 0; i < cap; i++)
        if (x[i] < ans) ans = x[i];
    return ans;
}
bool allNegative(int x[], int capacity) {
    for (int i = 0; i < capacity; i++)
        if (x[i] >= 0) return false;
    return true;
}

void swap(int &x, int &y) {
    int temp = x;
    x = y;
    y = temp;
}

Problem 156  Write a function called `evenCols` that returns the number of columns of a 2-dimensional array that have an even sum. The array contains integers and has 5 columns.

For example, a program that uses the function `evenCols` follows. The output is 2 because only columns 1 and 4 have even sum.

```cpp
int main() {
    int x[2][5] = {{1, 2, 3, 5, 4}, {2, 2, 2, 2, 2}};
    cout << evenCols(x, 2, 5) << endl;  // prints 2
    return 0;
}
```

Answer:

```cpp
int evenCols(int array[][5], int rows, int cols) {
    int ans = 0;
    for (int c = 0; c < cols; c++) {
        int total = 0;
        for (int r = 0; r < rows; r++)
            total += array[r][c];
        if (total % 2 == 0) ans++;
    }
    return ans;
}
```

Problem 157  Write a function called `positiveCols` that returns the number of columns of a 2-dimensional array that have a positive sum. The array contains doubles and has 6 columns.

For example, a program that uses the function `positiveCols` follows. The output is 2 because only columns 1 and 3 have positive sum.

```cpp
int main() {
    double x[2][6] = {{1.0, 6.0, 3.0, 5.0, 4.0, 2.0},
                       {-4.0, -4.0, -4.0, -4.0, -4.0, -4.0}};
    cout << positiveCols(x, 2, 6) << endl;  // prints 2
    return 0;
}
```

Answer:
int positiveCols(double array[][6], int rows, int cols) {
  int ans = 0;
  for (int c = 0; c < cols; c++) {
    double total = 0;
    for (int r = 0; r < rows; r++)
      total += array[r][c];
    if (total > 0) ans++;
  }
  return ans;
}

Problem 158  Write a function called largestCol that returns the largest sum of the entries in a single column of a 2-dimensional array. The array contains integers and has 5 columns.

For example, a program that uses the function largestCol follows. The output is 7 because this is the sum for columns 0 and 4 and the other columns have a smaller sum.

```cpp
int main() {
  int x[2][5] = {{1, 2, 3, 5, 4}, {6, 0, 0, 0, 3}};
  cout << largestCol(x, 2, 5) << endl; // prints 7
  return 0;
}
```

Answer:

```cpp
int largestCol(int array[][5], int rows, int cols) {
  int ans;
  for (int c = 0; c < cols; c++) {
    int total = 0;
    for (int r = 0; r < rows; r++)
      total += array[r][c];
    if (c == 0 || total > ans) ans = total;
  }
  return ans;
}
```

Problem 159  Write a function called smallestCol that returns the smallest sum of the entries in a single column of a 2-dimensional array. The array contains doubles and has 6 columns.

For example, a program that uses the function smallestCol follows. The output is 7.0 because this is the sum for columns 0 and 4 and the other columns have a larger sum.

```cpp
int main() {
  double x[2][6] = {{1.0, 9.0, 8.0, 6.0, 4.0, 8.0},
                     {6.0, 0.0, 0.0, 3.0, 3.0, 3.0}};
  cout << smallestCol(x, 2, 6) << endl; // prints 7.0
  return 0;
}
```

Answer:

```cpp
double smallestCol(double array[][6], int rows, int cols) {
  double ans;
  for (int c = 0; c < cols; c++) {
    double total = 0;
    for (int r = 0; r < rows; r++)
      total += array[r][c];
    if (c == 0 || total < ans) ans = total;
  }
  return ans;
}
```
Problem 160  Write a function called \texttt{not7s} that counts how many digits are not equal to 7 in a positive integer parameter.

For example, a program that uses the function \texttt{not7s} follows.

```c++
int main() {
    cout << not7s(747) << endl;  // prints 1
    cout << not7s(176) << endl;  // prints 2
    cout << not7s(12345) << endl; // prints 5
    cout << not7s(77777) << endl; // prints 0
    return 0;
}
```

Answer:

```c++
int not7s(int x) {
    if (x == 0) return 0;
    if (x % 10 == 7) return not7s(x/10);
    return not7s(x/10) + 1;
}
```

Problem 161  Write a function called \texttt{sixesAndSevens} that counts how many digits are equal to 6 or 7 in a positive integer parameter.

For example, a program that uses the function \texttt{sixesAndSevens} follows.

```c++
int main() {
    cout << sixesAndSevens(747) << endl; // prints 2
    cout << sixesAndSevens(176) << endl; // prints 2
    cout << sixesAndSevens(666) << endl; // prints 3
    cout << sixesAndSevens(12345) << endl; // prints 0
    return 0;
}
```

Answer:

```c++
int sixesAndSevens(int x) {
    if (x == 0) return 0;
    if (x % 10 == 7 || x% 10 == 6) return sixesAndSevens(x/10) + 1;
    return sixesAndSevens(x/10);
}
```

Problem 162  Write a function called \texttt{diff2} that returns the absolute value of the difference of the first two digits in an integer parameter that is at least 10.

For example, a program that uses the function \texttt{diff2} follows.

```c++
int main() {
    cout << diff2(747) << endl;  // prints 3
    cout << diff2(176) << endl;  // prints 6
    cout << diff2(10101) << endl; // prints 1
    cout << diff2(77777) << endl; // prints 0
    return 0;
}
```

Answer:

```c++
int diff2(int x) {
    if (x < 100) {
        return 0;
    }
    int a = x % 100 / 10;
    int b = x % 10;
    return abs(a - b);
}
```
int ans = x/10 - x % 10;
if (ans >= 0) return ans;
return -ans;
}
return diff2(x/10);
}

Problem 163 Write a function called \texttt{sum3} that returns the sum of the first three digits in an integer parameter that is at least 100.

For example, a program that uses the function \texttt{sum3} follows.

```c
int main() {
    cout << sum3(747) << endl; // prints 18
    cout << sum3(176) << endl; // prints 14
    cout << sum3(10199) << endl; // prints 2
    cout << sum3(77777) << endl; // prints 21
    return 0;
}
```

Answer:

```c
int sum3(int x) {
    if (x == 0) return 0;
    if (x < 1000) return sum3(x/10) + x%10;
    return sum3(x/10);
}
```

Problem 164 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer $n$ that is between 1 and 23.
2. It repeatedly reads $n$ from the user until the supplied value of $n$ is legal.
3. It prints out a rectangular picture with $2n - 1$ rows and $n$ columns that makes a large 5 as displayed by a digital clock.

Here is an example of how the program should work:

Give me an integer between 1 and 23: 4
****
***
****
***
****

Answer:

```c
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 23: ";
    cin >> n;
    while (n < 1 || n > 23) {
        cout << "Give me an integer between 1 and 23: ";
        cin >> n;
    }

    for (int r = 1; r < 2*n; r++) {
```
Problem 165  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter an integer \( n \) that is between 1 and 17.
2. It repeatedly reads \( n \) from the user until the supplied value of \( n \) is legal.
3. It prints out a rectangular picture with \( 2n - 1 \) rows and \( n \) columns that makes a large 2 as displayed by a digital clock.
Here is an example of how the program should work:

Give me an integer between 1 and 17: 5
********************

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 17: ";
    cin >> n;
    while (n < 1 || n > 17) {
        cout << "Give me an integer between 1 and 17: ";
        cin >> n;
    }
    for (int r = 1; r < 2*n; r++) {
        for (int c = 1; c <= n; c++)
            if (r == 1 || r == 2*n - 1 || r == n) cout << "*";
            else if (r < n && c == 1) cout << "*";
            else if (r > n && c == n) cout << "*";
            else cout << " ";
        cout << endl;
    }
    return 0;
}
```

Problem 166  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter an integer \( n \) that is between 1 and 23.
2. It repeatedly reads \( n \) from the user until the supplied value of \( n \) is legal.
3. It prints out a rectangular picture with \(2n - 1\) rows and \(n\) columns that makes a large 3 as displayed by a digital clock.

Here is an example of how the program should work:

Give me an integer between 1 and 23: 5

\[
\begin{array}{cccccccc}
* & * & * & * & * & * & * & * \\
* & * & * & * & * & * & * & * \\
* & * & * & * & * & * & * & * \\
\end{array}
\]

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 23: ";
    cin >> n;
    while (n < 1 || n > 23) {
        cout << "Give me an integer between 1 and 23: ";
        cin >> n;
    }

    for (int r = 1; r < 2*n; r++) {
        for (int c = 1; c <= n; c++)
            if (r == 1 || r == 2*n - 1 || r == n) cout << '*';
            else if (c == n) cout << '*';
            else cout << ' ';
        cout << endl;
    }

    return 0;
}
```

Problem 167  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer \(n\) that is between 1 and 17.
2. It repeatedly reads \(n\) from the user until the supplied value of \(n\) is legal.
3. It prints out a rectangular picture with \(2n - 1\) rows and \(n\) columns that makes a large 4 as displayed by a digital clock.

Here is an example of how the program should work:

Give me an integer between 1 and 17: 5

\[
\begin{array}{cccc}
* & * & * & * \\
* & * & * & * \\
* & * & * & * \\
\end{array}
\]

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int n;
    ```
cout << "Give me an integer between 1 and 17: ";
cin >> n;
while (n < 1 || n > 17) {
    cout << "Give me an integer between 1 and 17: ";
cin >> n;
}

for (int r = 1; r < 2*n; r++) {
    for (int c = 1; c <= n; c++)
        if (r == n) cout << "*";
        else if (r < n && c == 1) cout << "*";
        else if (c == n) cout << "*";
        else cout << " ";
    cout << endl;
}
return 0;
}

Problem 168 Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
    int x = 0, y = 1, z = 2;
    double b[2] = {1.1, 2.2};
    int d[2][2] = {{2,2},{3,4}};

    x = multiply(z, y); // (a) sets x to product 2
    copy(x, y); // (b) replaces x by value of y
    bigCol(d, 2, 2); // (c) prints biggest column: 2 4
    cout << printAll(b, 2) << endl; // (d) prints array: 1.1 2.2
    cout << add(b[1], b[1]) << endl; // (e) prints the sum 4.4
    return 0;
}

(a) Title line for multiply.
Answer:
int multiply(int z, int y)

(b) Title line for copy.
Answer:
void copy(int &x, int y)

(c) Title line for bigCol.
Answer:
void bigCol(int d[][2], int r, int c)

(d) Title line for printAll.
Answer:
string printAll(double b[], int cap)

(e) Title line for add.
Answer:
Problem 169  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```c++
int main() {
    int x = 0, y = 1, z = 2;
    double b[2] = {1.1, 2.2};
    int d[2][2] = {{0,1},{3,4}};

    d[0][0] = sum(x, y);  // (a) sets d[0][0] to the sum 1
    swap(x, y);          // (b) swaps x and y
    cout << biggest(d, 2, 2);  // (c) prints biggest entry 4
    printAll(b, 2);     // (d) prints 1.1 2.2
    cout << summit(b[0], b[0]) << endl;  // (e) prints the sum 2.2
    return 0;
}
```

(a) Title line for *sum*.
**Answer:**

```c++
int sum(int x, int y)
```

(b) Title line for *swap*.
**Answer:**

```c++
void swap(int &x, int &y)
```

(c) Title line for *biggest*.
**Answer:**

```c++
int biggest(int d[][2], int r, int c)
```

(d) Title line for *printAll*.
**Answer:**

```c++
void printAll(double b[], int cap)
```

(e) Title line for *summit*.
**Answer:**

```c++
double summit(double x, double y)
```

Problem 170  Consider the following C++ program.

```c++
#include <iostream>
using namespace std;

double down(int x[], int cap, int gap) {
    double ans = 0.0;
    for (int i = 0; i < cap; i+= gap)
        ans += x[i];
    return ans / 10;
}

int main() {
    int x[4] = {2, 1, 3, 0};
```
cout << x[2] << endl; // line (a)
cout << x[5/3] << endl; // line (b)
cout << x[x[3]] << endl; // line (c)
cout << down(x, 4, 1) << endl; // line (d)
cout << down(x, 4, 3) << endl; // line (e)
}

(a) What is the output at line (a)?

Answer:

3

(b) What is the output at line (b)?

Answer:

1

(c) What is the output at line (c)?

Answer:

2

(d) What is the output at line (d)?

Answer:

0.6

(e) What is the output at line (e)?

Answer:

0.2

Problem 171 Consider the following C++ program.

#include <iostream>
using namespace std;

double down(int x[], int cap, int gap) {
    double ans = 0.0;
    for (int i = 0; i < cap; i+= gap)
        ans += x[i];
    return ans / 10;
}

int main() {
    int x[4] = {3, 2, 0, 1};
    cout << x[2] << endl; // line (a)
cout << x[5/3] << endl; // line (b)
cout << x[x[3]] << endl; // line (c)
cout << down(x, 4, 1) << endl; // line (d)
cout << down(x, 4, 3) << endl; // line (e)
}

(a) What is the output at line (a)?

Answer:
(b) What is the output at line (b)?
Answer:
2

(c) What is the output at line (c)?
Answer:
2

(d) What is the output at line (d)?
Answer:
0.6

(e) What is the output at line (e)?
Answer:
0.4

Problem 172 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    int i = 2;
    int x[5] = {3, 1, 4, 1, 5};
    // (a) Is i even? Here YES is printed.
    if (isEven(i)) cout << "YES" << endl;
    // (b) Return the bigger. Here 4 is printed.
    cout << bigger(i, 4) << endl;
    // (c) Are all entries in the array x positive? Here YES is printed.
    if (allPositive(x, 5)) cout << "YES" << endl;
    // (d) Print the array with spaces between entries. Here 3 1 4 1 5.
    printArray(x, 5);
    // (e) Print the number of digits. Here 3.
    cout << numDigits(729) << endl;
    return 0;
}
```

Answer:

(a)

```cpp
bool isEven(int x) {
    return x % 2 == 0;
}
```

(b)

```cpp
int bigger(int x, int y) {
    if (x > y) return x;
    return y;
}
```
bool allPositive(int x[], int cap) {
    for (int i = 0; i < cap; i++)
        if (x[i] <= 0) return false;
    return true;
}

void printArray(int x[], int cap) {
    for (int i = 0; i < cap; i++) cout << x[i] << " ";
    cout << endl;
}

int numDigits(int x) {
    if (x < 10) return 1;
    return 1 + numDigits(x / 10);
}

Problem 173  Write blocks of code to perform the functions used in the following main program. Your blocks
must match the given title lines. Each block should be a short function of only a few lines.

int main() {
    double i = 2.5;
    string x = "Hello";
    // (a) Is i positive? Here YES is printed.
    if (isPositive(i)) cout << "YES" << endl;
    // (b) Return the bigger. Here 4 is printed.
    cout << bigger(i, 4) << endl;
    // (c) Does the string x start with an upper case character? Here YES.
    if (startsUpper(x)) cout << "YES" << endl;
    // (d) Add on a second copy of the string. Here HelloHello is printed.
    cout << twice(x) << endl;
    // (e) Print the first digit. Here 7.
    cout << firstDigit(729) << endl;
    return 0;
}

Answer:
(a)

bool isPositive(double x) {
    return x > 0;
}

(b)

double bigger(double x, double y) {
    if (x > y) return x;
    return y;
}
bool startsUpper(string x) {
    return x[0] >= 'A' && x[0] <= 'Z';
}

d string twice(string x) {
    return x + x;
}

e int firstDigit(int x) {
    if (x < 10) return x;
    return firstDigit(x / 10);
}

Problem 174 Write a function called shorten that shortens each element of an array of strings. Every string with more than two characters is cut down to its first two characters.

For example, a program that uses the function shorten follows.

```cpp
int main() {
    shorten(x, 6);
    for (int i = 0; i < 6; i++) cout << x[i] << " ";
    // Output: CS 1 11 Qu Co CU
    cout << endl;
    return 0;
}
```

Answer:

```cpp
void shorten(string x[], int cap) {
    for (int i = 0; i < cap; i++)
        if (x[i].length() > 2)
            x[i] = x[i].substr(0, 2);
}
```

Problem 175 Write a function called lengthen that lengthens each element of an array of strings. Every string with at least two characters has a XXX added after its first character.

For example, a program that uses the function lengthen follows.

```cpp
int main() {
    string x[3] = {"csci", "1", "11"};
    lengthen(x, 3);
    for (int i = 0; i < 3; i++) cout << x[i] << " ";
    // Output: cXXXsci 1XXX1
    cout << endl;
    return 0;
}
```

Answer:
void lengthen(string x[], int cap) {
    for (int i = 0; i < cap; i++)
        if (x[i].length() > 1)
            x[i] = x[i].insert(1, "XXX");
}

Problem 176   Write a function called *allOdd* that reports whether all the digits in a positive integer parameter are odd.
For example, a program that uses the function *allOdd* follows.

```cpp
int main() {
    if (allOdd(153)) cout << "All odd" << endl; // prints: All odd
    if (!allOdd(153972)) cout << "Not" << endl; // prints: Not
    if (!allOdd(222)) cout << "Not " << endl; // prints: Not
    if (allOdd(5)) cout << "All odd" << endl; // prints: All odd
    return 0;
}
```

**Answer:**

```cpp
bool allOdd(int x) {
    if (x < 10) return x % 2 == 1;
    return allOdd(x / 10) && allOdd(x % 10);
}
```

Problem 177   Write a function called *evenToNine* that returns a result obtained by turning all the even digits in a positive integer parameter to nines.
For example, a program that uses the function *evenToNine* follows.

```cpp
int main() {
    cout << evenToNine(1234) << endl; // prints: 1939
    cout << evenToNine(1357) << endl; // prints: 1357
    cout << evenToNine(22) << endl; // prints: 99
    cout << evenToNine(1) << endl; // prints: 1
    return 0;
}
```

**Answer:**

```cpp
int evenToNine(int x) {
    if (x <= 0) return 0;
    if (x % 2 == 0)
        return 10 * evenToNine(x / 10) + 9;
    return 10 * evenToNine(x / 10) + x % 10;
}
```

Problem 178   Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter 25 quiz scores each of which is an integer between 0 and 10.
2. It reads the 25 quiz scores.
3. It prints out the most common score (or scores).
For example if the scores 6 and 8 were the two most common scores, the output would be:
   6
   8
**Answer:**
```cpp
#include <iostream>
using namespace std;

int main() {
    int score, counts[11], maxCount = 0;
    for (int i = 0; i < 11; i++) counts[i] = 0;

    cout << "Enter 25 quiz scores: ";
    for (int i = 0; i < 25; i++) {
        cin >> score;
        counts[score] ++;
        if (counts[score] > maxCount)
            maxCount = counts[score];
    }

    for (int i = 0; i < 11; i++)
        if (counts[i] == maxCount)
            cout << i << " ";
    cout << endl;
    return 0;
}
```

**Problem 179**  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter quiz scores of 25 students. Each score is an integer between 0 and 10.
2. It reads the 25 quiz scores.
3. It prints out the score obtained by the middle student. (The middle student is ranked 13th in the class.)

**Answer:**

```cpp
#include <iostream>
using namespace std;

int main() {
    int score, counts[11];
    for (int i = 0; i < 11; i++) counts[i] = 0;

    cout << "Enter 25 quiz scores: ";
    for (int i = 0; i < 25; i++) {
        cin >> score;
        counts[score] ++;
    }

    score = 10;
    int numberStudents = counts[score];
    while (numberStudents < 13) {
        score--;
        numberStudents += counts[score];
    }

    cout << score << endl;
    return 0;
}
```

**Problem 180**  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.
```cpp
int main() {
    int x = 0, y = 1, z = 2;
    double b[2] = {1.1, 2.2};
    int d[2][2] = {{1,2},{3,4}};

    cout << diff(x, y) << endl; // (a) prints difference: -1
    y = addUp(x, y); // (b) sets y to sum 0 + 1
    cout << lastElt(b, 2); // (c) prints last element: 2.2
    b[0] = average(d, 2, 2); // (d) sets as average 2.5
    setZero(y, z); // (e) sets both to 0
    return 0;
}

(a) Title line for `diff`.
Answer:

```cpp
int diff(int a, int b)
```

(b) Title line for `addUp`.
Answer:

```cpp
int addUp(int x, int y)
```

(c) Title line for `lastElt`.
Answer:

```cpp
double lastElt(double array[], int cap)
```

(d) Title line for `average`.
Answer:

```cpp
double average(int array[][2], int r, int c)
```

(e) Title line for `setZero`.
Answer:

```cpp
void setZero(int &x, int &y)
```

**Problem 181** Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

double down(int x[], int cap, int gap) {
    double ans = 0.0;
    for (int i = 0; i < cap; i+= gap)
        ans += x[i];
    return ans / 10;
}

int main() {
    int x[4] = {1, 1, 3, 2};
    cout << x[2] << endl; // line (a)
    cout << x[5/3] << endl; // line (b)
    cout << x[x[3]] << endl; // line (c)
    cout << down(x, 4, 1) << endl; // line (d)
    cout << down(x, 4, 3) << endl; // line (e)
}
```
(a) What is the output at line (a)?
Answer:
3

(b) What is the output at line (b)?
Answer:
1

(c) What is the output at line (c)?
Answer:
3

(d) What is the output at line (d)?
Answer:
0.7

(e) What is the output at line (e)?
Answer:
0.3

Problem 182    Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    int i = 2;
    string x = "Hello";
    // (a) Does the number end in a 0? Here YES is printed.
    if (endInZero(100)) cout << "YES" << endl;
    // (b) Return the smaller. Here 2 is printed.
    cout << smaller(i, 4) << endl;
    // (c) Return the first character of the string. Here H is printed.
    cout << firstCharacter(x) << endl;
    // (d) Print first two characters in reverse order. Here eH is printed.
    swapFirstTwo(x); cout << endl;
    // (e) Print the sum of the digits. Here 18.
    cout << sumDigits(729) << endl;
    return 0;
}
```

Answer:

(a)

```cpp
bool endInZero(int x) {
    return x % 10 == 0;
}
```

(b)

```cpp
int smaller(int x, int y) {
    if (x < y) return x;
    return y;
}
```
char firstCharacter(string x) {
    return x[0];
}

void swapFirstTwo(string x) {
    cout << x[1] << x[0];
}

int sumDigits(int x) {
    if (x < 10) return x;
    return sumDigits(x / 10) + x % 10;
}

Problem 183  Write a function called setRandom that assigns a random value between 21 and 40 to each element of a 2-dimensional array of integers (with 3 columns). (You must use a standard C++ function to generate random numbers.)

For example, a program that uses the function setRandom follows.

```cpp
int main() {
    int x[2][3];
    setRandom(x, 2, 3);
    for (int c = 0; c < 3; c++) cout << x[1][c] << " ";
    // The output would be something like: 30 21 29
    cout << endl;
    return 0;
}
```

Answer:

```cpp
#include <cstdlib>

void setRandom(int x[][3], int r, int c) {
    for (int i = 0; i < r; i++)
        for (int j = 0; j < c; j++)
            x[i][j] = rand() % 20 + 21;
}
```

Problem 184  Write a function called startsWith that returns a result of even or odd that describes the first digit of a positive integer parameter.

For example, a program that uses the function startsWith follows.

```cpp
int main() {
    cout << startsWith(1234) << endl;   // prints: odd
    cout << startsWith(2345) << endl;   // prints: even
    cout << startsWith(22) << endl;     // prints: even
    cout << startsWith(1) << endl;      // prints: odd
    return 0;
}
```
string startsWith(int x) {
    if (x > 10) return startsWith(x / 10);
    if (x % 2 == 0) return "even";
    return "odd";
}

Problem 185  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter quiz scores of 24 students. Each score is an integer between 0 and 10.
2. It reads the 24 quiz scores.
3. It prints out the lowest score obtained by a student in the first quartile. (This is the score of the student ranked 6\textsuperscript{th} in the class.)
Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int score, counts[11];
    for (int i = 0; i < 11; i++) counts[i] = 0;

    cout << "Enter 24 quiz scores: ";
    for (int i = 0; i < 24; i++) {
        cin >> score;
        counts[score] ++;
    }

    score = 10;
    int numberStudents = counts[score];
    while (numberStudents < 6) {
        score--;
        numberStudents += counts[score];
    }

    cout << score << endl;
    return 0;
}
```

Problem 186  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```cpp
int main() {
    int x = 0, y = 1, z = 2;
    double b[3] = {1.9, 2.3, 3.0};
    int d[2][2] = {{1,2},{3,4}};

    x = sum(z, y);                       // (a) sets x to the sum: 3
    reset(d[1][1], z);                   // (b) replaces d[1][1] by the value of z
    diagonal(d, 2, 2);                   // (c) prints diagonal: 1 4
    cout << printAll(d, 2, 2) << endl;   // (d) prints array: 1 2 3 4
    cout << add(b[2], d[0][0]) << endl;  // (e) prints the sum: 4
    return 0;
}
```
Problem 187  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```cpp
int main() {
    double d = 2;
    string x[5] = {"3", "1", "4", "1", "5"};
    d = average(x, 5); // (a) sets d to 2.8
    d = max(d, x[4], 3); cout << d << endl; // (b) prints 5.0
    cout << inWords(x[1]) << endl; // (c) prints one
    cout << f(f(x[0],d), 1.0) << endl; // (d) mystery function prints 1.0
    percentage(8.0, x[2]); // (e) prints 200%
    return 0;
}
```

(a) Title line for **average**.
Answer:

```cpp
double average(string y[], int cap)
```

(b) Title line for **max**.
Answer:

```cpp
double max(double x, string y, int z)
```

(c) Title line for **inWords**.
Answer:

```cpp
string inWords(string x)
```

(d) Title line for **f**.
Answer:

```cpp
string f(string x, double y)
```
Problem 188  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

int recursive (int x) {
    if (x < 5) return 3;
    return recursive (x / 3) + x % 6;
}

char swap (int x, int y) {
    x = y;
    y = x;
    cout << x << y;
    return 's';
}

void set (int arr []) {
}

int main() {
    int x[5];
    set(x);
    swap(1, 2); cout << endl;     //line (a)
    set(x);
    cout << x[0 + 2] << x[0] + 2 << endl;     //line (b)
    cout << swap(1, 2) << endl;     //line (c)
    for (int i = 1; i < 4; i++) cout << x[i]; cout << endl;     //line (d)
    int e = 21;
    cout << recursive(e) << endl;     //line (e)
    return 0;
}
```

(a) What is the output at line (a)?
Answer:
22

(b) What is the output at line (b)?
Answer:
63

(c) What is the output at line (c)?
Answer:
22s

(d) What is the output at line (d)?
Answer:
968
What is the output at line (e)?
Answer:
7

Problem 189  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

int recursive (int x) {
    if (x < 5) return 4;
    return recursive (x / 4) + x % 6;
}

char swap (int x, int y) {
    y = x;
    x = y;
    cout << x << y;
    return '0';
}

void set (int arr []) {
}

int main() {
    int x[5];
    set(x);
    swap(1, 2); cout << endl; //line (a)
    set(x);
    cout << x[0 + 2] << x[0] + 2 << endl; //line (b)
    cout << swap(1, 2) << endl; //line (c)
    for (int i = 1; i < 4; i++) cout << x[i]; cout << endl; //line (d)
    int e = 21;
    cout << recursive(e) << endl; //line (e)
    return 0;
}
```

(a) What is the output at line (a)?
Answer:
11

(b) What is the output at line (b)?
Answer:
07

(c) What is the output at line (c)?
Answer:
110

(d) What is the output at line (d)?
Answer:
904
(c) What is the output at line (e)?

Answer:

12

Problem 190  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```c
int main() {
    int i = 2;
    int x[5] = {3, 1, 4, 1, 5};
    // (a) Return the sum. Here 4 is printed.
    cout << add(i, 2) << endl;
    // (b) Return number of odd entries. Here 4 is printed.
    cout << numOdd(x, 5) << endl;
    // (c) Multiply i by 2. Here 4 is printed.
    doubleIt(i); cout << i << endl;
    // (d) Find the index of the largest entry. Here 4 is printed.
    cout << findIndexMax(x, 5) << endl;
    // (e) Is it a lower case character? Here 4 is printed.
    if (isLowerCase('h')) cout << "4" << endl;
    return 0;
}
```

Answer:

(a)

```c
int add(int x, int y) {
    return x + y;
}
```

(b)

```c
int numOdd(int array[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (array[i] % 2 != 0) ans++;
    return ans;
}
```

(c)

```c
void doubleIt(int &x) {
    x *= 2;
}
```

(d)

```c
int findIndexMax(int array[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (array[i] > array[ans]) ans = i;
    return ans;
}
```
Problem 191

Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
bool isLowerCase(char x) {
    return 'a' <= x && x <= 'z';
}
```

```cpp
int main() {
    int i = 2;
    int x[5] = {3, 1, 4, 1, 5};
    // (a) Return the absoluteValue. Here 2 is printed.
    cout << absoluteValue(i) << endl;
    // (b) Return number of even entries, here 1 is printed.
    cout << numEven(x, 5) << endl;
    // (c) Cube i. Here 8 is printed.
    cubeIt(i); cout << i << endl;
    // (d) Find the (first) index of the smallest entry. Here 1 is printed.
    cout << findIndexMin(x, 5) << endl;
    // (e) Is it a digit? Here print nothing.
    if (isDigit('h')) cout << "Digit" << endl;
    return 0;
}
```

Answer:

(a)
```cpp
int absoluteValue(int x) {
    if (x < 0) return -x;
    return x;
}
```

(b)
```cpp
int numEven(int array[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (array[i] % 2 == 0) ans++;
    return ans;
}
```

(c)
```cpp
void cubeIt(int &x) {
    x = x * x * x;
}
```

(d)
```cpp
int findIndexMin(int array[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (array[i] < array[ans]) ans = i;
    return ans;
}
```
bool isDigit(char x) {
    return '0' <= x && x <= '9';
}

Problem 192  Write a function called noEl that returns the number of elements that do not contain the letter l in a 2-dimensional array of strings (that has 3 columns).

For example, a program that uses the function noEl follows.

```c
int main() {
    string x[2][3] = {"CSCI", "One", "eleven"}, {"Queens", "College", "CUNY"};
    cout << noEl(x, 2, 3) << endl;  // prints: 4
    return 0;
}
```

Answer:

```c
int noEl(string data[][3], int rows, int cols) {
    int count = 0;
    for (int r = 0; r < rows; r++)
        for (int c = 0; c < cols; c++)
            if ((int) data[r][c].find("l") < 0) count++;
    return count;
}
```

Problem 193  Write a function called cString that returns a comma separated list of all elements that start with the letter C in an array of strings.

For example, a program that uses the function cString follows.

```c
int main() {
    cout << cString(x, 6) << endl;  // prints: Computer,College,CUNY
    return 0;
}
```

Answer:

```c
string cString(string data[], int cap) {
    string ans = "";
    for (int c = 0; c < cap; c++)
        if (data[c].find("C") == 0) {
            if (ans != "") ans = ans + ",";
            ans = ans + data[c];
        }
    return ans;
}
```

Problem 194  Write a function called removeDuplicates that replaces any sequence of copies of a digit in a positive integer parameter by a single copy of that digit.

For example, a program that uses the function removeDuplicates follows.
int main() {
    cout << removeDuplicates(55511) << endl; // prints 51
    cout << removeDuplicates(51155) << endl; // prints 515
    cout << removeDuplicates(551155) << endl; // prints 515
    cout << removeDuplicates(515) << endl; // prints 515
    return 0;
}

Answer:

int removeDuplicates(int x) {
    if (x < 10) return x;
    int y = removeDuplicates(x / 10);
    if (y % 10 == x % 10) return y;
    return 10 * y + x % 10;
}

Problem 195 Write a function called makeDecreasing that makes a result with decreasing digits from a positive integer parameter. It selects the leftmost digit of the parameter and then later digits that are smaller than all that have already been selected.

For example, a program that uses the function makeDecreasing follows.

int main() {
    cout << makeDecreasing(89321) << endl; // prints 8321
    cout << makeDecreasing(892321) << endl; // prints 821
    cout << makeDecreasing(1995) << endl; // prints 1
    cout << makeDecreasing(7) << endl; // prints 7
    return 0;
}

Answer:

int makeDecreasing(int x) {
    if (x < 10) return x;
    int y = makeDecreasing(x / 10);
    if (y % 10 <= x % 10) return y;
    return 10 * y + x % 10;
}

Problem 196 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter 25 integers and it reads the numbers that the user gives.
2. It calculates the average of the entered numbers.
3. It reports all entered numbers that are greater than the average, by printing them to a file called output6.txt.

Answer:

#include <iostream>
#include <fstream>
using namespace std;

int main() {
    ofstream out;
    out.open("output6.txt");
    int x[25];
    cout << " Enter 25 integers: ";
    for (int i = 0; i < 25; i++) cin >> x[i];
int sum = 0;
for (int i = 0; i < 25; i++) sum += x[i];
double average = sum / 25.0;
for (int i = 0; i < 25; i++)
  if (x[i] > average) out << x[i] << endl;
out.close();
return 0;
}

Problem 197  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter 25 integers and it reads the numbers that the user gives.
2. It calculates the smallest of the entered numbers.
3. It reports all entered numbers that are greater than the square of the smallest one. This output is to be printed to a file called output6.txt (and not to the user’s screen).

Answer:

#include <iostream>
#include <fstream>
using namespace std;

int main() {
  ofstream out;
  out.open("output6.txt");
  int x[25];
  cout << " Enter 25 integers: ";
  for (int i = 0; i < 25; i++) cin >> x[i];
  int smallest = x[0];
  for (int i = 0; i < 25; i++)
    if (x[i] < smallest) smallest = x[i];
  for (int i = 0; i < 25; i++)
    if (x[i] > smallest * smallest) out << x[i] << endl;
  out.close();
  return 0;
}

Problem 198  Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
  int a[3] = {1, 1, 1}, i = 7, j = 8, k = 9;
  int b[5] = {1, 9, 6, 8, 3};
  int x[2][2] = {{2, 0}, {4, 8}};
  cout << max(i, j, k) << endl;  // (a) prints: 9
  printMax(b, 5);  // (b) prints: 9
  cout << max2d(x, 2, 2) << endl;  // (c) prints: 8
  swap(i, j);  // (d) swaps i and j
  swapArrays(a, b, 2);  // (e) swaps first 2 elements of arrays a and b
  return 0;
}

(a) Title line for max.

Answer:
int max(int x, int y, int z)
(a) Title line for max.
Answer:
void max(int x[], int y[], int z)

void printMax(int x[], int capacity)
(b) Title line for printMax.
Answer:
void printMax(int x[], int capacity)

int max2d(int x[][2], int r, int c)
(c) Title line for max2d.
Answer:
int max2d(int x[][2], int r, int c)

void swap(int &x, int &y)
(d) Title line for swap.
Answer:
void swap(double &x, double &y)

void swapArrays(int x[], int y[], int number)
(e) Title line for swapArrays.
Answer:
void swapArrays(double x[], double y[], int number)

Problem 199 Write the best title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
    double a[3] = {1.0, 1.0, 1.0}, i = 7.0, j = 8.0, k = 9.9;
    double b[5] = {1.9, 9.9, 6.9, 8.9, 3.9};
    double x[2][2] = {{2.9, 0.9}, {4.9, 8.9}};
    cout << max(i, j, k) << endl; // (a) prints: 9.9
    printMax(b, 5); // (b) prints: 9.9
    cout << max2d(x, 2, 2) << endl; // (c) prints: 8.9
    swap (i, j); // (d) swaps i and j
    swapArrays (a, b, 2); // (e) swaps first 2 elements of arrays a and b
    return 0;
}

(a) Title line for max.
Answer:
double max(double x, double y, double z)

(b) Title line for printMax.
Answer:
void printMax(double x[], int capacity)

(c) Title line for max2d.
Answer:
double max2d(double x[][2], int r, int c)

(d) Title line for swap.
Answer:
void swap(double &x, double &y)
void swapArrays(double x[], double y[], int number)

Problem 200  Consider the following C++ program.

#include <iostream>
using namespace std;

void yesNo(bool ans) {
    if (ans) cout << "Y";
    else cout << "N";
    cout << endl;
}

int main() {
    int x = 3, y = 4, z = 5, a[4] = {0, 1, 2, 3};
    if (x == y) cout << "Y
"; else cout << "N
";  // line (a)
    if (x == a[x]) cout << "Y
"; else cout << "N
";  // line (b)
    if (!(x != y)) cout << "Y
"; else cout << "N
";  // line (c)
    yesNo((y < z) && (z < x));                      // line (d)
    yesNo((x < y) || (z < y));                      // line (e)
}

(a) What is the output at line (a)?
Answer:

N

(b) What is the output at line (b)?
Answer:

Y

(c) What is the output at line (c)?
Answer:

N

(d) What is the output at line (d)?
Answer:

N

(e) What is the output at line (e)?
Answer:

Y

Problem 201  Consider the following C++ program.
```cpp
#include <iostream>
using namespace std;

void yesNo(bool ans) {
    if (ans) cout << "Y";
    else cout << "N";
    cout << endl;
}

int main() {
    int x = 3, y = 5, z = 4, a[4] = {3, 2, 1, 0};
    if (x == y) cout << "Y\n"; // line (a)
    if (x == a[0]) cout << "Y\n"; // line (b)
    if (!(y < x)) cout << "Y\n"; else cout << "N\n"; // line (c)
    yesNo((x < z) && (y < z)); // line (d)
    yesNo((x < z) || (y < z)); // line (e)
}

(a) What is the output at line (a)?
Answer:

(b) What is the output at line (b)?
Answer:
Y
(c) What is the output at line (c)?
Answer:
Y
(d) What is the output at line (d)?
Answer:
N
(e) What is the output at line (e)?
Answer:
Y

Problem 202 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```
Answer:

(a)

```c
int absoluteValue(int x) {
    if (x < 0) return -x;
    return x;
}
```

(b)

```c
int collatz(int x) {
    if (x % 2 == 0) return x / 2;
    return 3 * x + 1;
}
```

(c)

```c
int leastFactor(int x) {
    int ans = 2;
    while (x % ans != 0) ans++;
    return ans;
}
```

(d)

```c
bool allPositive(double x[], int capacity) {
    for (int i = 0; i < capacity; i++)
        if (x[i] <= 0) return false;
    return true;
}
```

(e)

```c
void swapArrays(double x[], double y[], int capacity) {
    for (int i = 0; i < capacity; i++) {
        double temp = x[i];
        x[i] = y[i];
        y[i] = temp;
    }
}
```

Problem 203 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```c
int main() {
    int x = 5;
    double e = 2.718;
    double a[4] = {1.0, 2.0, -3.0, -4.0};
    double b[2] = {5.5, 4.5};
    // (a) Changes the sign. Here to -5
    changeSign(x);
    // (b) Return first digit after decimal point. Here 7 is printed.
    cout << firstDecimal(e) << endl;
    // (c) Return the number of negative entries. Here 2 is printed.
}
```
// (d) Test whether the first argument is a factor of the second. Here: Yes
if (isFactor(7, 14)) cout << "Yes\n";
// (e) print average of all entries both arrays: Here 1.0 is printed.
averageArrays(a, 4, b, 2);
return 0;
}

Answer:
(a)

```cpp
void changeSign(int &x) {
    x = -x;
}
```

(b)

```cpp
int firstDecimal(double x) {
    int tenX = (int) (x * 10);
    return tenX % 10;
}
```

(c)

```cpp
int numberNeg(double x[], int capacity) {
    int ans = 0;
    for (int i = 0; i < capacity; i++)
        if (x[i] < 0) ans++;
    return ans;
}
```

(d)

```cpp
bool isFactor(int x, int y) {
    return y % x == 0;
}
```

(e)

```cpp
void averageArrays(double x[], int capacityX, double y[], int capacityY) {
    double sum = 0.0;
    for (int i = 0; i < capacityX; i++) sum += x[i];
    for (int i = 0; i < capacityY; i++) sum += y[i];
    cout << sum / (capacityX + capacityY) << endl;
}
```

Problem 204 Write a function called `longestString` that returns the longest element in a 2-dimensional array of strings (that is known to have 2 columns).
For example, a program that uses the function `longestString` follows.

```cpp
int main() {
    string x[3][2] = {"This", "is"}, {"an", "easy"}, {"question", ""}};
    cout << longestString(x, 3, 2) << endl; // prints: question
    return 0;
}
```
Answer:

string longestString(string x[][2], int rows, int cols) {
    string ans = "";
    for (int i = 0; i < rows; i++)
        for (int j = 0; j < cols; j++)
            if (x[i][j].length() > ans.length()) ans = x[i][j];
    return ans;
}

Problem 205 Write a function called print3 that prints the elements of an array of integers, separated by commas and with 3 elements on each output line.

For example, a program that uses the function print3 follows.

```cpp
int main() {
    int x[8] = {1,2,3,4,5,6,7,8};
    print3(x, 8);
    return 0;
}
```

The output should be exactly:

1,2,3
4,5,6
7,8

Answer:

```cpp
void print3(int x[], int capacity) {
    for (int i = 0; i < capacity; i++) {
        cout << x[i];
        if (i < (capacity - 1) && i % 3 != 2) cout << ",";
        else cout << endl;
    }
}
```

Problem 206 Write a function called become5 that has two inputs – the first input is a positive integer and the second input is a single-digit integer. (You may assume that the two inputs have these forms.) The function has an integer output. The output is identical to the first input, except that every digit that matches the second input is replaced with a 5.

For example, a program that uses the function become5 follows.

```cpp
int main() {
    cout << become5(232, 2) << endl; // prints 535
    cout << become5(232, 3) << endl; // prints 252
    cout << become5(232, 4) << endl; // prints 232
    return 0;
}
```

Answer:

```cpp
int become5(int n, int digit) {
    if (n == digit) return 5;
    if (n < 10) return n;
    return 10 * become5(n/10, digit) + become5(n % 10, digit);
}
```
Problem 207  Write a function called change5 that has two inputs – the first input is a positive integer and the second input is a single-digit integer. (You may assume that the two inputs have these forms.) The function has an integer output. The output is identical to the first input, except that every digit equal to 5 is replaced by the digit given by the second parameter.

For example, a program that uses the function change5 follows.

```cpp
int main() {
    cout << change5(535, 2) << endl; // prints 232
    cout << change5(252, 3) << endl; // prints 232
    cout << change5(232, 4) << endl; // prints 232
    return 0;
}

Answer:

int change5(int n, int digit) {
    if (n == 5) return digit;
    if (n < 10) return n;
    return 10 * change5(n/10, digit) + change5(n % 10, digit);
}
```

Problem 208  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It opens an input file called input14a.txt that contains only integers, including at least one negative integer. (You may assume that the file has exactly this content.)
2. It reads integers from the file until a negative integer is found.
3. It reports how many integers were read (upto and including the first negative value).

For example if the file input14a.txt has the following content:

```
12 16 29
17 10001
2 -34
-1 35 -3
11
```

The first negative entry in the file is its 7th number −34 and the program would output: 7

Answer:

```cpp
#include <fstream>
#include <iostream>
using namespace std;

int main() {
    ifstream f;
    f.open("input14a.txt");
    int x = 0, count = 0;

    while (x >= 0) {
        f >> x;
        count++;
    }
    cout << count << endl;
    f.close();
    return 0;
}
```
Problem 209  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It opens an input file called input14b.txt that contains only strings, including at least one that starts with the letter X. (You may assume that the file has exactly this content.)
2. It reads strings from the file until one beginning with X is found.
3. It reports how many strings were read (upto and including the first that begins with X).
For example if the file input14b.txt has the following content:

A BBB C

Dog

XYZ E XXX

The first X-word in the file is its 5th string XYZ and the program would output: 5

Answer:

#include <fstream>
#include <iostream>
using namespace std;

int main() {
    ifstream f;
    f.open("input14b.txt");
    int count = 0;
    string x = "A";

    while (x[0] != 'X') {
        f >> x;
        count++;
    }
    cout << count << endl;
    f.close();
    return 0;
}

Problem 210  Write title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

int main() {
    int i = 2;
    int x[5] = {3, 1, 4, 1, 5};
    cout << max(2.1, i, i) << endl; // (a) prints 2.1
    cout << min(x[2], x[3]) << endl; // (b) prints 1
    doubleIt(i); cout << i << endl; // (c) prints 4
    printIt(x, 3); // (d) prints 314
    cout << sum(sum(2,6), sum(x[0],x[1])) << endl; // (e) prints 12
    return 0;
}

(a) Title line for max.
Answer:

double max(double x, int y, int z)

(b) Title line for min.
Answer:
Problem 211 Write title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```cpp
int main() {
    int i = 3;
    int x[5] = {2, 7, 1, 8, 2};
    cout << min(i, 2.1, i) << endl; // (a) prints 2.1
    cout << max(x[2], 3) << endl; // (b) prints 3
    cout << doubleIt(i) << endl; // (c) prints the following: 2 x 3
    cout << sum(sum(2,6,i), i, i) << endl; // (d) prints 17
    sortIt(x, 3); // (e) sorts array x by selection sort
    return 0;
}
```

(a) Title line for **min**.
Answer:

double min(int x, double y, int z)

(b) Title line for **max**.
Answer:

int max(int x, int y)

(c) Title line for **doubleIt**.
Answer:

string doubleIt(int x)

(d) Title line for **sum**.
Answer:

int sum(int x, int y, int z)

(e) Title line for **sortIt**.
Answer:

void sortIt(int x[], int n)
Problem 212  Write title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```c
int main() {
    int i = 2;
    double x[5] = {3, 1, 4, 1, 5};
    cout << max(4.1, x[i], i) << endl; // (a) prints 4.1
    cout << min(x[2], x[3]) << endl; // (b) prints 1
    doubleIt(i); cout << i << endl; // (c) prints 4
    printIt(x, 3); // (d) prints 314
    cout << sum(sum(2.1, 6), sum(x[0], x[1])) << endl; // (e) prints 12.1
    return 0;
}
```

(a) Title line for **max**.
Answer:

double max(double x, double y, int z)

(b) Title line for **min**.
Answer:

double min(double x, double y)

(c) Title line for **doubleIt**.
Answer:

void doubleIt(int &x)

(d) Title line for **printIt**.
Answer:

void printIt(double x[], int n)

(e) Title line for **sum**.
Answer:

double sum(double x, double y)

Problem 213  Write title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```c
int main() {
    double i = 3;
    double x[5] = {2, 7, 1, 8, 2};
    cout << min(i, 2.1, i) << endl; // (a) prints 2.1
    cout << max(x[2], 3.1) << endl; // (b) prints 3.1
    cout << doubleIt(i) << endl; // (c) prints the following: 2 x 3
    cout << sum(sum(2.1, 6, i), i, i) << endl; // (d) prints 17.1
    sortIt(x, 3); // (e) sorts array x by selection sort
    return 0;
}
```

(a) Title line for **min**.
Answer:

double min(double x, double y, double z)
Problem 214  Write title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```c
int main() {
    int i = 2;
    int x[5] = {3, 1, 4, 1, 5};
    cout << add(i, i) << endl; // (a) prints 4
    cout << numOdd(x, 5) << endl; // (b) prints 4
    doubleIt(x[1]); cout << x[1] << endl; // (c) prints 2
    cout << diff(diff(3, 1), 1) << endl; // (d) prints 1
    cout << percentage(i, x[2]) << endl; // (e) prints 50%
    return 0;
}
```

(a) Title line for **add**.
   Answer:
   ```c
   int add(int y, int z)
   ```

(b) Title line for **numOdd**.
   Answer:
   ```c
   int numOdd(int x[], int y)
   ```

(c) Title line for **doubleIt**.
   Answer:
   ```c
   void doubleIt(int &x)
   ```

(d) Title line for **diff**.
   Answer:
   ```c
   int diff(int x, int y)
   ```

(e) Title line for **percentage**.
   Answer:
   ```c
   string percentage(int x, int y)
   ```
Problem 215  Write title lines for the functions that are called by the following main program. **Do not supply blocks for the functions.**

```c
int main() {
    int i = 2;
    int x[5] = {3, 1, 4, 1, 5};
    cout << average(x, 5) << endl; // (a) prints 2.8
    cout << max(i, i, 3) << endl; // (b) prints 3
    cout << doubleIt(x[1]) << endl; // (c) prints 2
    cout << total(total(3,1,1), 1, 1) << endl; // (d) prints 7
    percentage(i, x[2]); // (e) prints 50%
    return 0;
}
```

(a) Title line for `average`.  
**Answer:**

```c
double average(int y[], int cap)
```

(b) Title line for `max`.  
**Answer:**

```c
int max(int x, int y, int z)
```

(c) Title line for `doubleIt`.  
**Answer:**

```c
int doubleIt(int x)
```

(d) Title line for `total`.  
**Answer:**

```c
int total(int x, int y, int z)
```

(e) Title line for `percentage`.  
**Answer:**

```c
void percentage(int x, int y)
```

---

Problem 216  Write title lines for the functions that are called by the following main program. **Do not supply blocks for the functions.**

```c
int main() {
    double i = 2.5;
    int x[5] = {3, 1, 4, 1, 5};
    cout << add(i, i) << endl; // (a) prints 5.0
    if (oddSum(x, 5)) cout << "true" << endl; // (b) prints true
    doubleIt(i); cout << i << endl; // (c) prints 5.0
    cout << diff(diff(3.0,i), i) << endl; // (d) prints -2.0
    cout << percentage(x[1], x[2]) << endl; // (e) prints 25%
    return 0;
}
```

(a) Title line for `add`.  
**Answer:**

```c
double add(double y, double z)
```
(b) Title line for **oddSum**.
   Answer:
   ```
   bool oddSum(int x[], int y)
   ```

(c) Title line for **doubleIt**.
   Answer:
   ```
   void doubleIt(double &x)
   ```

(d) Title line for **diff**.
   Answer:
   ```
   double diff(double x, double y)
   ```

(e) Title line for **percentage**.
   Answer:
   ```
   string percentage(int x, int y)
   ```

**Problem 217** Write title lines for the functions that are called by the following main program. Do not supply blocks for the functions.

```c
int main() {
    double i = 2; int n = 2;
    double x[5] = {3, 1, 4, 1, 5};
    cout << average(x, 5) << endl; // (a) prints 2.8
    cout << max(i, i, 3.0) << endl; // (b) prints 3.0
    cout << doubleIt(x[1]) << endl; // (c) prints 2.0
    cout << ratio(ratio(3,1), n) << endl; // (d) prints 1.5
    percentage(i, x[2]); // (e) prints 50.0%
    return 0;
}
```

(a) Title line for **average**.
   Answer:
   ```
   double average(double y[], int cap)
   ```

(b) Title line for **max**.
   Answer:
   ```
   double max(double x, double y, double z)
   ```

(c) Title line for **doubleIt**.
   Answer:
   ```
   double doubleIt(double x)
   ```

(d) Title line for **ratio**.
   Answer:
   ```
   double ratio(double x, int y)
   ```

(e) Title line for **percentage**.
   Answer:
   ```
   void percentage(double x, double y)
   ```
Problem 218  Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out abc 123.

```
#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    string words[4] = {"An ", "easy ", "question ", ""};
    for (int i = 0; i <= 2; i++) cout << words[i]; cout << endl;  // line (a)
    for (int i = 0; i <= 2; i++) cout << words[i][i]; cout << endl;  // line (b)
    words[3] = argv[1];
    cout << words[3] << endl;  // line (c)
    cout << ++words[0][0] << endl;  // line (d)
    cout << argc << endl;  // line (e)
    return 0;
}
```

(a) What is the output at line (a)?
Answer:
An easy question

(b) What is the output at line (b)?
Answer:
Aae

(c) What is the output at line (c)?
Answer:
abc

(d) What is the output at line (d)?
Answer:
B

(e) What is the output at line (e)?
Answer:
3

Problem 219  Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out 123.

```
#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    string words[4] = {"An ", "easy ", "question ", ""};
    for (int i = 2; i >= 0; i--) cout << words[i]; cout << endl;   // line (a)
    for (int i = 2; i >= 0; i--) cout << words[i][i+1]; cout << endl; // line (b)
    words[3] = argv[1];
    cout << words[3] << endl;  // line (c)
    cout << ++words[0][0] << endl;  // line (d)
    cout << argc << endl;  // line (e)
    return 0;
}
```
(a) What is the output at line (a)?

Answer:

Not very difficult

(b) What is the output at line (b)?

Answer:

Nef

(c) What is the output at line (c)?

Answer:

xyz

Problem 220 Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out xyz 987.

```cpp
#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    string words[4] = {"Not ", "very ", "difficult ", ""};
    for (int i = 0; i <= 2; i++) cout << words[i]; cout << endl; // line (a)
    for (int i = 0; i <= 2; i++) cout << words[i][i]; cout << endl; // line (b)
    words[3] = argv[1];
    cout << words[3] << endl; // line (c)
    cout << ++words[0][0] << endl; // line (d)
    cout << argc << endl; // line (e)
    return 0;
}
```

(a) What is the output at line (a)?

Answer:

Not very difficult

(b) What is the output at line (b)?

Answer:

Nef

(c) What is the output at line (c)?

Answer:

xyz
Problem 221  Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out 007.

#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    string words[4] = {"Not ", "very ", "difficult ", ""};
    for (int i = 2; i >= 0; i--) cout << words[i]; cout << endl;  // line (a)
    for (int i = 2; i >= 0; i--) cout << words[i][i+1]; cout << endl;  // line (b)
    words[3] = argv[1];
    cout << words[3] << endl;  // line (c)
    cout << words[0][0]++ << endl;  // line (d)
    cout << argc << endl;  // line (e)
    return 0;
}

(a) What is the output at line (a)?
Answer:

difficult very Not

(b) What is the output at line (b)?
Answer:

fro

(c) What is the output at line (c)?
Answer:

007

(d) What is the output at line (d)?
Answer:

N

(e) What is the output at line (e)?
Answer:

2

Problem 222  Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out a 1.
#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    for (int i = 1; i <= 3; i++) cout << words[i]; cout << endl; // line (a)
    for (int i = 0; i <= 2; i++) cout << words[i][i]; cout << endl; // line (b)
    words[3] = argv[2];
    cout << words[3] << endl; // line (c)
    cout << ++words[0][0] << endl; // line (d)
    cout << argc << endl; // line (e)
    return 0;
}

(a) What is the output at line (a)?
Answer:
Queens College

(b) What is the output at line (b)?
Answer:
 Cul

(c) What is the output at line (c)?
Answer:
1

(d) What is the output at line (d)?
Answer:
D

(e) What is the output at line (e)?
Answer:
3

**Problem 223** Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out CS111.

#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    string words[4] = {"Queens ", "College ", "CUNY ", "NY"};
    for (int i = 3; i >= 0; i--) cout << words[i]; cout << endl; // line (a)
    for (int i = 2; i >= 0; i--) cout << words[i][i+1]; cout << endl; // line (b)
    words[3] = argv[1];
    cout << words[3] << endl; // line (c)
    cout << ++words[0][0] << endl; // line (d)
    cout << ++argc << endl; // line (e)
    return 0;
}
(a) What is the output at line (a)?

**Answer:**

NYCUNY College Queens

(b) What is the output at line (b)?

**Answer:**

Ylu

(c) What is the output at line (c)?

**Answer:**

CS111

(d) What is the output at line (d)?

**Answer:**

Q

(e) What is the output at line (e)?

**Answer:**

3

**Problem 224**  Consider the following C++ program. It is compiled to `a.out` and executed with the command `.a.out out out`.

```cpp
#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    string words[4] = {"CS ", "QC ", "CUNY ", "EDU ";
    for (int i = 0; i <= 2; i++) cout << words[i]; cout << endl;  // line (a)
    for (int i = 0; i <= 2; i++) cout << words[i][i]; cout << endl; // line (b)
    words[3] = argv[1];
    cout << words[3] << endl; // line (c)
    cout << ++words[0][0] << endl; // line (d)
    cout << argc++ << endl; // line (e)
    return 0;
}
```

(a) What is the output at line (a)?

**Answer:**

CS QC CUNY

(b) What is the output at line (b)?

**Answer:**

CCN

(c) What is the output at line (c)?

**Answer:**

out
Problem 225  Consider the following C++ program. It is compiled to a.out and executed with the command ./a.out 007.

```
#include <iostream>
using namespace std;

int main(int argc, char *argv[]) {
    for (int i = 3; i >= 0; i--) cout << words[i]; cout << endl;  // line (a)
    for (int i = 3; i >= 0; i--) cout << words[i][i+1]; cout << endl;  // line (b)
    words[3] = argv[1];
    cout << words[3] << endl;  // line (c)
    cout << words[0][0]++ << endl;  // line (d)
    cout << --argc << endl;  // line (e)
    return 0;
}
```

(a) What is the output at line (a)?
Answer:

New YorkFlushing College Queens

(b) What is the output at line (b)?
Answer:

Yslu

(c) What is the output at line (c)?
Answer:

007

(d) What is the output at line (d)?
Answer:

Q

(e) What is the output at line (e)?
Answer:

1

Problem 226  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.
int main() {
    int a = 2, b = 3, c = 4;
    ifstream f;
    string s = "HELLO"; char t[] = "HELLO";
    f.open("testFile.txt");
    // (a) Tests whether a number is even, here Even!
    if (isEven(c)) cout << "Even!" << endl;
    // (b) Removes first and last chars from a string, here ELL
    cout << removeEnds(s) << endl;
    // (c) Prints first word in the input file
    cout << firstWord(f) << endl;
    // (d) Print last character of a C-string, here O
    cout << lastChar(t) << endl;
    // (e) Rotate a,b,c so as to print 3,4,2
    rotate(a, b, c);
    cout << a << b << c << endl;
    return 0;
}

Answer:
(a)

bool isEven(int x) {
    return x % 2 == 0;
}

(b)

string removeEnds(string x) {
    return x.substr(1, x.length() - 2);
}

(c)

string firstWord(ifstream &file) {
    string x;
    file >> x;
    return x;
}

(d)

char lastChar(char x[]) {
    return x[strlen(x) - 1];
}

(e)

void rotate(int &x, int &y, int &z) {
    int temp = x;
    x = y;
    y = z;
    z = temp;
}
Problem 227  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    int a = 23, b = 3, c = 4;
    ifstream f;
    string s = "HELLO"; char t[] = "HELLO";
    f.open("testFile.txt");
    // (a) Tests whether a number has 2 digits, here Yes!
    if (is2digit(a)) cout << "Yes!" << endl;
    // (b) Doubles a string, here HELLOHELLO
    cout << doubleIt(s) << endl;
    // (c) The number of words read from the input file before eof() is true
    cout << countWords(f) << endl;
    // (d) Print middle character of a C-string that has a middle, here L
    cout << midChar(t) << endl;
    // (e) Rotate a,b,c so as to print 4,23,3
    rotate(a, b, c);
    cout << a << "," << b << "," << c << endl;
    return 0;
}

Answer:

(a)
bool is2digit(int x) {
    return (x > 9) && (x < 100);
}

(b)
string doubleIt(string x) {
    return x + x;
}

(c)
int countWords(ifstream &file) {
    string x;
    int count = 0;
    while (!file.eof()) {
        file >> x;
        count++;
    }
    return count;
}

(d)
char midChar(char x[]) {
    return x[(strlen(x) - 1)/2];
}

(e)
```
void rotate(int &x, int &y, int &z) {
    int temp = x;
    x = z;
    z = y;
    y = temp;
}

Problem 228   Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

int main() {
    int a = 2, b = 3, c = 4;
    ifstream f;
    string s = "HELLO"; char t[] = "HELLO";
    f.open("testFile.txt");
    // (a) Tests whether a number is seven, here No!
    if (!isSeven(c)) cout << "No!" << endl;
    // (b) Removes the last char from a string, here HELL
    cout << removeLast(s) << endl;
    // (c) Prints second word in the input file
    cout << secondWord(f) << endl;
    // (d) Print first character of a C-string, here H
    cout << firstChar(t) << endl;
    // (e) swap a with the biggest of a,b,c. Here prints 4,3,2
    swapBig(a, b, c);
    cout << a << b << c << endl;
    return 0;
}

Answer:
(a)
bool isSeven(int x) {
    return x == 7;
}

(b)
string removeLast(string x) {
    return x.substr(0, x.length() - 1);
}

(c)
string secondWord(ifstream &file) {
    string x;
    file >> x;
    file >> x;
    return x;
}

(d)
char firstChar(char x[]) {
    return x[0];
}
void swapBig(int &x, int &y, int &z) {
    int temp = x;
    if (x < y && z <= y) {
        x = y;
        y = temp;
    } else if (x < z) {
        x = z;
        z = temp;
    }
}

Problem 229  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    int a = 123, b = 3, c = 4;
    ifstream f;
    string s = "HELLO"; char t[] = "HELLO";
    f.open("testFile.txt");
    // (a) Tests whether a number has 3 digits, here Yes!
    if (is3digit(a)) cout << "Yes!" << endl;
    // (b) Returns the part of a string before its midpoint, here HE
    cout << halfIt(s) << endl;
    // (c) The number of characters read from the input file before eof() is true
    cout << countChar(f) << endl;
    // (d) Print third character of a C-string that has a middle, here L
    cout << thirdChar(t) << endl;
    // (e) Replace a, b and c by their sum to print 130, 130, 130
    replace(a, b, c);
    cout << a << "," << b << "," << c << endl;
    return 0;
}
```

Answer:
(a)
```cpp
bool is3digit(int x) {
    return (x > 99) && (x < 1000);
}
```

(b)
```cpp
string halfIt(string x) {
    return x.substr(0, x.length()/2);
}
```

(c)
```cpp
int countChar(ifstream &file) {
    char x;
    int count = 0;
    while (!file.eof()) {
        x = file.get();
        count++;
    }
    return count;
}
```
count++;  
}  
return count;  
}

(d)
char thirdChar(char x[]) {  
    return x[2];
}

(e)
vvoid replace(int &x, int &y, int &z) {
    x = x + y + z;
    y = x;
    z = x;
}

Problem 230 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

int main() {
    string s = "HELLO", t = "GOODBYE";
    // (a) Tests whether a string has 5 or more letters
    if (isLong(s)) cout << "Long!" << endl;
    // (b) Tests whether a string contains the letter E
    cout << hasE(s) << endl;
    // (c) Returns a string with just the first 4 characters
    cout << first4(t) << endl;
    // (d) Prints the last character at or before the middle of the string
    cout << middle(t) << endl;
    // (e) swaps them
    swap(s, t);
    cout << s << " " << t << endl;
    return 0;
}

Answer:
(a)
bool isLong(string x) {
    return x.length() > 4;
}

(b)
bool hasE(string x) {
    return x.find("E") >= 0;
}

(c)
Problem 231  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    string s = "HELLO", t = "GOODBYE";
    // (a) return number of characters
    cout << stringLength(s) << endl;
    // (b) Tests whether a string contains a target
    cout << contains(s, "HELL") << endl;
    // (c) Returns a string with just the last 4 characters
    cout << last4(t) << endl;
    // (d) Prints the first character
    cout << first(t) << endl;
    // (e) adds on the second string
    addOn(s, t);
    cout << s << endl;
    return 0;
}
```

**Answer:**

(a)  
```cpp
int stringLength(string x) {
    return x.length();
}
```

(b)  
```cpp
bool contains(string x, string target) {
    return x.find(target) >= 0;
}
```

(c)  
```cpp
string last4(string x) {
    return x.substr(x.length() - 4, 4);
}
```
Problem 232  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
int main() {
    string s = "HELLO", t = "GOODBYE";
    // (a) Tests whether a string starts in upper case
    if (isUpper(s)) cout << "Upper Case!" << endl;
    // (b) Tests whether a string omits the letter E
    cout << hasNoE(s) << endl;
    // (c) Returns a string that drops the first character
    cout << dropFirst(t) << endl;
    // (d) Prints the last character
    cout << last(t) << endl;
    // (e) If t is shorter than s, swap the strings, otherwise do nothing
    sort(s, t);
    cout << s << " " << t << endl;
    return 0;
}

Answer:

(a)

bool isUpper(string x) {
    return 'A' <= x[0] && x[0] <= 'Z';
}

(b)

bool hasNoE(string x) {
    return x.find("E") < 0;
}

(c)

string dropFirst(string x) {
    return x.substr(1);
}

(d)

char last(string x) {
    return x[x.length() - 1];
}
```
Problem 233  Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```cpp
void sort(string &x, string &y) {
    if (x.length() <= y.length()) return;
    string temp = x;
    x = y;
    y = temp;
}
```

```cpp
int main() {
    string s = "HELLO", t = "GOODBYE";
    // (a) Do two strings have the same number of characters?
    cout << sameLength(s, t) << endl;
    // (b) Tests whether a string contains a target
    cout << contains("HELL", s) << endl;
    // (c) Returns a string that drops the last character
    cout << dropLast(t) << endl;
    // (d) Prints the third character
    cout << third(t) << endl;
    // (e) Turns an upper case character to lower case
    lower(s[0]);
    cout << s << endl;
    return 0;
}
```

**Answer:**

(a)

```cpp
bool sameLength(string x, string y) {
    return x.length() == y.length();
}
```

(b)

```cpp
bool contains(string target, string x) {
    return x.find(target) >= 0;
}
```

(c)

```cpp
string dropLast(string x) {
    return x.substr(0, x.length() - 1);
}
```

(d)

```cpp
char third(string x) {
    return x[2];
}
```
void lower(char &x) {
    if ('A' <= x && x <= 'Z') x = x + 'a' - 'A';
}

Problem 234  Write a function called *subtractAverage* that calculates the average of the entries in a 2-dimensional array (that is known to have 2 columns) and subtracts this average from every entry of the array.

For example, a program that uses the function *subtractAverage* follows.

```c
int main() {
    double x[3][2] = {{1,3}, {1,3}, {1,3}} ; // average is 2 here
    subtractAverage(x, 3, 2);
    cout << x[0][0] << " " << x[0][1] << endl; // prints: -1 1
    return 0;
}
```

Answer:

```c
void subtractAverage(double x[][2], int rows, int cols) {
    double sum = 0;
    for (int r = 0; r < rows; r++)
        for (int c = 0; c < cols; c++) sum += x[r][c];
    double average = sum / (rows * cols);
    for (int r = 0; r < rows; r++)
        for (int c = 0; c < cols; c++) x[r][c] -= average;
}
```

Problem 235  Write a function called *addMin* that calculates the minimum of the entries in a 2-dimensional array (that is known to have 2 columns) and adds this minimum to every entry of the array.

For example, a program that uses the function *addMin* follows.

```c
int main() {
    int x[3][2] = {{1,3}, {1,3}, {1,3}} ; // min is 1 here
    addMin(x, 3, 2);
    cout << x[0][0] << " " << x[0][1] << endl; // prints: 2 4
    return 0;
}
```

Answer:

```c
void addMin(int x[][2], int rows, int cols) {
    int min = x[0][0];
    for (int r = 0; r < rows; r++)
        for (int c = 0; c < cols; c++)
            if (x[r][c] < min) min = x[r][c];
    for (int r = 0; r < rows; r++)
        for (int c = 0; c < cols; c++)
            x[r][c] += min;
}
```

Problem 236  Write a function called *subtractAverage* that calculates the average of the entries in an array and subtracts this average from every positive entry of the array.

For example, a program that uses the function *subtractAverage* follows.

```c
int main() {
    double x[3][2] = {{1,3}, {1,3}, {1,3}} ; // average is 2 here
    subtractAverage(x, 3, 2);
    cout << x[0][0] << " " << x[0][1] << endl; // prints: -1 1
    return 0;
}
```
int main() {
    double x[5] = {3, 1, 4, 1, 6}; // average is 3 here
    subtractAverage(x, 5);
    cout << x[0] << " " << x[1] << x[2] << endl; // prints: 0 -2 1
    return 0;
}

Answer:

void subtractAverage(double x[], int capacity) {
    double sum = 0;
    for (int r = 0; r < capacity; r++) sum += x[r];
    double average = sum / capacity;
    for (int r = 0; r < capacity; r++)
        if (x[r] > 0) x[r] -= average;
}

Problem 237  Write a function called addMin that calculates the minimum of the entries in an array and adds this minimum to every odd entry of the array.

For example, a program that uses the function addMin follows.

int main() {
    int x[5] = {3, 1, 4, 1, 5}; // min is 1 here
    addMin(x, 5);
    cout << x[0] << " " << x[1] << " " << x[2] << endl; // prints: 4 2 4
    return 0;
}

Answer:

void addMin(int x[], int cols) {
    int min = x[0];
    for (int c = 0; c < cols; c++)
        if (x[c] < min) min = x[c];
    for (int c = 0; c < cols; c++)
        if (x[c] % 2 == 1)
            x[c] += min;
}

Problem 238  Write a function called minGap that calculates the smallest gap between adjacent entries of an array. (A gap between two numbers is the absolute value of their difference.)

For example, a program that uses the function minGap follows.

int main() {
    int x[5] = {3, 1, 4, 1, 5};
    cout << minGap(x, 5) << endl; // prints 2 corresponding to the gap from 3 to 1.
    return 0;
}

Answer:

int minGap(int x[], int cap) {
    int ans = x[1] - x[0];
    if (ans < 0) ans = -ans;
    for (int i = 1; i < cap; i++)
        if (x[i] > 0) x[i] -= average;
}
if (x[i] > x[i-1]) {
    if ((x[i] - x[i-1]) < ans)
        ans = x[i] - x[i - 1];
} else {
    if ((x[i-1] - x[i]) < ans)
        ans = x[i - 1] - x[i];
}
}
return ans;

Problem 239 Write a function called *gapSum* that calculates the sum of the gaps between adjacent entries of an array. (A gap between two numbers is the absolute value of their difference.)

For example, a program that uses the function *gapSum* follows.

```c
int main() {
    int x[5] = {3, 1, 4, 1, 5};
    cout << gapSum(x, 5) << endl; // prints 12
    // The gaps are 2, 3, 3, 4 and these add to 12
    return 0;
}
Answer:

int gapSum(int x[], int cap) {
    int ans = 0;
    for (int i = 1; i < cap; i++) {
        if (x[i] > x[i-1]) {
            ans = ans + x[i] - x[i - 1];
        } else {
            ans = ans + x[i - 1] - x[i];
        }
    }
    return ans;
}
```

Problem 240 Write a function called *maxGap* that calculates the biggest gap between adjacent entries of an array. (A gap between two numbers is the absolute value of their difference.)

For example, a program that uses the function *maxGap* follows.

```c
int main() {
    int x[5] = {3, 1, 4, 1, 5};
    cout << maxGap(x, 5) << endl; // prints 4 corresponding to the gap from 1 to 5.
    return 0;
}
Answer:

int maxGap(int x[], int cap) {
    int ans = 0;
    for (int i = 1; i < cap; i++) {
        if ((x[i] - x[i-1]) > ans)
            ans = x[i] - x[i - 1];
        if ((x[i-1] - x[i]) > ans)
            ans = x[i - 1] - x[i];
    }
    return ans;
}
Problem 241 Write a function called *gapProd* that calculates the product of the gaps between adjacent entries of an array. (A gap between two numbers is the absolute value of their difference.)

For example, a program that uses the function *gapProd* follows.

```c
int main() {
    int x[5] = {3, 1, 4, 1, 5};
    cout << gapProd(x, 5) << endl; // prints 72
    // The gaps are 2, 3, 3, 4 and these multiply to 72
    return 0;
}
```

*Answer:*

```c
int gapProd(int x[], int cap) {
    int ans = 1;
    for (int i = 1; i < cap; i++) {
        if (x[i] > x[i-1]) {
            ans = ans * (x[i] - x[i - 1]);
        } else {
            ans = ans * (x[i - 1] - x[i]);
        }
    }
    return ans;
}
```

Problem 242 Write a function called *roundOff* that returns the result of turning all digits (except the first) in a positive integer parameter to 0.

For example, a program that uses the function *roundOff* follows.

```c
int main() {
    cout << roundOff(19683) << endl; // prints 10000
    cout << roundOff(2) << endl; // prints 2
    return 0;
}
```

*Answer:*

```c
int roundOff(int x) {
    if (x < 10) return x;
    return 10* roundOff(x/10);
}
```

Problem 243 Write a function called *allFirst* that returns the result of turning all digits in a positive integer parameter to match the first digit.

For example, a program that uses the function *allFirst* follows.

```c
int main() {
    cout << allFirst(19683) << endl; // prints 11111
    cout << allFirst(2048) << endl; // prints 2222
    return 0;
}
```

*Answer:*

```c
int allFirst(int x) {
    if (x < 10) return x;
    int y = allFirst(x/10);
    return 10*y + y%10;
}
```
Problem 244  Write a function called firstDown that returns the result of decreasing the first digit in a positive integer by 1.
For example, a program that uses the function firstDown follows.

```cpp
int main() {
    cout << firstDown(2048) << endl; // prints 1048
    cout << firstDown(19683) << endl; // prints 9683
    return 0;
}
```

**Answer:**

```cpp
int firstDown(int x) {
    if (x < 10) return x - 1;
    return 10 * firstDown(x/10) + x % 10;
}
```

Problem 245  Write a function called firstUp that returns the result of increasing the first digit of the parameter by 1, unless this first digit is 9 in which case it is not changed.
For example, a program that uses the function firstUp follows.

```cpp
int main() {
    cout << firstUp(19683) << endl; // prints 29683
    cout << firstUp(95) << endl; // prints 95
    return 0;
}
```

**Answer:**

```cpp
int firstUp(int x) {
    if (x < 9) return x + 1;
    if (x == 9) return x;
    return 10 * firstUp(x/10) + x % 10;
}
```

Problem 246  Write a function called oddOne that returns the result of turning all odd digits in a positive integer parameter to 1.
For example, a program that uses the function oddOne follows.

```cpp
int main() {
    cout << oddOne(19683) << endl; // prints 11681
    cout << oddOne(2) << endl; // prints 2
    return 0;
}
```

**Answer:**

```cpp
int oddOne(int x) {
    if (x == 0) return 0;
    if (x % 2 == 0) return 10 * oddOne(x/10) + x % 10;
    return 10 * oddOne(x/10) + 1;
}
```

Problem 247  Write a function called oddOneOut that returns the result of removing the rightmost odd digit in a positive integer parameter.
For example, a program that uses the function oddOneOut follows.
int main() {
    cout << oddOneOut(19682) << endl; // prints 1682
    cout << oddOneOut(2) << endl; // prints 2
    return 0;
}

Answer:

int oddOneOut(int x) {
    if (x == 0) return 0;
    if (x % 2 == 1) return x/10;
    return 10 * oddOneOut(x/10) + x % 10;
}

Problem 248 Write a function called eveNine that returns the result of turning all even digits in a positive integer parameter to 9.
For example, a program that uses the function eveNine follows.

int main() {
    cout << eveNine(19683) << endl; // prints 19993
    cout << eveNine(3) << endl; // prints 3
    return 0;
}

Answer:

int eveNine(int x) {
    if (x == 0) return 0;
    if (x % 2 != 0) return 10 * eveNine(x/10) + x % 10;
    return 10 * eveNine(x/10) + 9;
}

Problem 249 Write a function called evenOut that returns the result of removing the rightmost even digit in a positive integer parameter.
For example, a program that uses the function evenOut follows.

int main() {
    cout << evenOut(19683) << endl; // prints 1963
    cout << evenOut(2) << endl; // prints 0
    return 0;
}

Answer:

int evenOut(int x) {
    if (x == 0) return 0;
    if (x % 2 == 0) return x/10;
    return 10 * evenOut(x/10) + x % 10;
}

Problem 250 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It reads the entries in a 2-dimensional array with 4 rows and 4 columns from the user.
2. It prints (all) rows that have the greatest sum.
Here is an example of how the program should work:
Give me the entries of a 4 x 4 array:
0 0 0 -1
1 2 3 4
1 1 1 1
2 3 3 2

Largest rows:
1 2 3 4
2 3 3 2

Answer:

#include <iostream>
using namespace std;

int main() {
    int x[4][4];
    cout << "Give me the entries of a 4 x 4 array:" << endl;
    for (int i = 0; i < 4; i++)
        for (int j = 0; j < 4; j++) cin >> x[i][j];

    int sums[4] = {0, 0, 0, 0};
    for (int i = 0; i < 4; i++)
        for (int j = 0; j < 4; j++) sums[i] += x[i][j];

    int max = sums[0];
    for (int i = 1; i < 4; i++)
        if (sums[i] > max) max = sums[i];

    cout << "Largest rows\n";
    for (int i = 0; i < 4; i++) {
        if (sums[i] == max) {
            for (int j = 0; j < 4; j++) cout << x[i][j] << " ";
            cout << endl;
        }
    }
}

Problem 251 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It reads the entries in a 2-dimensional array with 5 rows and 3 columns from the user.
2. It prints the last row that has an even sum.
Here is an example of how the program should work:

Give me the entries of a 5 x 3 array:
0 0 0
1 2 3
1 1 1
3 3 3
1 1 1

Last row with even sum:
1 2 3

Answer:

#include <iostream>
using namespace std;

int main() {
    int x[5][3];
    cout << "Give me the entries of a 5 x 3 array:" << endl;
    for (int i = 0; i < 5; i++)
        for (int j = 0; j < 3; j++) cin >> x[i][j];

    int sums[5] = {0, 0, 0, 0, 0};
    for (int i = 0; i < 5; i++)
        for (int j = 0; j < 3; j++) sums[i] += x[i][j];

    cout << "Last row with even sum: \n";
    for (int i = 4; i >= 0; i--){
        if (sums[i] % 2 == 0) {
            for (int j = 0; j < 3; j++) cout << x[i][j] << " ";
            cout << endl;
            return 0;
        }
    }
    return 0;
}

Problem 252  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It reads the entries in a 2-dimensional array with 4 rows and 4 columns from the user.
2. It prints (all) columns that have the greatest sum.

Here is an example of how the program should work:

Give me the entries of a 4 x 4 array:
0 0 0 -1
1 2 3 4
1 1 1 1
2 3 3 2

Largest columns:
0 3 1 3

Answer:

#include <iostream>
using namespace std;

int main() {
    int x[4][4];
    cout << "Give me the entries of a 4 x 4 array:" << endl;
    for (int i = 0; i < 4; i++)
        for (int j = 0; j < 4; j++) cin >> x[i][j];

    int sums[4] = {0, 0, 0, 0};
    for (int i = 0; i < 4; i++)
        for (int j = 0; j < 4; j++) sums[j] += x[i][j];

    int max = sums[0];
    for (int i = 1; i < 4; i++)
        if (sums[i] > max) max = sums[i];
cout << "Largest columns\n";
for (int j = 0; j < 4; j++) {
    if (sums[j] == max) {
        for (int i = 0; i < 4; i++) cout << x[i][j] << " ";
        cout << endl;
    }
}
}

Problem 253  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It reads the entries in a 2-dimensional array with 5 rows and 3 columns from the user.
2. It prints the last column that has an even sum.
Here is an example of how the program should work:

Give me the entries of a 5 x 3 array:
0 0 0
1 2 3
1 1 1
3 3 3
1 2 0

Last column with even sum:
0 2 1 3 2

Answer:
#include <iostream>
using namespace std;

int main() {
    int x[5][3];
    cout << "Give me the entries of a 5 x 3 array:" << endl;
    for (int i = 0; i < 5; i++)
        for (int j = 0; j < 3; j++) cin >> x[i][j];

    int sums[5] = {0, 0, 0, 0, 0};
    for (int i = 0; i < 5; i++)
        for (int j = 0; j < 3; j++) sums[j] += x[i][j];

    cout << "Last column with even sum: \n";
    for (int i = 2; i >= 0; i--) {
        if (sums[i] % 2 == 0) {
            for (int j = 0; j < 5; j++) cout << x[j][i] << " ";
            cout << endl;
            return 0;
        }
    }
    return 0;
}

Problem 254  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It reads (from the user) the entries in a 2-dimensional array with 5 rows and 5 columns.
2. It prints (all) rows that have the property that entries increase as we move along their columns.
Here is an example of how the program should work:
Give me the entries of a 5 x 5 array:
0 0 0 0 0
1 2 3 4 5
1 5 6 7 99
2 -1 3 4 5
5 4 3 2 1

Increasing rows:
1 2 3 4 5
1 5 6 7 99

Answer:
#include <iostream>
using namespace std;

int main() {
    int x[5][5];
    cout << "Give me the entries of a 5 x 5 array:" << endl;
    for (int i = 0; i < 5; i++)
        for (int j = 0; j < 5; j++) cin >> x[i][j];

    cout << "Increasing rows\n";
    for (int i = 0; i < 5; i++) {
        bool ok = true;
        for (int j = 1; j < 5; j++)
            if (x[i][j] <= x[i][j - 1]) ok = false;
        if (ok) {
            for (int j = 0; j < 5; j++) cout << x[i][j] << " ";
            cout << endl;
        }
    }
}

Problem 255 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It reads (from the user) the entries in a 2-dimensional array with 5 rows and 5 columns.
2. It prints (all) columns that have the property that entries increase as we move down their rows.

Here is an example of how the program should work:

Give me the entries of a 5 x 5 array:
0 1 5 10 10
0 2 4 11 20
0 3 3 9 21
0 4 2 12 41
0 5 1 13 99

Increasing columns:
1 2 3 4 5
10 20 21 41 99

Answer:
#include <iostream>
using namespace std;

int main() {
Problem 256 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It reads (from the user) the entries in a 2-dimensional array with 5 rows and 5 columns.
2. It prints (all) rows that have the property that entries decrease as we move along their columns.

Here is an example of how the program should work:

Give me the entries of a 5 x 5 array:
0 0 0 0 0
1 2 3 4 5
501 5 306 107 99
2 -1 -3 -4 -5
5 4 3 2 1

Decreasing rows:
2 -1 -3 -4 -5
5 4 3 2 1

Answer:

#include <iostream>
using namespace std;

int main() {
    int x[5][5];
    cout << "Give me the entries of a 5 x 5 array:" << endl;
    for (int i = 0; i < 5; i++)
        for (int j = 0; j < 5; j++) cin >> x[i][j];

    cout << "Decreasing rows\n";
    for (int i = 0; i < 5; i++)
        for (int j = 1; j < 5; j++)
            if (x[i][j] >= x[i][j - 1]) ok = false;
        if (ok) {
            for (int j = 0; j < 5; j++)
                cout << x[i][j] << " ";
            cout << endl;
        }
}
}
Problem 257  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It reads (from the user) the entries in a 2-dimensional array with 5 rows and 5 columns.
2. It prints (all) columns that have the property that entries decrease as we move down their rows.
Here is an example of how the program should work:

Give me the entries of a 5 x 5 array:
0 1 5 10 99
0 2 4 11 41
0 3 3 9 21
0 4 2 12 20
0 5 1 13 10

Decreasing columns:
5 4 3 2 1
99 41 21 20 10

Answer:

#include <iostream>
using namespace std;

int main() {
    int x[5][5];
    cout << "Give me the entries of a 5 x 5 array:" << endl;
    for (int i = 0; i < 5; i++)
        for (int j = 0; j < 5; j++) cin >> x[i][j];

    cout << "Decreasing columns\n";
    for (int j = 0; j < 5; j++) {
        bool ok = true;
        for (int i = 1; i < 5; i++)
            if (x[i][j] >= x[i - 1][j]) ok = false;
        if (ok) {
            for (int i = 0; i < 5; i++) cout << x[i][j] << " ";
            cout << endl;
        }
    }
}

Problem 258  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter an integer \( n \) that is between 1 and 21.
2. It terminates if the user supplies an illegal value for \( n \).
3. It prints out a triangular picture with \( n \) rows like the one shown in the example (below). The triangle has a vertical left edge and a horizontal bottom edge. Odd numbered rows of the triangle are made from the letter A and even numbered rows with the letter B, as in the example.
Here is an example of how the program should work:

Give me an integer between 1 and 21: 9
A
BB
AAA
BBBB
AAAAA
BBBBBB
#include <iostream>
using namespace std;

int main() {  
    int n;
    cout << "Give me an integer between 1 and 21:";
    cin >> n;

    if (n < 1 || n > 21) return 0;
    for (int r = 0; r < n; r++) {  
        for (int c = 0; c <= r; c++)
            cout << (char) ('A' + r % 2);
        cout << endl;
    }
}

Problem 259  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter an integer \( n \) that is between 1 and 23.
2. It terminates if the user supplies an illegal value for \( n \).
3. It prints out a triangular picture with \( n \) rows like the one shown in the example (below). The triangle has a vertical right edge and a horizontal top edge. Odd numbered rows of the triangle are made from the letter x and even numbered rows with the letter y, as in the example.

Here is an example of how the program should work:

Give me an integer between 1 and 23:  5
xxxxx
yyyy
xxx
yy
x

Answer:

#include <iostream>
using namespace std;

int main() {  
    int n;
    cout << "Give me an integer between 1 and 23:";
    cin >> n;

    if (n < 1 || n > 23) return 0;
    for (int r = 0; r < n; r++) {  
        for (int c = 0; c < n; c++)
            if (c < r) cout << " ";
            else cout << (char) ('x' + r % 2);
        cout << endl;
    }
}

Problem 260  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer \( n \) that is between 1 and 16.
2. It terminates if the user supplies an illegal value for \( n \).
3. It prints out a triangular picture with \( n \) rows like the one shown in the example (below). The triangle has a vertical left edge and a horizontal bottom edge. Odd numbered columns of the triangle are made from the letter A and even numbered columns with the letter B, as in the example.

Here is an example of how the program should work:

Give me an integer between 1 and 16: 6
A
AB
ABA
ABAB
ABABA
ABABAB

Answer:

```
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 16:";
    cin >> n;
    if (n < 1 || n > 16) return 0;
    for (int r = 0; r < n; r++) {
        for (int c = 0; c <= r; c++)
            cout << (char) ('A' + c % 2);
        cout << endl;
    }
}
```

Problem 261  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer \( n \) that is between 1 and 18.
2. It terminates if the user supplies an illegal value for \( n \).
3. It prints out a triangular picture with \( n \) rows like the one shown in the example (below). The triangle has a vertical right edge and a horizontal top edge. Odd numbered columns of the triangle are made from the letter x and even numbered columns with the letter y, as in the example.

Here is an example of how the program should work:

Give me an integer between 1 and 18: 5
xyxyx
xyyx
xyx
yx
x

Answer:

```
#include <iostream>
using namespace std;

```

```
int main() {
    int n;
    cout << "Give me an integer between 1 and 18:";
    cin >> n;

    if (n < 1 || n > 18) return 0;
    for (int r = 0; r < n; r++) {
        for (int c = 0; c < n; c++)
            if (c < r) cout << " ";
            else cout << (char) ('x' + c % 2);
        cout << endl;
    }
}

Problem 262 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

int main() {
    int x = 1, y = 10, z = 19;
    double b[5] = {1.9, 2.3, 3.0};
    int d[2][2] = {{1,2},{3,4}};

    b[1] = divide(z, y); // (a) sets b[1] to quotient 2
    reset(d[1][1], x); // (b) replaces d[1][1] by value of x
    cout << bigRow(d, 2, 2); // (c) prints biggest row: 3 4
    printAll(b, 3); // (d) prints array: 1.9 2.3 3.0
    cout << add(d[0][0], b[2]) << endl; // (e) prints the sum 4
    return 0;
}

(a) Title line for divide.
Answer:
double divide(int z, int y)

(b) Title line for reset.
Answer:
void reset(int &x, int y)

(c) Title line for bigRow.
Answer:
string bigRow(int d[][2], int r, int c)

(d) Title line for printAll.
Answer:
void printAll(double b[], int cap)

(e) Title line for add.
Answer:
int add(int x, double y)
Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string fun(int x) {
    string ans = "9876543210";
    if (x <= 10) return "0";
    if ((x <= 30) || (x > 10000)) return ans.substr(x % 10);
    if ((x >= 0) && (x < 100)) return "x+1";
    return ans.substr(x%4, x%4);
}

int nuf(int &x) {
    cout << x << endl;
    x = x * x - 3;
    return x;
}

int main() {
    int x = 2;
    cout << fun(23) << endl; // line (a)
    cout << fun(233) << endl; // line (b)
    cout << fun(2333) << endl; // line (c)
    nuf(x); // line (d)
    cout << nuf(x) << endl; // line (e)
}
```

(a) What is the output at line (a)?
Answer: 6543210

(b) What is the output at line (b)?
Answer: 8

(c) What is the output at line (c)?
Answer: 8

(d) What is the output at line (d)?
Answer: 2

(e) What is the output at line (e)?
Answer: 1

~2

Problem 264 Write a function called `smallRow` that calculates and returns the smallest possible sum of entries of any row in a 2-dimensional array.

For example, a program that uses the function `smallRow` follows.
int main() {
    int x[2][3] = {{3, 1, 4}, {1, 5, 9}};
    cout << smallRow (x, 2, 3) << endl;
    // from the 2-d array x that has size 2 x 3, find the smallest row sum
    // output will be 8 since row #0 contains 3, 1 and 4 is smallest.
    return 0;
}

Answer:

int smallRow(int x[][3], int r, int c) {
    int ans;
    for (int row = 0; row < r; row++) {
        int sum = 0;
        for (int col = 0; col < c; col++)
            sum += x[row][col];
        if (row == 0 || sum < ans) ans = sum;
    }
    return ans;
}

Problem 265 Write a function called bond that changes any sequence of digits 006 to 007 in a positive integer parameter.

For example, a program that uses the function bond follows.

int main() {
    cout << bond(4006) << endl; // prints 4007
    cout << bond(4006006) << endl; // prints 4007007
    cout << bond(106) << endl; // prints 106
    cout << bond(1006) + 1 << endl; // prints 1008
    return 0;
}

Answer:

int bond(int x) {
    if (x <= 0) return 0;
    if (x % 1000 == 6) return 1000 * bond(x / 1000) + 7;
    return 10 * bond(x / 10) + x % 10;
}

Problem 266 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer $n$ that is between 1 and 24.
2. It terminates if the user supplies an illegal value for $n$.
3. It prints out a triangular picture with $n$ rows like the one shown in the example (below). The triangle has a vertical right edge and a horizontal top edge. The right edge is formed from the letter A, next to it is a vertical line formed from the letter B, then one formed from the letter C and so on. The top edge is also formed from the letter A, just below it is a line formed from the letter B and so on as in the example. Here is an example of how the program should work:

Give me an integer between 1 and 24: 8
AAAAAAA
BBBBBBBA
CCCCBA
DDCBA
#include <iostream>
using namespace std;

int main() {
    int n;
    char picture[24][24];
    cout << "Give me an integer between 1 and 24:";
    cin >> n;

    if (n < 1 || n > 24) {
        cout << "Illegal." << endl;
        return 0;
    }
    int mid = (n + 1) / 2;

    char letter = 'A';
    for (int step = 0; step < mid; step++) {
        for (int r = step; r < n - step; r++)
            for (int c = step; c < n - step; c++)
                picture[r][c] = letter;
        letter++;
    }

    for (int r = 0; r < n; r++)
        for (int c = 0; c < n; c++)
            if (r <= c) cout << picture[r][c];
            else cout << " ";
    cout << endl;
}

Problem 267 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

int main() {
    int x = 0, y = 1, z = 2;
    double b[3] = {1.9, 2.3, 3.0};
    int d[2][2] = {{1,2},{3,4}};

    x = diffTwo(y, b[0]); // (a) sets x to approx difference 1
    swap(d[1][1], x); // (b) swaps x with value of d[1][1]
    cout << biggest(d, 2, 2); // (c) prints biggest row: 3 4
    printThree(b); // (d) prints three entries: 1.9 2.3 3.0
    summit(b[2], d[0][0]); // (e) prints the sum 4
    return 0;
}

(a) Title line for diffTwo.
Answer:

int diffTwo(int y, double z)
(b) Title line for swap.
Answer:

```cpp
void swap(int &x, int &y)
```

(c) Title line for biggest.
Answer:

```cpp
string biggest(int d[][2], int r, int c)
```

(d) Title line for printThree.
Answer:

```cpp
void printThree(double b[])
```

(e) Title line for summit.
Answer:

```cpp
void summit(double x, int y)
```

**Problem 268** Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string fun(int x) {
    string ans = "0123456789";
    if (x <= 0) return "0";
    if ((x <= 10) || (x > 10000)) return ans.substr(x % 10);
    if ((x >= 0) && (x < 100)) return "x+1";
    return ans.substr(x%4, x%4);
}

int nuf(int &x) {
    cout << x << endl;
    x = x * x;
    return x - 6;
}

int main() {
    int x = 4;
    cout << fun(3) << endl; // line (a)
    cout << fun(32) << endl; // line (b)
    cout << fun(323) << endl; // line (c)
    nuf(x); // line (d)
    cout << nuf(x) << endl; // line (e)
}
```

(a) What is the output at line (a)?
Answer:

```
3456789
```

(b) What is the output at line (b)?
Answer:

```
x+1
```
(c) What is the output at line (c)?

**Answer:**

345

(d) What is the output at line (d)?

**Answer:**

4

(e) What is the output at line (e)?

**Answer:**

16

250

**Problem 269** Write a function called `smallCol` that calculates and returns the smallest possible sum of entries of any column in a 2-dimensional array.

For example, a program that uses the function `smallCol` follows.

```cpp
int main() {
    int x[2][3] = {{3, 1, 4}, {1, 5, 9}};
    cout << smallCol (x, 2, 3) << endl;
    // from the 2-d array x that has size 2 x 3, find the smallest col sum
    // output will be 4 since col #0 contains 3 and 1 is smallest.
    return 0;
}
```

**Answer:**

```cpp
int smallCol(int x[][3], int r, int c) {
    int ans;
    for (int col = 0; col < c; col++) {
        int sum = 0;
        for (int row = 0; row < r; row++)
            sum += x[row][col];
        if (col == 0 || sum < ans) ans = sum;
    }
    return ans;
}
```

**Problem 270** Write a function called `bond` that inserts a digit 0 before any digit pair 07 in a positive integer parameter.

For example, a program that uses the function `bond` follows.

```cpp
int main() {
    cout << bond(407) << endl; // prints 4007
    cout << bond(401) << endl; // prints 401
    cout << bond(40707) << endl; // prints 4007007
    cout << bond(107) + 1 << endl; // prints 1008
    return 0;
}
```

**Answer:**
int bond(int x) {
    if (x <= 0) return 0;
    if (x % 100 == 7) return 100 * bond(x / 10) + 7;
    return 10 * bond(x / 10) + x % 10;
}

Problem 271 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter an integer \( n \) that is between 1 and 23.
2. It terminates if the user supplies an illegal value for \( n \).
3. It prints out a triangular picture with \( n \) rows like the one shown in the example (below). The triangle has a vertical right edge and a horizontal bottom edge. The right edge is formed from the letter A, next to it is a vertical line formed from the letter B, then one formed from the letter C and so on. The bottom edge is also formed from the letter A, just above it is a line formed from the letter B and so on as in the example.
Here is an example of how the program should work:

Give me an integer between 1 and 23: 9

A
BA
CBA
DCBA
EDCBA
DDDCBA
CCCCCBA
BBBBBBBA
AAAAAAAAA

Answer:

#include <iostream>
using namespace std;

int main() {
    int n;
    char picture[23][23];
    cout << "Give me an integer between 1 and 23: ";
    cin >> n;

    if (n < 1 || n > 23) {
        cout << "Illegal." << endl;
        return 0;
    }
    int mid = (n + 1) / 2;

    char letter = 'A';
    for (int step = 0; step < mid; step++) {
        for (int r = step; r < n - step; r++)
            for (int c = step; c < n - step; c++)
                picture[r][c] = letter;
        letter++;
    }

    for (int r = 0; r < n; r++)
        for (int c = 0; c < n; c++)
            if ((r + c) >= (n - 1)) cout << picture[r][c];
            else cout << " ";
    cout << endl;
Problem 272  Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    int x = 0, y = 1, z = 2;
    double b[3] = {1.9, 2.3, 3.0};
    int d[2][2] = {{1,2},{3,4}};
    cout << twoD(y, b[0]) << endl; // (a) prints difference: 0.9
    y = addUp(d[1][1], y); // (b) sets y to sum 4 + 1
    cout << firstElt(d, 2, 2); // (c) prints last element: 1
    b[2] = av(b, 3); // (d) sets as average
    setOne(b[2], d[0][0]); // (e) sets both to 1
    return 0;
}
```

(a) Title line for `twoD`.
**Answer:**

double twoD(int a, double b)

(b) Title line for `addUp`.
**Answer:**

int addUp(int x, int y)

(c) Title line for `firstElt`.
**Answer:**

int firstElt(int d[][2], int r, int c)

(d) Title line for `av`.
**Answer:**

double av(double b[], int cap)

(e) Title line for `setOne`.
**Answer:**

void setOne(double &x, int &y)

Problem 273  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string fun(int x) {
    string ans = "0123456789";
    if (x <= 10) return "0";
    if ((x <= 30) || (x > 10000)) return ans.substr(x % 10);
    if ((x >= 0) && (x < 100)) return "x+1";
    return ans.substr(x%4, x%4);
}
```
```cpp}
int nuf(int &x) {
    cout << x << endl;
    x = x * x;
    return x;
}

int main() {
    int x = 2;
    cout << fun(2) << endl;    // line (a)
    cout << fun(22) << endl;   // line (b)
    cout << fun(222) << endl;  // line (c)
    nuf(x);                    // line (d)
    cout << nuf(x) << endl;    // line (e)
}
```

(a) What is the output at line (a)?
**Answer:**
0

(b) What is the output at line (b)?
**Answer:**
23456789

(c) What is the output at line (c)?
**Answer:**
23

(d) What is the output at line (d)?
**Answer:**
2

(e) What is the output at line (e)?
**Answer:**
4

16

**Problem 274**  Write a function called `bigRow` that calculates and returns the biggest possible sum of entries of any row in a 2-dimensional array.

For example, a program that uses the function `bigRow` follows.

```cpp
int main() {
    int x[2][3] = {{3, 1, 4}, {1, 5, 9}};
    cout << bigRow (x, 2, 3) << endl;
        // from the 2-d array x that has size 2 x 3, find the biggest row sum
        // output will be 15 since row #1 contains 1, 5 and 9 is biggest.
    return 0;
}
```

**Answer:**
```cpp
int bigRow(int x[][3], int r, int c) {
    int ans;
    for (int row = 0; row < r; row++) {
        int sum = 0;
        for (int col = 0; col < c; col++)
            sum += x[row][col];
        if (row == 0 || sum > ans) ans = sum;
    }
    return ans;
}

Problem 275 Write a function called bond that inserts the digit 7 after any pair of zero digits in a positive integer parameter.

For example, a program that uses the function bond follows.

```cpp
int main() {
    cout << bond(400) << endl; // prints 4007
    cout << bond(401) << endl; // prints 41
    cout << bond(4007) << endl; // prints 40077
    cout << bond(400) + 1 << endl; // prints 4008
    return 0;
}
```

Answer:

```cpp
int bond(int x) {
    if (x <= 0) return 0;
    if (x % 100 == 0) return 1000 * bond(x / 100) + 7;
    return 10 * bond(x / 10) + x % 10;
}
```

Problem 276 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer n that is between 1 and 22.
2. It terminates if the user supplies an illegal value for n.
3. It prints out a triangular picture with n rows like the one shown in the example (below). The triangle has a vertical left edge and a horizontal top edge. The left edge is formed from the letter A, next to it is a vertical line formed from the letter B, then one formed from the letter C and so on. The top edge is also formed from the letter A, just below it is a line formed from the letter B and so on as in the example.

Here is an example of how the program should work:

```cpp
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 22: ";
    cin >> n;
    if (n < 1 || n > 22) { // Error handling
        cout << "Illegal value for n.
```

Answer:
int main() {
    int n;
    char picture[22][22];
    cout << "Give me an integer between 1 and 22:";
    cin >> n;

    if (n < 1 || n > 22) {
        cout << "Illegal." << endl;
        return 0;
    }
    int mid = (n + 1) / 2;

    char letter = 'A';
    for (int step = 0; step < mid; step++) {
        for (int r = step; r < n - step; r++)
            for (int c = step; c < n - step; c++)
                picture[r][c] = letter;
        letter++;
    }

    for (int r = 0; r < n; r++)
        for (int c = 0; c < n; c++)
            if ((r + c) < n) cout << picture[r][c];
            else cout << " ";
        cout << endl;
}

Problem 277  Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

int main() {
    double x = 0, y = 1, z = 2;
    int b[3] = {1, 2, 3};
    double d[2][2] = {{1.9,2},{3.9,4}};

    cout << add3(b[0], y, d[0][0]) << endl; // (a) prints sum: 3.9
    y = addUp(d[1][1], x) + 1; // (b) sets y to sum 4.0 + 0 + 1
    cout << col(d, 2, 2, 0); // (c) prints column 0 as: 1.9,3.9
    b[0] = min(b, 3); // (d) sets as min element
    decrease(b[2], d[0][0]); // (e) decreases both by 1
    return 0;
}

(a) Title line for `add3`.
Answer:

double add3(int a, double b, double c)

(b) Title line for `addUp`.
Answer:

double addUp(double x, double y)

(c) Title line for `col`.
Answer:
Problem 278    Consider the following C++ program.

#include <iostream>
using namespace std;

string fun(int x) {
    string ans = "0123456789";
    if (x <= 10) return "0";
    if ((x <= 30) || (x > 10000)) return ans.substr(x % 10);
    if ((x >= 0) && (x < 100)) return "x+1";
    return ans.substr(x%4, x%4);
}

int nuf(int &x) {
    cout << x << endl;
    x = x * x;
    return x;
}

int main() {
    int x = 4;
    cout << fun(3) << endl;    // line (a)
    cout << fun(33) << endl;   // line (b)
    cout << fun(333) << endl;  // line (c)
    nuf(x);                     // line (d)
    cout << nuf(x) << endl;    // line (e)
}

(a) What is the output at line (a)?
Answer:
0

(b) What is the output at line (b)?
Answer:
x+1

(c) What is the output at line (c)?
Answer:
1

(d) What is the output at line (d)?
Answer:
(e) What is the output at line (e)?

**Answer:**

16
256

**Problem 279** Write a function called `bigCol` that calculates and returns the biggest possible sum of entries of any column in a 2-dimensional array.

For example, a program that uses the function `bigCol` follows.

```cpp
int main() {
    int x[2][3] = {{3, 1, 4}, {1, 5, 9}};
    cout << bigCol(x, 2, 3) << endl;
    // from the 2-d array x that has size 2 x 3, find the biggest col sum
    // output will be 13 since col #2 contains 4 and 9 is biggest.
    return 0;
}
```

**Answer:**

```cpp
int bigCol(int x[][3], int r, int c) {
    int ans;
    for (int col = 0; col < c; col++) {
        int sum = 0;
        for (int row = 0; row < r; row++)
            sum += x[row][col];
        if (col == 0 || sum > ans) ans = sum;
    }
    return ans;
}
```

**Problem 280** Write a function called `bond` that the insert the digits 07 after each digit 0 in a positive integer parameter.

For example, a program that uses the function `bond` follows.

```cpp
int main() {
    cout << bond(40) << endl; // prints 4007
    cout << bond(41) << endl; // prints 41
    cout << bond(400) << endl; // prints 4007007
    cout << bond(10) + 1 << endl; // prints 1008
    return 0;
}
```

**Answer:**

```cpp
int bond(int x) {
    if (x <= 0) return 0;
    if (x % 10 == 0) return 1000 * bond(x / 10) + 7;
    return 10 * bond(x / 10) + x % 10;
}
```

**Problem 281** Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter an integer \( n \) that is between 1 and 21.
2. It terminates if the user supplies an illegal value for \( n \).
3. It prints out a triangular picture with \( n \) rows like the one shown in the example (below). The triangle has a vertical left edge and a horizontal bottom edge. The left edge is formed from the letter A, next to it is a vertical line formed from the letter B, then one formed from the letter C and so on. The bottom edge is also formed from the letter A, just above it is a line formed from the letter B and so on as in the example.

Here is an example of how the program should work:

Give me an integer between 1 and 21: 9
A
AB
ABC
ABCD
ABCDE
ABCDDD
ABCCCCC
ABBBBBBBB
AAAAAAAAAA

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int n;
    char picture[21][21];
    cout << "Give me an integer between 1 and 21:"; 
    cin >> n;
    if (n < 1 || n > 21) {
        cout << "Illegal." << endl;
        return 0;
    }
    int mid = (n + 1) / 2;
    char letter = 'A';
    for (int step = 0; step < mid; step++) {
        for (int r = step; r < n - step; r++)
            for (int c = step; c < n - step; c++)
                picture[r][c] = letter;
        letter++;
    }
    for (int r = 0; r < n; r++)
        for (int c = 0; c < n; c++)
            if (r >= c) cout << picture[r][c];
            else cout << " ";
        cout << endl;
}
```

**Problem 282** Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    int x = 0, y = 1, z = 2;
```
Problem 283    Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string fun(int x) {
    string ans = "012345";
    if (x <= 0) return "";
    if ((x >= 30) && (x < 1000)) return ans.substr(x % 5);
    if ((x >= 0) || (x < 100)) return "xyz";
    return ans;
}

int up(int &x) {
    x += 3;
    cout << x << endl;
    return x - 1;
}

int main() {
    int b[3] = {1, 2, 3};
    double d[2][2] = {{1.9, 2}, {3.9, 4}};
    cout << sum3(b[0], y, d[0][0]) << endl;  // (a) prints sum: 3.9
    y = addUp(x, d[1][1]) + 1;           // (b) sets y to sum 0 + 4.0 + 1
    cout << col0(d, 2, 2);              // (c) prints column as: 1.9, 3.9
    b[0] = max(b, 3);                   // (d) sets as max element
    increase(b[2], d[0][0]);          // (e) increases both by 1
    return 0;
```
int x = 7;
cout << fun(0) << endl;  // line (a)
cout << fun(33) << endl;  // line (b)
cout << fun(3003) << endl; // line (c)
up(x);                // line (d)
cout << up(x) << endl;  // line (e)
}

(a) What is the output at line (a)?
Answer:

(b) What is the output at line (b)?
Answer:
345

(c) What is the output at line (c)?
Answer:
xyz

(d) What is the output at line (d)?
Answer:
10

(e) What is the output at line (e)?
Answer:
13
12

**Problem 284**  Write a function called `rowProd` that calculates and returns the product of the entries of a specified row of a 2-dimensional array.

For example, a program that uses the function `rowProd` follows.

```cpp
int main() {
    int x[2][3] = {{3, 1, 4}, {1, 5, 9}};
cout << rowProd (x, 2, 3, 1) << endl;
    // from the 2-d array x that has size 2 x 3, find the product of row 1
    // output will be 45 since row #1 contains 1, 5 and 9.
    return 0;
}
```

Answer:

```cpp
int rowProd(int x[][3], int r, int c, int row) {
    int ans = 1;
    for (int j = 0; j < c; j++)
        ans *= x[row][j];
    return ans;
}
```

**Problem 285**  Write a function called `numOdd` that the returns the number of digits in a positive integer parameter that are odd.

For example, a program that uses the function `numOdd` follows.
int main() {
    cout << numOdd(777) << endl;  // prints 3
    cout << numOdd(747) << endl;  // prints 2
    cout << numOdd(42) << endl;   // prints 0
    return 0;
}

Answer:

int numOdd(int x) {
    if (x <= 0) return 0;
    if (x % 2 != 0) return numOdd(x / 10) + 1;
    return numOdd(x / 10);
}

Problem 286  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an odd integer $n$ that is between 1 and 19.
2. It repeatedly reads $n$ from the user until the supplied value of $n$ is legal.
3. It prints out a triangular picture (as shown in the diagram, but with $n$ characters in the first row). Reading from the right, along each row the characters to be used is the sequence of uppercase letters A, B, C, ..., and so on.

Here is an example of how the program should work:

Give me an odd integer between 1 and 19:  7
GFEDCBA
EDCBA
CBA
A

Answer:

#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an odd integer between 1 and 19:";
    cin >> n;

    while (n < 1 || n > 19 || (n % 2) != 1) {
        cout << "Illegal. Try again: ";
        cin >> n;
    }

    int mid = n / 2;

    for (int r = mid; r >= 0; r--) {
        char out = 'A' + 2 * r;
        for (int c = 0; c < n; c++)
            if (((c >= mid - r) && (c <= mid + r))
                cout << out;
            out--;
    }
    cout << endl;
  
}
Problem 287  Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    int x = 0, y = 1, z = 2;
    double b[3] = {1.9, 2.3, 3.0};
    int d[2][2] = {{1,2},{3,4}};

    cout << twoD(b[0], y) << endl; // (a) prints difference: 0.9
    y = addUp(x, d[1][1]); // (b) sets y to sum 0 + 4
    cout << lastElt(d, 2, 2); // (c) prints last element: 4
    b[0] = average(b, 3); // (d) sets as average
    setZero(b[2], d[0][0]); // (e) sets both to 0
    return 0;
}
```

(a) Title line for `twoD`.
Answer:

```cpp
double twoD(double a, int b)
```

(b) Title line for `addUp`.
Answer:

```cpp
int addUp(int x, int y)
```

(c) Title line for `lastElt`.
Answer:

```cpp
int lastElt(int d[][2], int r, int c)
```

(d) Title line for `average`.
Answer:

```cpp
double average(double b[], int cap)
```

(e) Title line for `setZero`.
Answer:

```cpp
void setZero(double &x, int &y)
```

Problem 288  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string fun(int x) {
    string ans = "9876543210";
    if (x <= 0) return "5";
    if ((x >= 30) && (x < 1000)) return ans.substr(x % 10);
    if ((x >= 0) || (x < 100)) return "1+x";
    return ans + ans;
}

int up(int &x) {
    x++;
}
```
cout << x << endl;
return x - 2;
}

int main() {
    int x = 2;
cout << fun(0) << endl;    // line (a)
cout << fun(33) << endl;   // line (b)
cout << fun(3003) << endl; // line (c)
up(x);                      // line (d)
cout << up(x) << endl;     // line (e)
}

(a) What is the output at line (a)?
Answer:
5

(b) What is the output at line (b)?
Answer:
6543210

(c) What is the output at line (c)?
Answer:
1+x

(d) What is the output at line (d)?
Answer:
3

(e) What is the output at line (e)?
Answer:
4
2

Problem 289  Write a function called $colProd$ that calculates and returns the product of the entries of a specified
column in a 2-dimensional array.

For example, a program that uses the function $colProd$ follows.

int main() {
    int x[2][3] = {{3, 2, 4}, {1, 5, 9}};
cout << colProd (x, 2, 3, 1) << endl;
    // from the 2-d array x that has size 2 x 3, find the product of column 1
    // output will be 10 since col #1 contains 2 and 5.
    return 0;
}

Answer:

int colProd(int x[][3], int r, int c, int col) {
    int ans = 1;
    for (int i = 0; i < r; i++) ans *= x[i][col];
    return ans;
}
Problem 290  Write a function called \textit{numBig} that returns the number of digits in a positive integer parameter that are greater than or equal to 7.

For example, a program that uses the function \textit{numBig} follows.

```c++
int main() {
    cout << numBig(777) << endl; // prints 3
    cout << numBig(747) << endl; // prints 2
    cout << numBig(41) << endl;  // prints 0
    return 0;
}
```

Answer:

```c++
int numBig(int x) {
    if (x <= 0) return 0;
    if (x % 10 >= 7) return numBig(x / 10) + 1;
    return numBig(x / 10);
}
```

Problem 291  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an odd integer \( n \) that is between 1 and 23.
2. It repeatedly reads \( n \) from the user until the supplied value of \( n \) is legal.
3. It prints out a triangular picture (as shown in the diagram, but with \( n \) characters in the last row). Reading from the right, along each row the characters to be used is the sequence of uppercase letters \( A, B, C, \ldots \), and so on.

Here is an example of how the program should work:

Give me an odd integer between 1 and 23: 7

A
B
C
D
E
F

Answer:

```c++
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an odd integer between 1 and 23:";
    cin >> n;

    while (n < 1 || n > 23 || (n % 2) != 1) {
        cout << "Illegal. Try again: ";
        cin >> n;
    }

    int mid = n / 2;

    for (int r = 0; r <= mid; r++) {
        char out = 'A' + 2 * r;
        for (int c = 0; c < n; c++)
            if ((c >= mid - r) && (c <= mid + r)) {
                cout << out;
                out--;
            }
    }
```
Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    int x = 0, y = 1, z = 2;
    double b[3] = {1.9, 2.3, 3.0};
    int d[2][2] = {{1,2},{3,4}};

    x = diffTwo(b[0], y); // (a) sets x to approx difference 1
    swap(x, d[1][1]); // (b) swaps x with value of d[1][1]
    cout << biggest(d, 2, 2); // (c) prints biggest row: 3 4
    printTwo(b); // (d) prints two entries: 1.9 2.3
    cout << summit(b[2], d[0][0]) << endl; // (e) prints the sum 4
    return 0;
}
```

(a) Title line for `diffTwo`.
Answer:

```cpp
int diffTwo(double z, int y)
```

(b) Title line for `swap`.
Answer:

```cpp
void swap(int &x, int &y)
```

(c) Title line for `biggest`.
Answer:

```cpp
string biggest(int d[][2], int r, int c)
```

(d) Title line for `printTwo`.
Answer:

```cpp
void printTwo(double b[])
```

(e) Title line for `summit`.
Answer:

```cpp
double summit(double x, int y)
```

Problem 293 Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string fun(int x) {
    string ans = "0123456789";
    if (x <= 0) return "4";
    if ((x >= 30) && (x < 1000)) return ans.substr(x % 7);
```
if (((x >= 0) || (x < 100)) return "x11";
    return ans;
}

int up(int &x) {
    x--;
    cout << x << endl;
    return x - 1;
}

int main() {
    int x = 5;
    cout << fun(0) << endl;  // line (a)
    cout << fun(33) << endl; // line (b)
    cout << fun(3003) << endl; // line (c)
    up(x); // line (d)
    cout << up(x) << endl; // line (e)
}

(a) What is the output at line (a)?
Answer:
4

(b) What is the output at line (b)?
Answer:
56789

(c) What is the output at line (c)?
Answer:
x11

(d) What is the output at line (d)?
Answer:
4

(e) What is the output at line (e)?
Answer:
3
  2

Problem 294 The following C++ program has errors at the lines marked a,b,c,d, and e. For each answer write a single line of C++ that fixes the errors in the corresponding line.

```cpp
#include <iostream>
#include <fstream>
using namespace std;

void main(double x, string s[]) {  // line a
    ofstream f;
    f.open("outputFile");
    if (f == 0) return f;  // line b
```
while (1 == 1) { // line c
    x -= 1; // line d
    if (x < 0) return 0;
    cout << s[x] << endl; // line e
}
return 0;
}

(a) Correct line (a):
Answer:

int main(int x, char *y[]) { // line a

(b) Correct line (b):
Answer:

    if (f == 0) return 0; // line b

(c) Correct line (c):
Answer:

    while (1 == 1) { // line c

(d) Correct line (d):
Answer:

    x -= 1; // line d

(e) Correct line (e):
Answer:

    cout << y[x] << endl; // line e

Problem 295 Write a function called rowSum that calculates and returns the sum of the entries of a specified row of a 2-dimensional array.

For example, a program that uses the function rowSum follows.

int main() {
    int x[2][3] = {{3, 1, 4}, {1, 5, 9}};
    cout << rowSum(x, 2, 3, 1) << endl;
    // from the 2-d array x that has size 2 x 3, find the sum of row 1
    // output will be 15 since row #1 contains 1, 5 and 9.
    return 0;
}

Answer:

int rowSum(int x[][3], int r, int c, int row) {
    int ans = 0;
    for (int j = 0; j < c; j++) ans += x[row][j];
    return ans;
}
Problem 296  Write a function called `numEven` that returns the number of digits in a positive integer parameter that are even.

For example, a program that uses the function `numEven` follows.

```cpp
int main() {
    cout << numEven(444) << endl;       // prints 3
    cout << numEven(414) << endl;       // prints 2
    cout << numEven(91) << endl;        // prints 0
    return 0;
}
```

Answer:

```cpp
int numEven(int x) {
    if (x <= 0) return 0;
    if (x % 2 == 0) return numEven(x / 10) + 1;
    return numEven(x / 10);
}
```

Problem 297  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter an odd integer \( n \) that is between 1 and 25.
2. It repeatedly reads \( n \) from the user until the supplied value of \( n \) is legal.
3. It prints out a triangular picture (as shown in the diagram, but with \( n \) characters in the first row). Along each row the characters to be used is the sequence of uppercase letters A, B, C, ..., and so on.

Here is an example of how the program should work:

Give me an odd integer between 1 and 25: 7
```
ABCDEFG
ABCDEF
ABCDEF
ABCDEF
```

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an odd integer between 1 and 25:";
    cin >> n;
    while (n < 1 || n > 25 || (n % 2) != 1) {
        cout << "Illegal. Try again: ";
        cin >> n;
    }
    int mid = n / 2;
    for (int r = mid; r >= 0; r--) {
        char out = 'A';
        for (int c = 0; c < n; c++)
            if ((c >= mid - r) && (c <= mid + r))
                cout << out;
        out++;
    }
```
Problem 298  Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    int x = 0, y = 1, z = 2;
    double b[5] = {1.9, 2.3, 3.0};
    int d[2][2] = {{1,2},{3,4}};
    
    x = subtract(z, y);  // (a) sets x to difference 1
    reset(x, d[1][1]);    // (b) replaces x by value of d[1][1]
    bigRow(d, 2, 2);      // (c) prints biggest row: 3 4
    cout << printAll(b, 3) << endl;  // (d) prints array: 1.9 2.3 3.0
    cout << add(b[2], d[0][0]) << endl; // (e) prints the sum 4
    return 0;
}
```

(a) Title line for `subtract`.
Answer:

```cpp
int subtract(int z, int y)
```

(b) Title line for `reset`.
Answer:

```cpp
void reset(int &x, int y)
```

(c) Title line for `bigRow`.
Answer:

```cpp
void bigRow(int d[][2], int r, int c)
```

(d) Title line for `printAll`.
Answer:

```cpp
string printAll(double b[], int cap)
```

(e) Title line for `add`.
Answer:

```cpp
double add(double x, int y)
```

Problem 299  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string fun(int x) {
    string ans = "0123456789";
    if (x <= 0) return "0";
    if ((x >= 30) && (x < 1000)) return ans.substr(x % 10);
```
if ((x >= 0) || (x < 100)) return "x+1";
    return ans + ans;
}

int up(int &x) {
    x++;
    cout << x << endl;
    return x;
}

int main() {
    x = 4;
    cout << fun(0) << endl; // line (a)
    cout << fun(33) << endl; // line (b)
    cout << fun(3003) << endl; // line (c)
    up(x); // line (d)
    cout << up(x) << endl; // line (e)
}

(a) What is the output at line (a)?
Answer:
0

(b) What is the output at line (b)?
Answer:
3456789

(c) What is the output at line (c)?
Answer:
x+1

(d) What is the output at line (d)?
Answer:
5

(e) What is the output at line (e)?
Answer:
6

6

Problem 300 The following C++ program has errors at the lines marked a,b,c,d, and e. For each answer write a single line of C++ that fixes the errors in the corresponding line.

#include <iostream>
#include <fstream>
using namespace std;

int main(int x, string y[]) { // line a
    while (0 < x < 5) { // line b
        cout >> y[x - 1] >> end; // line c
    }
x = -1; // line d

} // line a

ifstream f;
f.open("inputFile");
if (f == 0) return -1; // line e

return 0;
} // line e

(a) Correct line (a):
Answer:

int main(int x, char *y[]) { // line a

(b) Correct line (b):
Answer:

while (0 < x && x < 5) { // line b

(c) Correct line (c):
Answer:

cout << y[x - 1] << endl; // line c

(d) Correct line (d):
Answer:

x -= 1; // line d

(e) Correct line (e):
Answer:

if (f == 0) return -1; // line e

Problem 301 Write a function called colSum that calculates and returns the sum of the entries of a specified column in a 2-dimensional array.

For example, a program that uses the function colSum follows.

int main() {
    int x[2][3] = {{3, 1, 4}, {1, 5, 9}};
    cout << colSum(x, 2, 3, 1) << endl;
    // from the 2-d array x that has size 2 x 3, find the sum of column 1
    // output will be 6 since col #1 contains 1 and 5.
    return 0;
}

Answer:

int colSum(int x[][3], int r, int c, int col) {
    int ans = 0;
    for (int i = 0; i < r; i++) ans += x[i][col];
    return ans;
}
**Problem 302** Write a function called `num4` that returns the number of digits in a positive integer parameter that are equal to 4.

For example, a program that uses the function `num4` follows.

```cpp
int main() {
    cout << num4(444) << endl; // prints 3
    cout << num4(414) << endl; // prints 2
    cout << num4(81) << endl;  // prints 0
    return 0;
}
```

**Answer:**

```cpp
int num4(int x) {
    if (x <= 0) return 0;
    if (x % 10 == 4) return num4(x / 10) + 1;
    return num4(x / 10);
}
```

**Problem 303** Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an odd integer \( n \) that is between 1 and 21.
2. It repeatedly reads \( n \) from the user until the supplied value of \( n \) is legal.
3. It prints out a triangular picture (as shown in the diagram, but with \( n \) characters in the last row). Along each row the characters to be used is the sequence of uppercase letters \( A, B, C, \ldots \), and so on.

Here is an example of how the program should work:

```
Give me an odd integer between 1 and 21: 7
   A
  ABC
 ABCDE
 ABCDEFG
```

**Answer:**

```cpp
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an odd integer between 1 and 21:";
    cin >> n;
    while (n < 1 || n > 21 || (n % 2) != 1) {
        cout << "Illegal. Try again: ";
        cin >> n;
    }

    int mid = n / 2;

    for (int r = 0; r <= mid; r++) {
        char out = 'A';
        for (int c = 0; c < n; c++)
            if ((c >= mid - r) && (c <= mid + r)) {
                cout << out;
                out++;
            }
    }

    return 0;
}
```
### Problem 304
Write **title lines** for the functions that are called by the following main program. **Do not supply** the blocks for the functions.

```cpp
int main() {
    double b[5] = {1.9, 2.3, 3.0, 4.4, 5.7};
    double d = 3.1415926;
    int x = 2;
    cout << decimalPart(b[1]) << endl; // (a) prints 0.3
    medianPosition(b, 5); // (b) prints 2, the index of the median
    swap1(d, b[1]); // (c) swaps b[1] with d
    swap2(b, 3, x); // (d) swaps entry b[3] with b[x]
    cout << sqrt(d) << endl; // (e) prints the square root of d
    return 0;
}
```

(a) Title line for `decimalPart` as called at the line marked (a).

**Answer:**

```cpp
double decimalPart(double x)
```

(b) Title line for `medianPosition` as called at the line marked (b).

**Answer:**

```cpp
void medianPosition(double x[], int cap)
```

(c) Title line for `swap1` as called at the line marked (c).

**Answer:**

```cpp
void swap1(double &x, double &y)
```

(d) Title line for `swap2` as called at the line marked (d).

**Answer:**

```cpp
void swap2(double x[], int y, int z)
```

(e) Title line for `sqrt` as called at the line marked (e).

**Answer:**

```cpp
double sqrt(double x)
```

### Problem 305
Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string fun(int x) {
    if (x <= 0) return " ";
    if (x >= 9 && x % 2 == 1) return "x+1";
    if (x >= 9 || x % 3 == 0) return "x+2";
    return "5";
}
```
int rec(int x) {
    if (x < 100) return x/5;
    return rec(x / 10) + rec(x % 100);
}

int main() {
    cout << fun(-3) << endl; // line (a)
    cout << fun(33) << endl; // line (b)
    cout << rec(36) << endl; // line (c)
    cout << rec(-555) << endl; // line (d)
    cout << rec(987) << endl; // line (e)
}

(a) What is the output at line (a)?
Answer:

(b) What is the output at line (b)?
Answer:
x+1

(c) What is the output at line (c)?
Answer:
7

(d) What is the output at line (d)?
Answer:
-111

(e) What is the output at line (e)?
Answer:
36

Problem 306  Write a function called dropEvens that forms a new number from a positive integer parameter by dropping all even digits. In case all digits are even or a negative parameter is given an answer of 0 is to be returned.

For example, a program that uses the function dropEvens follows.

int main() {
    cout << dropEvens(1245); // prints 15
    cout << dropEvens(19683); // prints 193
    cout << dropEvens(0);    // prints 0
    cout << dropEvens(-10);  // prints 0
    return 0;
}

Answer:

int dropEvens(int x) {
    if (x <= 0) return 0;
    if (x % 2 == 0) return dropEvens(x/10);
    return 10 * dropEvens(x/10) + x % 10;
}
**Problem 307**  Write a function called `randChange` that selects one entry at random in an array of integers and changes it to a random negative integer that lies between $-99$ and $-1$ inclusive. (You must use an appropriate standard C++ function to generate all random numbers.)

For example, a program that uses the function `randChange` follows.

```cpp
int main() {
    int x[6] = {3, 1, 4, 1, 5, 9};
    randChange(x, 6);
    for (int i = 0; i <= 5; i++)
        cout << x[i] << " ";  // might print 3 1 -17 1 5 9
    cout << endl;
    return 0;
}
```

Answer:

```cpp
void randChange(int x[], int cap) {
    int r = rand() % cap;
    x[r] = -(1 + rand() % 99);
}
```

**Problem 308**  Suppose that a C++ program called `prog.cpp` is compiled and correctly executed on venus with the instructions:

```
venus> g++ prog.cpp
venus> a.out file1 file2 file3
```

For each of the following short segments of the program `prog.cpp` write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)

```cpp
char a = 'b';
cout << a << endl;
```

Answer:

`b`

(ii)

```cpp
char a = 'b';
while (a <= 'f') {
    cout << a - 'a';
    a = a + 1;
}
```

Answer:

`12345`

(iii)

```cpp
int main(int argc, char *argv[]) {
    cout << argv[1];
}
```

Answer:

`file1`
Problem 309 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer \( n \) that is between 1 and 20.
2. It repeatedly reads \( n \) from the user until the supplied value of \( n \) is legal.
3. It prints out a square picture (as shown in the diagram, but with \( n \) rows) that uses the uppercase letters \( A, B, C, \ldots \) in sequence, to form an outer stepeter of As that contains a stepeter of Bs, that contains a permimeter of Cs, and so on.

Here is an example of how the program should work:

Give me an integer between 1 and 20: 7
AAAAAAA
ABBBBBBA
ABCCCCBA
ABCDCCBA
ABCCCCBA
ABBBBBBA
AAAAAAA

Answer:

```c++
#include <iostream>
using namespace std;

int main() {
    char picture[20][20];

    int n = 0;
    while (n < 1 || n > 20) {
        cout << "Give me an integer between 1 and 20: ";
        cin >> n;
    }
    int mid = (n + 1) / 2;

    for (int step = 0; step < mid; step++) {
        char x = 'A' + step;
        for (int r = step; r < n -step; r++)
            for (int c = step; c < n -step; c++)
                picture[r][c] = x;
    }
    return 0;
}
```
Problem 310 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    bool b[5] = {true, true, false, true, true};
    int x = 2;
    cout << isTrue(b[1 + 2]) << endl; // (a) prints true
    allTrue(b, 5); // (b) prints False
    swap1(b, 3, x); // (d) swaps entry b[3] with b[x]
    swap2(b[x], b[x+1]); // (d) swaps entries
    cout << sqrt(x) << endl; // (e) prints the square root of x
    return 0;
}
```

(a) Title line for `isTrue` as called at the line marked (a).
Answer:

```cpp
bool isTrue(bool x)
```

(b) Title line for `allTrue` as called at the line marked (b).
Answer:

```cpp
void allTrue(bool x[], int cap)
```

(c) Title line for `swap1` as called at the line marked (c).
Answer:

```cpp
void swap1(bool x[], int y, int z)
```

(d) Title line for `swap2` as called at the line marked (d).
Answer:

```cpp
void swap2(bool &x, bool &y)
```

(e) Title line for `sqrt` as called at the line marked (e).
Answer:

```cpp
double sqrt(int x)
```

Problem 311 Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

double fun(int x) {
    if (x <= 0) return sqrt((double) (-x));
    if (x >= 9 && x % 2 == 1) return x+1.0;
    if (x >= 9 || x % 3 == 0) return x+2.0;
}


```cpp
int rec(int x) {
    if (x < 100) return x/3;
    return rec(x / 10) + rec(x % 100);
}

int main() {
    cout << fun(-3) << endl; // line (a)
    cout << fun(33) << endl; // line (b)
    cout << rec(36) << endl; // line (c)
    cout << rec(-555) << endl; // line (d)
    cout << rec(987) << endl; // line (e)
}

(a) What is the output at line (a)?
Answer:
1.73205

(b) What is the output at line (b)?
Answer:
34

(c) What is the output at line (c)?
Answer:
12

(d) What is the output at line (d)?
Answer:
-185

(e) What is the output at line (e)?
Answer:
61

Problem 312  Write a function called `onlyEvens` that forms a new number from a positive integer parameter by dropping all odd digits. In case all digits are odd or a negative parameter is given an answer of 0 is to be returned.

For example, a program that uses the function `onlyEvens` follows.

```cpp
int main() {
    cout << onlyEvens(1245); // prints 24
    cout << onlyEvens(19683); // prints 68
    cout << onlyEvens(0);    // prints 0
    cout << onlyEvens(-10);  // prints 0
    return 0;
}
```

Answer:

```cpp
int onlyEvens(int x) {
    if (x <= 0) return 0;
    if (x % 2 != 0) return onlyEvens(x/10);
    return 10*onlyEvens(x/10) + x % 10;
}
```
Problem 313   Write a function called randChange that selects one entry at random in a 2-dimensional array of integers and changes it to -17. (You must use an appropriate standard C++ function to generate all random numbers.)

For example, a program that uses the function randChange follows.

```cpp
int main() {
    int x[2][3] = {{3, 1, 4}, {1, 5, 9}};
    randChange(x, 2, 3);
    for (int i = 0; i <= 1; i++)
        for (int j = 0; j <= 2; j++)
            cout << x[i][j] << " ";       // might print  3 1 -17 1 5 9
    cout << endl;
    return 0;
}
```

Answer:

```cpp
void randChange(int x[][3], int rows, int cols) {
    int r = rand()%rows;
    int c = rand()%cols;
    x[r][c] = -17;
}
```

Problem 314   Suppose that a C++ program called prog.cpp is compiled and correctly executed on venus with the instructions:

venus> g++ prog.cpp
venus> a.out file1 file2 file3

For each of the following short segments of the program prog.cpp write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)

```cpp
char a = 'a';
cout << a << endl;
```

Answer:

a

(ii)

```cpp
char a = 'a';
while (a <= 'f') {
    cout << 'a' - a;
    a = a + 1;
}
```

Answer:

0-1-2-3-4-5

(iii)

```cpp
int main(int argc, char *argv[]) {
    cout << argc;
}
```

Answer:
(iv)
```
string x = "Easy Question"
    cout << x.substr(6, 0);
```

Answer:
```
8
```

(v)
```
string x = "Easy Question"
    cout << x.rfind("s");
```

Answer:
```
8
```

**Problem 315**  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer \( n \) that is between 1 and 20.
2. It repeatedly reads \( n \) from the user until the supplied value of \( n \) is legal.
3. It prints out a square picture (as shown in the diagram, but with \( n \) rows) that uses the uppercase letters O and X in sequence, to form an outer perimeter of Os that contains a perimeter of Xs, that contains a perimeter of Os, and so on.

Here is an example of how the program should work:

```
Give me an integer between 1 and 20: 7
OOOOOOO
OXXXXXO
OXOOOXO
OXOXOXO
OXOOOXO
OXXXXXO
OOOOOOO
```

Answer:
```
#include <iostream>
using namespace std;

int main() {
    char picture[20][20];

    int n = 0;
    while (n < 1 || n > 20) {
        cout << "Give me an integer between 1 and 20: ";
        cin >> n;
    }
    int mid = (n + 1) / 2;

    for (int perim = 0; perim < mid; perim++) {
        char x = 'O';
        if (perim % 2 == 1) x = 'X';
        for (int r = perim; r < n -perim; r++)
            for (int c = perim; c < n -perim; c++)
            {
            }
    }
    return 0;
}
```
Problem 316 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    string b[5] = {"1.9", "2.3", "3.0", "4.4", "5.7"};
    double d = 3.1415926;
    int x = 2;
    cout << decimalPart(b[1]) << endl; // (a) prints 0.3
    medianPosition(b, 5); // (b) prints 2, the index of the median
    swap1(d, b[1]); // (c) changes b[1] and d
    swap2(b, 3, x); // (d) swaps entry b[3] with b[x]
    cout << sqrt(d) << endl; // (e) prints the square root of d
    return 0;
}
```

(a) Title line for `decimalPart` as called at the line marked (a).

Answer:

```cpp
double decimalPart(string s)
```

(b) Title line for `medianPosition` as called at the line marked (b).

Answer:

```cpp
void medianPosition(string x[], int cap)
```

(c) Title line for `swap1` as called at the line marked (c).

Answer:

```cpp
void swap1(double &d, string &s)
```

(d) Title line for `swap2` as called at the line marked (d).

Answer:

```cpp
void swap2(string x[], int i, int j)
```

(e) Title line for `sqrt` as called at the line marked (e).

Answer:

```cpp
double sqrt(double d)
```

Problem 317 Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;
```
string fun(char x) {
    if (x <= 'k') return "";
    if (x >= 'l' && x <= 't') return "x++";
    if (x >= 'p') return "x-1";
    return "20";
}

int rec(int x) {
    if (x < 1000) return x/5;
    return rec(x / 10) + rec(x % 100);
}

int main() {
    cout << fun('m') << endl; // line (a)
    cout << fun('p') << endl; // line (b)
    cout << rec(666) << endl; // line (c)
    cout << rec(-555) << endl; // line (d)
    cout << rec(2013) << endl; // line (e)
}

(a) What is the output at line (a)?
Answer:

x++

(b) What is the output at line (b)?
Answer:

x++

(c) What is the output at line (c)?
Answer:

133

(d) What is the output at line (d)?
Answer:

-111

(e) What is the output at line (e)?
Answer:

42

Problem 318 Write a function called upEvens that forms a new number from a non-negative integer parameter by increasing all even digits. In case a negative parameter is given an answer of 0 is to be returned.

For example, a program that uses the function upEvens follows.

int main() {
    cout << upEvens(1245); // prints 1355
    cout << upEvens(19683); // prints 19793
    cout << upEvens(0);    // prints 1
    cout << upEvens(-10);  // prints 0
    return 0;
}

Answer:
int upEvens(int x) {
    if (x < 0) return 0;
    if (x < 10)
        if (x % 2 == 0) return x + 1;
        else return x;
    return 10*upEvens(x/10) + upEvens(x%10);
}

Problem 319    Write a function called randSelect that selects one row at random in a 2-dimensional array of integers and returns the sum of the entries in that row. (You must use an appropriate standard C++ function to generate all random numbers.)

For example, a program that uses the function randSelect follows.

int main() {
    int x[2][3] = {{3, 1, 4}, {1, 5, 9}};
    cout << randSelect(x, 2, 3); // might print 8 if the first row is selected
    cout << endl;
    return 0;
}

Answer:

int randSelect(int x[][3], int rows, int cols) {
    int r = rand() % rows;
    int ans = 0;
    for (int c = 0; c < cols; c++)
        ans += x[r][c];
    return ans;
}

Problem 320    Suppose that a C++ program called prog.cpp is compiled and correctly executed on venus with the instructions:

venus> g++ prog.cpp
venus> a.out file1 file2 file3

For each of the following short segments of the program prog.cpp write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)

    char a = 'a';
    cout << (char) (a + 2) << endl;

Answer:

c

(ii)

    char a = 'b';
    while ((a - 'a') <= 5) {
        cout << a;
        a = a + 1;
    }

Answer:
Problem 321  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter an integer \( n \) that is between 1 and 20.
2. It exits if the user enters an illegal value for \( n \).
3. It prints out a triangular picture (as shown in the diagram, but with \( n \) rows) that uses the uppercase letters A, B, C, ... in sequence, to form the diagonal sides of the triangle. The vertical straight side should be at the right.

Here is an example of how the program should work:

Give me an integer between 1 and 20: 7

A
AB
ABC
ABCD
ABCDE
ABCDEF
ABCDEFG

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int n = 0;
    cout << "Give me an integer between 1 and 20: ";
    cin >> n;
    if (n < 1 || n > 20) return 0;

    for (int r = n; r >= 1; r--) {
```
Problem 322  Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    char b[5] = {'t', 't', 'f', 't', 't'};
    int x = 2;
    cout << isT(b[1 + 2]) << endl; // (a) prints true
    allTrue(b, 5); // (b) prints false
    swap1(b, 3, x); // (d) swaps entry b[3] with b[x]
    swap2(b[x], b[x+1]); // (d) swaps entries
    cout << sqrt(x) << endl; // (e) prints the square root of x
    return 0;
}
```

(a) Title line for `isT` as called at the line marked (a).
Answer:

```cpp
bool isT(char x)
```

(b) Title line for `allTrue` as called at the line marked (b).
Answer:

```cpp
void allTrue(char b[], int cap)
```

(c) Title line for `swap1` as called at the line marked (c).
Answer:

```cpp
void swap1(char b[], int i, int j)
```

(d) Title line for `swap2` as called at the line marked (d).
Answer:

```cpp
void swap2(char &x, char &y)
```

(e) Title line for `sqrt` as called at the line marked (e).
Answer:

```cpp
double sqrt(int x)
```

Problem 323  Consider the following C++ program.
```cpp
#include <iostream>
using namespace std;

double fun(double x) {
    if (x <= 0.0) return sqrt(-x);
    if (x >= 9.0 && x <= 100.0) return x+1.0;
    if (x >= 90.0 || x >= 5.0) return x+2.0;
    return 3.0;
}

int rec(int x) {
    if (x < 100) return x/6;
    return rec(x / 10) + rec(x % 100);
}

int main() {
    cout << fun(-4.0) << endl; // line (a)
    cout << fun(99.0) << endl; // line (b)
    cout << fun(2.0) << endl; // line (c)
    cout << rec(-666) << endl; // line (d)
    cout << rec(987) << endl; // line (e)
}
```

(a) What is the output at line (a)?
Answer:
2

(b) What is the output at line (b)?
Answer:
100

(c) What is the output at line (c)?
Answer:
3

(d) What is the output at line (d)?
Answer:
-111

(e) What is the output at line (e)?
Answer:
30

Problem 324 Write a function called downOdds that forms a new number from a non-negative integer parameter by decreasing all odd digits. In case a negative parameter is given an answer of 0 is to be returned.

For example, a program that uses the function downOdds follows.

```cpp
int main() {
    cout << downOdds(3245); // prints 2244
    cout << downOdds(19683); // prints 8682
    cout << downOdds(1); // prints 0
    cout << downOdds(-10); // prints 0
    return 0;
}
```
int downOdds(int x) {
    if (x <= 0) return 0;
    if (x < 10)
        if (x % 2 == 1) return x - 1;
        else return x;
    return 10 * downOdds(x / 10) + downOdds(x % 10);
}

Problem 325 Write a function called randSelect that selects one column at random in a 2-dimensional array of integers and returns the product of the entries in that row. (You must use an appropriate standard C++ function to generate all random numbers.)

For example, a program that uses the function randSelect follows.

int main() {
    int x[2][3] = {{3, 1, 4}, {1, 5, 9}};
    cout << randSelect(x, 2, 3); // might print 36 if the last col is selected
    cout << endl;
    return 0;
}

Answer:

int randSelect(int x[][3], int rows, int cols) {
    int c = rand() % cols;
    int ans = 1;
    for (int r = 0; r < rows; r++)
        ans *= x[r][c];
    return ans;
}

Problem 326 Suppose that a C++ program called prog.cpp is compiled and correctly executed on venus with the instructions:

venus> g++ prog.cpp
venus> a.out file1 file2 file3

For each of the following short segments of the program prog.cpp write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)

char c = 'a';
cout << (char) (c + 3) << endl;

Answer:

d

(ii)

char a = 'a';
while (((a - 'a') <= 3) {
    cout << 'a';
    a = a - 1;
}
Problem 327  Write a complete C++ program that does the following. (Programs that correctly carry out some
of the tasks will receive partial credit.)
1. It asks the user to enter an integer $n$ that is between 1 and 25.
2. It exits if the user enters an illegal value for $n$.
3. It prints out a downward pointing triangular picture (as shown in the diagram, but with $n$ rows) that uses the
lowercase letters $a$, $b$, $c$, ... in sequence, to form the diagonal sides of the triangle.
Here is an example of how the program should work:

Give me an integer between 1 and 25: 7
abcdefg
abcdef
abcde
abcd
abc
ab
a

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int n = 0;
    cout << "Give me an integer between 1 and 25: ";
    cin >> n;
    if (n < 1 || n > 20) return 0;
```
for (int r = n; r >= 1; r--) {
    for (int c = 1; c <= n; c++) {
        if (c < r) cout << " ";
        else cout << (char) ('a' + c - r);
    }
    cout << endl;
}
cout << endl;
return 0;
}

Problem 328 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

int main() {
    int b[5] = {9, 3, 0, 4, 7};
    int x = 17;
    cout << decimalPart(3.14159) << endl; // (a) prints 0.14159
    median(b, 5); // (b) prints 4, the median entry
    swap1(x, b[1]); // (c) swaps b[1] with x
    swap2(b, 3, 4); // (d) swaps entry b[3] with b[4]
    cout << sqrt(5, 10, 12) << endl; // (e) prints "Hello" for any input values
    return 0;
}

(a) Title line for decimalPart as called at the line marked (a).
Answer:

double decimalPart(double x)

(b) Title line for median as called at the line marked (b).
Answer:

void median(int a[], int cap)

(c) Title line for swap1 as called at the line marked (c).
Answer:

void swap1(int &x, int &y)

(d) Title line for swap2 as called at the line marked (d).
Answer:

void swap2(int x[], int a, int b)

(e) Title line for sqrt as called at the line marked (e).
Answer:

string sqrt(int a, int b, int c)

Problem 329 Consider the following C++ program.

#include <iostream>
using namespace std;

int fun(int x) {
if (x <= 0) return 10;
if (x >= 9 && x % 2 == 1) return x + 1;
if (x >= 9 || x % 3 == 0) return x + 2;
return 5;
}

int rec(int x) {
    if (x < 100) return x/10;
    return rec(x / 10) + rec(x % 100);
}

int main() {
    cout << fun(-3) << endl;  // line (a)
    cout << fun(33) << endl;  // line (b)
    cout << rec(36) << endl;  // line (c)
    cout << rec(-666) << endl;  // line (d)
    cout << rec(987) << endl;  // line (e)
}

(a) What is the output at line (a)?
Answer:
10

(b) What is the output at line (b)?
Answer:
34

(c) What is the output at line (c)?
Answer:
3

(d) What is the output at line (d)?
Answer:
-66

(e) What is the output at line (e)?
Answer:
17

Problem 330 Write a function called multiDigit that prints a new number formed from a positive integer parameter by printing each odd digit once and each even digit twice. If a negative parameter is given, it should print the word Idiot and if 0 is entered it should do nothing.

For example, a program that uses the function multiDigit follows.

int main() {
    multiDigit(1245); cout << endl;  // prints 122445
    multiDigit(19683); cout << endl;  // prints 1966883
    multiDigit(0); cout << endl;  // prints
    multiDigit(-10); cout << endl;  // prints Idiot
    return 0;
}

Answer:
void multiDigit(int n) {
    if (n < 0) cout << "Idiot";
    else if (n == 0) return;
    else {
        multiDigit(n / 10);
        if (n % 2 == 0) cout << n % 10;
        cout << n % 10;
    }
}

Problem 331   Write a function called randFill that fills the entries of an array with random negative integers that lie between \(-99\) and \(-1\) inclusive. (Use an appropriate C++ function to generate the random numbers.)

For example, a program that uses the function follows.

```cpp
int main() {
    int x[4];
    randFill(x, 4);
    for (int i = 0; i <= 3; i++)
        cout << x[i] << endl;  // prints 4 random negative numbers
    return 0;
}
```

Answer:

```cpp
void randFill(int a[], int c) {
    for (int i = 0; i < c; i++)
        a[i] = rand() % 99 - 99;
}
```

Problem 332   Suppose that a C++ program called prog.cpp is compiled and correctly executed on venus with the instructions:

```bash
venus> g++ prog.cpp  
venus> a.out input1.txt input2 out.txt
```

For each of the following short segments of the program prog.cpp write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)
```
int x = 4, y = 10;
cout << (x/y + 1.0) << endl;
```

Answer:

1.0

(ii)
```
char x = 'a';
while (x <= 'f') {
    cout << (char) (x + 1);
    x = x + 1;
}
```

Answer:

bcdefg
cout << 'a' - 'd';

Answer:
-3

(iv)

string x = "Easy Question";
cout << x.substr(1,2);

Answer:
as

(v)

int main(int argc, char *argv[]) {
cout << argc;

Answer:
4

Problem 333  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)   
1. It asks the user to enter an integer \( n \) that is between 1 and 20.  
2. It repeatedly reads \( n \) from the user until the supplied value of \( n \) is legal.  
3. It prints out a triangular picture (as shown in the diagram, but with \( n \) rows) that uses the uppercase letters \( A, B, C, \ldots \) in sequence, and if necessary returns to the letter \( A \) after any \( Z \).  

Here is an example of how the program should work:

Give me an integer between 1 and 20: 6

A
BC
DEF
GHIJ
KLMNO
PQRSTU

Answer:

#include <iostream>
using namespace std;

int main() {
  int n;
cout << "Give me an integer between 1 and 20: ";
cin >> n;

  while (n < 1 || n > 20) {
    cout << "That is out of range. Give me an integer between 1 and 20: ";
cin >> n;
  }

  char x = 'A';
for (int i = 1; i <= n; i++) {
    for (int j = 1; j <= n; j++)
        if ((i + j) <= n) cout << " ";
    else {
        cout << x;
        x = x + 1;
        if (x > 'Z') x = 'A';
    }
    cout << endl;
}

Problem 334 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

int main() {
    int a[5] = {9, 3, 0, 4, 7};
    int x = 17;
    cout << reducedFraction(2, 6) << endl; // (a) prints 1/3
    swap1(a[1], a[2]);                   // (b) swaps a[1] with a[2]
    swap2(x, a, 3);                      // (c) swaps entry a[3] with x
    median(5, 4, 6);                     // (d) prints 5, the median entry
    cout << sqrt(5, 10, 12, 14) << endl; // (e) prints 25 for any input values
    return 0;
}

(a) Title line for reducedFraction as called at the line marked (a).
Answer:

string reducedFraction(int a, int b)

(b) Title line for swap1 as called at the line marked (b).
Answer:

void swap1(int &x, int &y)

(c) Title line for swap2 as called at the line marked (c).
Answer:

void swap2(int &x, int a[], int i)

(d) Title line for median as called at the line marked (d).
Answer:

void median(int a, int b, int c)

(e) Title line for sqrt as called at the line marked (e).
Answer:

int sqrt(int a, int b, int c, int d)

Problem 335 Consider the following C++ program.

#include <iostream>
using namespace std;
int fun(int x) {
    if (x <= 0) return 10;
    if (x >= 9 && x % 2 == 1) return x + 1;
    if (x >= 9 || x % 3 == 0) return x + 2;
    return 5;
}

int rec(int x) {
    if (x < 100) return x/10;
    return rec(x / 10) + rec(x % 10);  
}

int main() {
    cout << fun(-6) << endl; // line (a)
    cout << fun(63) << endl; // line (b)
    cout << rec(66) << endl; // line (c)
    cout << rec(-747) << endl; // line (d)
    cout << rec(876) << endl; // line (e)
}

(a) What is the output at line (a)?
Answer:
10

(b) What is the output at line (b)?
Answer:
64

(c) What is the output at line (c)?
Answer:
6

(d) What is the output at line (d)?
Answer:
-74

(e) What is the output at line (e)?
Answer:
15

Problem 336  Write a function called multiDigit that prints a new number formed from a positive integer parameter by printing each odd digit twice and each even digit once. If a negative parameter is given, it should print the word Negative and if 0 is entered it should do nothing.

For example, a program that uses the function multiDigit follows.

int main() {
    multiDigit(1245); cout << endl; // prints 112455
    multiDigit(19683); cout << endl; // prints 11996833
    multiDigit(0); cout << endl; // prints
    multiDigit(-10); cout << endl; // prints Negative
    return 0;
}
Answer:

```cpp
void multiDigit(int n) {
    if (n < 0) cout << "Negative";
    else if (n == 0) return;
    else {
        multiDigit(n / 10);
        if (n % 2 != 0) cout << n % 10;
        cout << n % 10;
    }
}
```

**Problem 337**  Write a function called `randFill` that fills the entries of an array with random integers between 1 and a specified maximum value. (Use an appropriate C++ function to generate the random numbers.)

For example, a program that uses the function follows.

```cpp
int main() {
    int x[4];
    int max = 999;
    randFill(x, 4, max);
    for (int i = 0; i <= 3; i++)
        cout << x[i] << endl;  // prints 4 random numbers between 1 and 999
    return 0;
}
```

Answer:

```cpp
void randFill(int a[], int c, int max) {
    for (int i = 0; i < c; i++)
        a[i] = rand() % max + 1;
}
```

**Problem 338**  Suppose that a C++ program called `prog.cpp` is compiled and correctly executed on venus with the instructions:

```
venus> g++ prog.cpp
venus> a.out input1.txt input2 out.txt
```

For each of the following short segments of the program `prog.cpp` write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)  
```cpp
int x = 8, y = 10;
cout << ((x + 1.0)/y) << endl;
```

Answer:

0.9

(ii)  
```cpp
char x = 'f';
while (x <= 'a') {
    cout << (char) (x + 1);
    x = x + 1;
}
```
Problem 339  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer \( n \) that is between 1 and 9.
2. It repeatedly reads \( n \) from the user until the supplied value of \( n \) is legal.
3. It prints out a triangular picture (as shown in the diagram, but with \( n \) rows) that uses the lowercase letters \( a, b, c, \ldots \) in sequence, and if necessary continues with uppercase letter starting at \( A \) after any \( z \).

Here is an example of how the program should work:

\[
\text{Give me an integer between 1 and 9: 7}
\]

\[
a
bc
def
ghij
klmno
pqrstu
vwxyzAB
\]

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 9: ";
    cin >> n;
    while (n < 1 || n > 9) {
```

cout << "That is out of range. Give me an integer between 1 and 9: ";
cin >> n;
}

char x = 'a';
for (int i = 1; i <= n; i++) {
    for (int j = 1; j <= i; j++) {
        cout << x;
        x = x + 1;
        if (x > 'z') x = 'A';
    }
    cout << endl;
}

Problem 340 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

int main() {
    int b[5] = {9, 3, 0, 4, 7};
    int x = 17;
    cout << integerPart(3.14159) << endl; // (a) prints 3
    swap1(x, b[1]); // (b) swaps b[1] with x
    swap2(b, 1, x); // (c) swaps b[1] with x
    median(x +1, x, x+2); // (d) prints 18 the median value
    cout << sqrt(5, 10, 12) << endl; // (e) prints "Error" for any input values
    return 0;
}

(a) Title line for integerPart as called at the line marked (a).
Answer:

int integerPart(double x)

(b) Title line for swap1 as called at the line marked (b).
Answer:

void swap1(int &a, int &b)

(c) Title line for swap2 as called at the line marked (c).
Answer:

void swap2(int a[], int i, int &b)

(d) Title line for median as called at the line marked (d).
Answer:

void median(int a, int b, int c)

(e) Title line for sqrt as called at the line marked (e).
Answer:

string sqrt(int a, int b, int c)

Problem 341 Consider the following C++ program.
#include <iostream>
using namespace std;

int fun(int x) {
    if (x <= 0) return 100;
    if (x >= 9 && x % 2 == 1) return x + 1;
    if (x >= 9 || x % 3 == 0) return x + 2;
    return 5;
}

int rec(int x) {
    if (x < 100) return x/10;
    return rec(x / 10) + rec(x % 100);
}

int main() {
    cout << fun(-144) << endl; // line (a)
    cout << fun(92) << endl; // line (b)
    cout << rec(92) << endl; // line (c)
    cout << rec(-144) << endl; // line (d)
    cout << rec(678) << endl; // line (e)
}

(a) What is the output at line (a)?
Answer:
100

(b) What is the output at line (b)?
Answer:
94

(c) What is the output at line (c)?
Answer:
9

(d) What is the output at line (d)?
Answer:
-14

(e) What is the output at line (e)?
Answer:
13

Problem 342 Write a function called multiDigit that prints a new number formed from a positive integer parameter by printing each odd digit twice and omitting all even digits. If a negative parameter is given, it should print the word Done and if 0 is entered it should do nothing.

For example, a program that uses the function multiDigit follows.

```cpp
int main() {
    multiDigit(1245); cout << endl; // prints 1155
    multiDigit(19683); cout << endl; // prints 119933
    multiDigit(220); cout << endl; // prints
    multiDigit(-10); cout << endl; // prints Done
    return 0;
}
```
void multiDigit(int n) {
    if (n < 0) cout << "Done";
    else if (n == 0) return;
    else {
        multiDigit(n / 10);
        if (n % 2 != 0) {
            cout << n % 10;
            cout << n % 10;
        }
    }
}

Problem 343  Write a function called randFill that fills the entries of an array with random two digit integers. (Use an appropriate C++ function to generate the random numbers.)

For example, a program that uses the function follows.

int main() {
    int x[4];
    randFill(x, 4);
    for (int i = 0; i <= 3; i++)
        cout << x[i] << endl;  // prints 4 random two digit numbers
    return 0;
}

Answer:

void randFill(int a[], int c) {
    for (int i = 0; i < c; i++)
        a[i] = rand() % 90 + 10;
}

Problem 344  Suppose that a C++ program called prog.cpp is compiled and correctly executed on venus with the instructions:

venus> g++ prog.cpp
venus> a.out input1.txt input2 out.txt

For each of the following short segments of the program prog.cpp write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)

    int x = 8, y = 10;
    cout << (x + 1.0/y) << endl;

Answer:

8.1

(ii)

    char x = 'f';
    while (x <= 'i') {
        cout << (char) (x - 1);
        x = x + 1;
    }
Problem 345  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer $n$ that is between 1 and 25.
2. It immediately stops if the supplied value of $n$ is not legal.
3. Otherwise it prints out a triangular picture (as shown in the diagram, but with $n$ rows) that uses the lowercase letters $a$, $b$, $c$, ... in sequence, and if necessary returns to the letter $a$ after any $z$.

Here is an example of how the program should work:

Give me an integer between 1 and 25:  6
abcdef
ghijk
lmno
pqr
st
u

Answer:

#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 25: ";
    cin >> n;

    while (n < 1 || n > 25) {
        cout << "That is out of range. Give me an integer between 1 and 25: ";
    
    int main(int argc, char *argv[]) {
        cout << argv[0];

    a.out
Problem 346 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    int a[5] = {9, 3, 0, 4, 7};
    int x = 17;
    cout << asFraction(2, 6) << endl; // (a) prints 2/6
    swap1(x, a[2]); // (b) swaps x with a[2]
    swap2(a[1], a[3]); // (c) swaps entry a[1] with a[3]
    median(1, 5, 4, 6, 7); // (d) prints 5, the median entry
    cout << sqrt(5, 10, 12, 14) << endl; // (e) prints 0.5 for any input values
    return 0;
}
```

(a) Title line for `asFraction` as called at the line marked (a).
Answer:

```cpp
string asFraction(int a, int b)
```

(b) Title line for `swap1` as called at the line marked (b).
Answer:

```cpp
void swap1(int &a, int &b)
```

(c) Title line for `swap2` as called at the line marked (c).
Answer:

```cpp
void swap2(int &a, int &b)
```

(d) Title line for `median` as called at the line marked (d).
Answer:

```cpp
void median(int a, int b, int c, int d, int e)
```

(e) Title line for `sqrt` as called at the line marked (e).
Answer:

```cpp
double sqrt(int a, int b, int c, int d)
```

Problem 347 Consider the following C++ program.
#include <iostream>
using namespace std;

int fun(int x) {
    if (x <= 0) return 100;
    if (x >= 9 && x % 2 == 1) return x + 1;
    if (x >= 9 || x % 3 == 0) return x + 2;
    return 5;
}

int rec(int x) {
    if (x < 100) return x/10;
    return rec(x / 10) + rec(x % 100);
}

int main() {
    cout << fun(-144) << endl; // line (a)
    cout << fun(71) << endl; // line (b)
    cout << rec(71) << endl; // line (c)
    cout << rec(-256) << endl; // line (d)
    cout << rec(729) << endl; // line (e)
}

(a) What is the output at line (a)?
Answer:
100

(b) What is the output at line (b)?
Answer:
72

(c) What is the output at line (c)?
Answer:
7

(d) What is the output at line (d)?
Answer:
-25

(e) What is the output at line (e)?
Answer:
9

Problem 348 Write a function called multiDigit that prints a new number formed from an integer parameter
by printing each odd digit and omitting all even digits. If a negative parameter is given, it should ignore the — sign
and treat the parameter as if it was positive.

For example, a program that uses the function multiDigit follows.

int main() {
    multiDigit(1245); cout << endl; // prints 15
    multiDigit(19683); cout << endl; // prints 193
    multiDigit(220); cout << endl; // prints
    multiDigit(-132); cout << endl; // prints 13
    return 0;
}
void multiDigit(int n) {
    if (n < 0) multiDigit(-n);
    else if (n == 0) return;
    else {
        multiDigit(n / 10);
        if (n % 2 != 0) cout << n % 10;
    }
}

Problem 349 Write a function called randFill that fills the entries of an array with random integers between a specified pair of limits. (Use an appropriate C++ function to generate the random numbers.)

For example, a program that uses the function follows.

int main() {
    int x[4];
    int min = 20, max = 29;
    randFill(x, 4, min, max);
    for (int i = 0; i <= 3; i++)
        cout << x[i] << endl; // prints 4 random numbers between 20 and 29
    return 0;
}

Answer:

void randFill(int a[], int c, int min, int max) {
    for (int i = 0; i < c; i++)
        a[i] = rand() % (max - min + 1) + min;
}

Problem 350 Suppose that a C++ program called prog.cpp is compiled and correctly executed on venus with the instructions:

venus> g++ prog.cpp
venus> a.out input1.txt input2 out.txt

For each of the following short segments of the program prog.cpp write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)

    int x = 7, y = 10;
    cout << (x/y + 2.0/y) << endl;

Answer:

0.2

(ii)

    char x = 'f';
    while (x >= 'a') {
        cout << x;
        x = x - 1;
    }

Answer:
cout << 'Z' - 'A';

Answer:
25

string x = "Easy Question";
cout << x.substr(4,2);

Answer:
Q

int main(int argc, char *argv[]) {
    cout << argv[2];
}

Answer:
input2

Problem 351 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer $n$ that is between 1 and 9.
2. It immediately stops if the supplied value of $n$ is not legal.
3. Otherwise it prints out a triangular picture (as shown in the diagram, but with $n$ rows) that uses the lowercase letters $a, b, c, \ldots$ in sequence, and if necessary continues with uppercase letter starting at $A$ after any $z$.

Here is an example of how the program should work:

Give me an integer between 1 and 9: 7
abedefg
hijklm
nopqr
stuv
wxy
zA
B

Answer:
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 9: ";
    cin >> n;
    if (n < 1 || n > 9) return 0;

    char x = 'a';
    for (int i = n; i >= 1; i--) {
        cout << x;
    }

    return 0;
}
for (int j = 1; j <= i; j++) {
    cout << x;
    x = x + 1;
    if (x > 'z') x = 'A';
}
cout << endl;
}

Problem 352 Write title lines for the functions most of which are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    cout << numSixes("19683") << endl; // (a) prints 1
    printNumSixes(19683); // (b) prints 1
    cout << longest(961, 1961, 5) << endl; // (c) prints 1961
    average(2.5, 3.4, 4.0); // (d) prints 3.3
    return 0;
}
```

(a) Title line for `numSixes`
Answer:

```cpp
int numSixes(string a)
```

(b) Title line for `printNumSixes`
Answer:

```cpp
void printNumSixes(int x)
```

(c) Title line for `longest`
Answer:

```cpp
int longest(int a, int b, int c)
```

(d) Title line for `average`
Answer:

```cpp
void average(double a, double b, double c)
```

(e) The required title line for a main program that uses arguments.
Answer:

```cpp
int main(int argc, char *argv[])
```

Problem 353 Consider the following C++ program.

```cpp
#include <iostream>
#include <fstream>
using namespace std;
int main() {
    ifstream infile("file.txt");
    for (int line = 1; line <= 5; line++) {
        cout << "Line " << line << " ";
        int x;
        if (infile.eof()) cout << "Done";
```
```cpp
infile >> x;
if (x > 10) cout << ++x;
if (x > 5) cout << 2 * x;
if (x > 0) cout << x;
if (x < 0) {
    infile >> x;
    cout << x;
}
cout << endl;
}
return 0;
}
```

The file called `file.txt` exists in the directory in which the above program is run. The file consists of the following data:

```
0 2 22 -2 2 -2 -22 22 222 2222
```

(a) What is the output line that begins: Line 1?

**Answer:**

Line 1

(b) What is the output line that begins: Line 2?

**Answer:**

Line 2 2

(c) What is the output line that begins: Line 3?

**Answer:**

Line 3 234623

(d) What is the output line that begins: Line 4?

**Answer:**

Line 4 2

(e) What is the output line that begins: Line 5?

**Answer:**

Line 5 -22

**Problem 354** Write a function called `sum3` that determines the sum of the first 3 digits in a parameter. If the parameter has fewer than 3 digits, the sum of whatever digits are present is reported. (Assume that the parameter always has a positive value.)

For example, a program that uses the function `sumSq` follows.

```cpp
int main() {
    cout << sum3(3456) << endl;  // prints 12 as the sum 3 + 4 + 5
    cout << sum3(11113) << endl; // prints 3 as the sum 1 + 1 + 1
    cout << sum3(9) << endl;     // prints 9
    return 0;
}
```

**Answer:**
int sum3(int x) {
    if (x < 1000) return x / 100 + (x / 10) % 10 + x % 10;
    return sum3(x / 10);
}

Problem 355 Write a function called numPositive that finds the number of rows with positive sum in a 2-dimensional array of decimals that has 4 columns. The array and the capacities are parameters. (Note that 0 is not positive.)

For example, a program that uses the function follows.

int main() {
    double d[2][4] = {{2, 4, -6, -8}, {-1, -3, 5, 1.5}};
    cout << numPositive(d, 2, 4) << endl;
    // prints 1 because only one row, the 2nd has a positive sum
    return 0;
}

Answer:

int numPositive(double d[][4], int r, int c) {
    int count = 0;
    for (int i = 0; i < r; i++) {
        double rowSum = 0;
        for (int j = 0; j < c; j++)
            rowSum = rowSum + d[i][j];
        if (rowSum > 0) count++;
    }
    return count;
}

Problem 356 Write a function called numX that reports the number of elements in a array of strings that contain an uppercase letter X.

For example, a program that uses the function follows.

int main() {
    cout << numX(data, 4);  // prints: 2 because 2 strings include an X
    return 0;
}

Answer:

int numX(string a[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (((int) a[i].find("X")) >= 0) ans++;
    return ans;
}

Problem 357 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter a positive integer n.
2. It repeatedly reads n from the user until the supplied value of n is positive.
3. It prints out a large letter N that has height n and width n. The locations of the printed characters should lie in the \(n \times n\) square region that the letter occupies.

Here is an example of how the program should work:
Give me a positive integer: 5
N N
NN N
N N N
N NN
N N

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Enter a value for n: " << endl;
    cin >> n;
    while (n <= 0) {
        cout << "No good. Give a positive value: " << endl;
        cin >> n;
    }
    for (int i = 1; i <= n; i++) {
        for (int j = 1; j <= n; j++)
            if (j == 1 || j == n || i == j)
                cout << "N" << " ";
            else cout << " ";
        cout << endl;
    }
    return 0;
}
```

Problem 358 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    cout << numDigits(19683) << endl; // (a) prints 5
    printNumDigits("19683"); // (b) prints 5
    cout << longer("Hello", "Goodbye") << endl; // (c) prints "Goodbye"
    biggest(3.14, 2.718, 1.5); // (d) prints 3.14
    cout << sqrt(5, 10, 12) << endl; // (e) prints the sum as 27
    return 0;
}
```

(a) Title line for `numDigits`
Answer:

```cpp
int numDigits(int x)
```

(b) Title line for `printNumDigits`
Answer:

```cpp
void printNumDigits(string x)
```

(c) Title line for `longer`
Answer:

```cpp
string longer(string a, string b)
```
(d) Title line for biggest
Answer:

```cpp
void biggest(double a, double b, double c)
```

(e) Title line for sqrt as called at the line marked (e).
Answer:

```cpp
int sqrt(int a, int b, int c)
```

**Problem 359**   Consider the following C++ program.

```cpp
#include <iostream>
#include <fstream>
using namespace std;

int main() {
    ifstream infile("file.txt");
    for (int line = 1; line <= 5; line++) {
        cout << "Line " << line << " ";
        int x;
        if (infile.eof()) cout << "Done";
        infile >> x;
        if (x > 10) cout << ++x;
        if (x > 5) cout << 2 * x;
        if (x > 0) cout << x;
        if (x < 0) {
            infile >> x;
            cout << x;
        }
        cout << endl;
    }
    return 0;
}
```

The file called file.txt exists in the directory in which the above program is run. The file consists of the following data:

```
0 4 6 14 -1 3 -2 -5 1 2 3
```

(a) What is the output line that begins: Line 1?
Answer:

Line 1

(b) What is the output line that begins: Line 2?
Answer:

Line 2 4

(c) What is the output line that begins: Line 3?
Answer:

Line 3 126
(d) What is the output line that begins: Line 4?

Answer:

Line 4 153015

(e) What is the output line that begins: Line 5?

Answer:

Line 5 3

Problem 360  Write a function called \textit{sumSq} that determines the sum of the squares of the digits in a parameter. For example, a program that uses the function \textit{sumSq} follows.

```c
int main() {
    cout << sumSq(34) << endl; // prints 25 because this is 9 + 16
    cout << sumSq(11113) << endl; // prints 13 found as 1+1+1+1+9
    cout << sumSq(9) << endl; // prints 81
    return 0;
}
```

Answer:

```c
int sumSq(int n) {
    if (n < 10) return n * n;
    return sumSq(n/10) + sumSq(n%10);
}
```

Problem 361  Write a function called \textit{smallestPositive} that finds the smallest positive entry in a 2-dimensional array of decimals that has 4 columns. The array and the capacities are parameters. If no entry in the array is positive, the function should return an answer of 0.0. (Note that 0 is not positive.) For example, a program that uses the function follows.

```c
int main() {
    double d[2][4] = {{2, 4, -6, 8}, {-1, -3, 5, 1.5}};
    cout << smallestPositive(d, 2, 4) << endl; // prints 1.5
    return 0;
}
```

Answer:

```c
double smallestPositive(double d[][4], int r, int c) {
    double answer = d[0][0];
    for (int i = 0; i < r; i++)
        for (int j = 0; j < c; j++)
            if (d[i][j] > 0) {
                if (answer <= 0 || d[i][j] < answer)
                    answer = d[i][j];
            if (answer > 0) return answer;
    return 0.0;
}
```

Problem 362  Write a function called \textit{insertX} that inserts an \textit{X} at the middle of each element of an array of strings. (If a string has even length, the \textit{X} should be added exactly at its middle, otherwise the \textit{X} should be added immediately before the middle.) For example, a program that uses the function follows.
int main() {
    insertX(data, 4);
    for (int i = 0; i < 4; i++)
        cout << data[i] << " "; // output: abXcd HeXllo 12X34 X
    return 0;
}

Answer:

void insertX(string d[], int cap) {
    for (int i = 0; i < cap; i++)
        d[i].insert(d[i].length()/2, "X");
}

Problem 363  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter a positive integer n.
2. It repeatedly reads n from the user until the supplied value of n is positive.
3. It prints out a large letter Z that has height n and width n. The locations of the printed characters should lie in the $n \times n$ square region that the letter occupies.
Here is an example of how the program should work:

Give me a positive integer:  5
ZZZZZ
  Z
  Z
ZZZZZ

Answer:

#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Enter a value for n: ";
    cin >> n;
    while (n <= 0) {
        cout << "No good. Give a positive value: ";
        cin >> n;
    }
    for (int i = 1; i <= n; i++) {
        for (int j = 1; j <= n; j++)
            if (i == 1 || i == n || (i + j) == (n + 1))
                cout << "Z";
            else cout << " ";
        cout << endl;
    }
    return 0;
}

Problem 364  Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.
int main() {
    int a[10] = {3,1,4,1,5,9,2,6,5,3};
    int x[3][2] = {{0,1},{2,3},{4,5}};
    int n = 7, m = 2;
    int i = sum(n, m); // sets i as the sum
    swap(n, m); // swaps n and m
    printArray(a, 10); // prints content of a
    print2dArray(x, 3, 2); // prints content of x
    cout << minElement(a, 10); // minimum element of array
    cout << firstDigit(n*n + m*m); // first digit
    return 0;
}

(a) Title line for sum
Answer:
int sum(int a, int b)

(b) Title line for swap
Answer:
void swap(int &a, int &b)

(c) Title line for printArray
Answer:
void printArray(int a[], int cap)

(d) Title line for print2dArray
Answer:
void print2dArray(int a[][2], int rows, int cols)

(e) Title line for minElement
Answer:
int minElement(int a[], int cap)

(f) Title line for firstDigit
Answer:
int firstDigit(int x)

Problem 365  Write a function called array2F that returns the largest entry in a 2-dimensional array (of integer values). The parameters are the array, its number of rows and its number of columns. For example, a program that uses the function array2F follows.

int main() {
    int a[3][4] = {{0, -2, 2, 4}, {10, -5, 1, 3}, {1, 4, 1, 0}};
    cout << array2F(a, 3, 4) << endl; // output is 10
    return 0;
}

Answer:
Problem 366  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

char recursive(char array[], int n) {
    char x = array[n];
    if ('a' <= x && x <= 'z') return x;
    cout << x;
    return recursive(array, n - 1);
}

int main() {
    char array[8] = {'a','b','c','d','0','1','2','3'};
    cout << array[1] << endl; // line a
    cout << (char) (array[1] + 1) << endl; // line b
    cout << recursive(array, 0) << endl; // line c
    cout << recursive(array, 4) << endl; // line d
    cout << recursive(array, 7) << endl; // line e
    return 0;
}
```

What is the output from the program at each of the following lines:

(a) line a:

b

(b) line b:

c

(c) line c:

a

(d) line d:

0d

(e) line e:

3210d

(f) line f:

-1
Problem 367  Write a function called `useRecursion` that returns the sum of the first two digits in a positive number. If there is only one digit, that digit is returned. For example, a program that uses the function `useRecursion` follows.

```cpp
int main() {
    cout << useRecursion(567982) << endl; // prints 11
    cout << useRecursion(107982) << endl; // prints 1
    cout << useRecursion(7) << endl; // prints 7
    return 0;
}
```

Answer:

```cpp
int useRecursion(int x) {
    if (x < 100) return x % 10 + x / 10;
    return useRecursion(x / 10);
}
```

Problem 368  Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Declare and initialize any variables that you use in each part.

(i) Print the number 7 to an output file whose system name is `out.txt`

```cpp
ofstream f("out.txt");
f << 7 << endl;
```

(ii) Read the first line of text in an input file whose system name is `in.txt`. Store the line in an appropriate variable called `line`.

```cpp
ifstream g("in.txt");
string line;
gline(g, line);
```

(iii) Write the title line for a main function that uses arguments.

```cpp
int main(int argc, char *argv[])
```

(iv) Print the 5th character of a string variable called `line` to the output screen.

```cpp
cout << line[4] << endl;
```

(v) Print the character after the first character equal to K in a string variable called `line` to the output screen. If there is no character K, print the first character of the string.

```cpp
int x = line.find('K');
if (x >= 0 && x < line.size() - 1)
    cout << line[x + 1];
else cout << line[0];
```

(vi) Print a random 2 digit integer to the output screen.

```cpp
cout << rand() % 90 + 10 << endl;
```

Problem 369  Write a complete C++ program that does the following.
1. It asks the user to enter a positive integer \( n \) that is at most 20. It continues asking until the user enters a correct input.
2. The program generates two random upper case letters (using the standard C++ random number generation function).
3. The program prints an \( n \times n \) square that uses the two characters to make a checkerboard pattern.

For example, if the user enters 5 and the random letters are K and W the following square picture is printed.
#include <iostream>
#include <cstdlib>
using namespace std;

int main() {

    int n;
    cout << "Enter a positive value for n that is at most 20: ";
    cin >> n;
    while ( n <= 0 || n > 20 ) {
        cout << "That is not legal. Try again: ";
        cin >> n;
    }

    char x = 'A' + rand() % 26;
    char y = 'B' + rand() % 26;

    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            if ((i + j) % 2 == 0) cout << x;
            else cout << y;
        }
        cout << endl;
    }

    return 0;
}

Problem 370 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

int main() {
    int a[10] = {3,1,4,1,5,9,2,6,5,3};
    int x[3][2] = {{0,1},{2,3},{4,5}};
    int n = 7, m = 2;
    int i = sum(n, m, n);       // sets i as the sum
    swap(n, m);                // swaps n and m
    addToArray(a, 10, 5);      // adds 5 to every entry
    printArray(x, 3, 2);       // prints content of x
    cout << maxElement(a, 10); // maximum element of array
    cout << firstDigit(n);     // first digit
    return 0;
}

(a) Title line for sum
Answer:

int sum(int a, int b, int c)

(b) Title line for swap
Answer:
void swap(int &a, int &b)

(c) Title line for addToArray
Answer:
void addToArray(int a[], int cap, int x)

(d) Title line for printArray
Answer:
void printArray(int a[][2], int rows, int cols)

(e) Title line for maxElement
Answer:
int maxElement(int a[], int cap)

(f) Title line for firstDigit
Answer:
int firstDigit(int x)

Problem 371 Write a function called array2F that returns the product of the negative entries in a 2-dimensional array (of integer values). The parameters are the array, its number of rows and its number of columns. For example, a program that uses the function array2F follows.

int main() {
    int a[3][4] = {{0, -2, 2, 4}, {10, -5, 1, 3}, {1, 4, 1, 0}};
    cout << array2F(a, 3, 4) << endl; // output is 10
    return 0;
}

Answer:
int array2F(int a[][4], int rows, int cols) {
    int answer = 1;
    for (int i = 0; i < rows; i++)
        for (int j = 0; j < cols; j++)
            if (a[i][j] < 0) answer *= a[i][j];
    return answer;
}

Problem 372 Consider the following C++ program.

#include <iostream>
using namespace std;

char recursive(char array[], int n) {
    char x = array[n];
    if ('a' == x || x == 'b') return x;
    cout << x;
    return recursive(array, n - 1);
}

int main() {
    char array[8] = { 'a', 'b', 'c', 'd', '0', '1', '2', '3' };
    cout << array[0] << endl; // line a
cout << (char) (array[0] + 3) << endl; // line b
cout << recursive(array, 0) << endl; // line c
cout << recursive(array, 2) << endl; // line d
cout << recursive(array, 7) << endl; // line e
return 0;
}

What is the output from the program at each of the following lines:
(a) line a:

a

(b) line b:

d

(c) line c:

a

(d) line d:

cb

(e) line e:

3210dcb

(f) line f:

2

**Problem 373**  Write a function called *useRecursion* that returns the larger of the first two digits in a positive number. If there is only one digit, that digit is returned. For example, a program that uses the function *useRecursion* follows.

```cpp
int main() {
    cout << useRecursion(567982) << endl; // prints 6
    cout << useRecursion(107982) << endl; // prints 1
    cout << useRecursion(7) << endl; // prints 7
    return 0;
}
```

**Answer:**

```cpp
int useRecursion(int x) {
    if (x < 100) {
        if (x / 10 > x % 10) return x / 10;
        return x % 10;
    }
    return useRecursion(x / 10);
}
```

**Problem 374**  Write C++ statements to carry out the following tasks. **Do not write complete programs**, just give a single line, or a few lines of C++ instructions. Declare and initialize any variables that you use in each part.

(i) Read the first line of text in an input file whose system name is *input.txt*. Store the line in an appropriate variable called *line*. 

(ii) Print the number 2 to an output file whose system name is output.txt

    ofstream f("output.txt");
    f << 2 << endl;

(iii) Print the length of a string variable called line to the output screen.

    cout << line.length() << endl;

(iv) Write the title line for a main function that uses arguments.

    int main(int argc, char *argv[])

(v) Print the character before the first character equal K in a string variable called line to the output screen. If there is no character K, or no character before it print the first character of the string.

    int x = line.find('K');
    if (x <= 0) cout << line[0];
    cout << line[x - 1];

(vi) Print a random 3 digit integer to the output screen.

    cout << rand() % 900 + 100 << endl;

**Problem 375** Write a complete C++ program that does the following.
1. It asks the user to enter a positive integer \( n \) that is at most 20. It continues asking until the user enters a correct input.
2. The program generates \( n^2 \) random upper case letters (using the standard C++ random number generation function).
3. The program prints an \( n \times n \) square that is filled with its chosen random letters.
   
   For example, if the user enters 5 the following square picture might be printed.

   
   KWXDG
   YKWQT
   AGDKE
   IEXVL
   UGBLQ

   **Answer:**

   ```cpp
   #include <iostream>
   #include <cstdlib>
   using namespace std;

   int main() {
       int n;
       cout << "Enter a positive value for n that is at most 20: ";
       cin >> n;
       while (n <= 0 || n > 20) {
           cout << "That is not legal. Try again: ";
           cin >> n;
       }
   }
   ```
Problem 376  Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```c
int main() {
    int a[10] = {3,1,4,1,5,9,2,6,5,3};
    int x[3][2] = {{0,1},{2,3},{4,5}};
    int n = 7, m = 2;
    int i = diff(n, m); // sets i as the difference
    swap(n, m); // swaps values of inputs
    printArray(a, 10); // prints content of a
    addToArray(x, 3, 2, 5); // adds 5 to every entry in array
    cout << average(a, 10); // average of array
    cout << first2Digits(n + m); // first two digits
    return 0;
}
```

(a) Title line for `diff`
Answer:

```c
int diff(int a, int b)
```

(b) Title line for `swap`
Answer:

```c
void swap(int &a, int &b)
```

(c) Title line for `printArray`
Answer:

```c
void printArray(int a[], int cap)
```

(d) Title line for `addToArray`
Answer:

```c
void addToArray(int a[][2], int rows, int cols, int x)
```

(e) Title line for `average`
Answer:

```c
double average(int a[], int cap)
```

(f) Title line for `first2Digits`
Answer:
Problem 377  Write a function called \texttt{array2F} that returns the number of non-zero entries in a 2-dimensional array (of integer values). The parameters are the array, its number of rows and its number of columns. For example, a program that uses the function \texttt{array2F} follows.

```cpp
int main() {
    int a[3][4] = {{0, -2, 2, 4}, {10, -5, 1, 3}, {1, 4, 1, 0}};
    cout << array2F(a, 3, 4) << endl;  // output is 10
    return 0;
}
```

\textbf{Answer:}

```cpp
int array2F(int a[][4], int rows, int cols) {
    int answer = 0;
    for (int i = 0; i < rows; i++)
        for (int j = 0; j < cols; j++)
            if (a[i][j] != 0) answer++;
    return answer;
}
```

Problem 378  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

char recursive(char array[], int n) {
    char x = array[n];
    if ('0' <= x && x <= '9') return x;
    cout << x;
    return recursive(array, n - 1);
}

int main() {
    char array[8] = {'0','1','2','3','a','b','c','d'};
    cout << array[1] << endl;  // line a
    cout << (char) (array[1] + 1) << endl;  // line b
    cout << recursive(array, 0) << endl;  // line c
    cout << recursive(array, 4) << endl;  // line d
    cout << recursive(array, 7) << endl;  // line e
    return 0;
}
```

What is the output from the program at each of the following lines:

(a) line a:

1

(b) line b:

2

(c) line c:
Problem 379  Write a function called useRecursion that returns the second digit in a positive number. If there is only one digit, that digit is returned. For example, a program that uses the function useRecursion follows.

```cpp
int main() {
    cout << useRecursion(567982) << endl;  // prints 6
    cout << useRecursion(107982) << endl;  // prints 0
    cout << useRecursion(7) << endl;       // prints 7
    return 0;
}
```

Answer:

```cpp
int useRecursion(int x) {
    if (x < 100) return x % 10;
    return useRecursion(x / 10);
}
```

Problem 380  Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Declare and initialize any variables that you use in each part.

(i) Write the title line for a main function that uses arguments.

```cpp
int main(int argc, char *argv[]) {
}
```

(ii) Print the number 13 to an output file whose system name is out.txt

```cpp
ofstream f("out.txt");
f << 13 << endl;
```

(iii) Read the first string in an input file whose system name is in.txt. Store the string in an appropriate variable called data.

```cpp
ifstream g("in.txt");
string data;
getline(g, data);
```

(iv) Print the 8th character of a string variable called line to the output screen.

```cpp
cout << line[7] << endl;
```

(v) Print the position of the first character equal to K in a string variable called line to the output screen. If there is no character K, print -1.
Problem 381  Write a complete C++ program that does the following.
1. It asks the user to enter a positive integer $n$ that is at most 20. If an incorrect response is entered it exits.
2. The program generates a random upper case letter and a random lower case letter (using the standard C++ random number generation function).
3. The program prints an $n \times n$ square that uses the two characters to make a checkerboard pattern.
For example, if the user enters 5 and the random letters are K and w the following square picture is printed.

\[
\begin{array}{c}
KwKwK \\
wKwKw \\
KwKwK \\
wKwKw \\
KwKwK
\end{array}
\]

Answer:

```cpp
#include <iostream>
#include <cstdlib>
using namespace std;

int main() {
    int n;
    cout << "Enter a positive value for n that is at most 20: ";
    cin >> n;
    if (n <= 0 || n > 20) {
        cout << "That is not legal. " << endl;
        exit(0);
    }

    char x = 'A' + rand() % 26;
    char y = 'a' + rand() % 26;

    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            if ((i + j) % 2 == 0) cout << x;
            else cout << y;
        }
        cout << endl;
    }
    return 0;
}
```

Problem 382  Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```cpp
int main() {
    int a[4] = {3,1,4,1}, i = 3, j = 5, k = 4;
```
Problem 383 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter a positive integer that is between 1 and 26.
2. The program reads a value $n$ entered by the user. If the value is not legal, the program exits.
3. The program prints an $n \times n$ pattern of characters, in which the bottom right character is an 'A'. The bottom right $2 \times 2$ block is completed by three 'B' characters. The bottom right $3 \times 3$ block is completed by five 'C' characters, and so on.

For example, if the user enters 5 for $n$ the program should print the following picture.

```
EEEEE
EDDDD
EDCCC
EDCBB
EDCBA
```

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int n;
    // ...
}
```
cout << "Enter an integer between 1 and 26: ";
cin >> n;
if (n < 1 || n > 26) exit(1);

for (int r = 1; r <= n; r++) {
    char k = (char) ('A' + n - r);
    for (int c = 1; c <= n; c++) {
        if (c < r) k = (char) ('A' + n - c);
        cout << k;
    }
    cout << endl;
}
return 0;

Problem 384
Write a function called emergency that detects whether a number contains the sequence of digits 911. For example, a program that uses the function emergency follows.

int main() {
    if (emergency(56791182)) cout << "Warning" << endl; // prints warning
    if (emergency(56791212)) cout << "Warning" << endl; // no print here
    if (emergency(91191191)) cout << "Warning" << endl; // prints warning
    return 0;
}

Answer:

bool emergency(int x) {
    if (x <= 0) return false;
    if (x % 1000 == 911) return true;
    return emergency(x / 10);
}

Problem 385
Consider the following C++ program.

#include <iostream>
using namespace std;

string recursive(string x) {
    if (x.length() == 0) return ":";
    return x.substr(0,1) + "#" + recursive(x.substr(1));
}

int main(int argc, char *argv[]) {
    int i = 1, j = 2, k = 3;
    string array[2] = {"", "hello"};
    cout << ++k << endl; // line a
    k = ++i - j++;
    cout << i << j << k << endl; // line b
    cout << recursive(array[0]) << endl; // line c
    cout << recursive(array[1]) << endl; // line d
    cout << argv[1] << endl; // line e
    return 0;
}

The program is compiled to produce a binary called a.out. The binary is run with the command:
What is the output from the program at each of the following lines:
(a) line a:
4
(b) line b:
230
(c) line c:
:
(d) line d:
h#e#l#l#o#
(e) line e:
CS111

Problem 386    Write C++ statements to carry out the following tasks. **Do not write complete programs,** just give a single line, or a few lines of C++ instructions. Assume that the following variables have been declared, and if necessary have values, for each part. All other necessary variables should be declared and initialized.

```cpp
int x, y, table[100][100];
string name;
```

(i) Print the quotient when \( x \) is divided into \( y \).

```cpp
cout << y/x << endl;
```

(ii) Print \( table[2][2] \) to the file `out.txt`. (In this part you need to declare a variable to access the file.)

```cpp
ofstream f("out.txt");
f << table[2][2];
```

(iii) Print HELLO if you can find the substring *Freddy* within *name*. Otherwise print HI.

```cpp
if (name.find("Freddy") >= 0) cout << "HELLO";
else cout << "HI";
```

(iv) Print the sum of all the numbers in column number 17 of the 2-dimensional array called `table`. (The array `table` has 100 rows and 100 columns. As usual the array begins with row number 0.)

```cpp
int ans = 0;
for (int r = 0; r <= 99; r++)
    ans += table[r][17];
cout << ans;
```

(v) Print a random integer value between 13 and 19 (inclusive) to the screen. (The random integer should be determined by using an appropriate C++ function.)

```cpp
cout << rand() % 7 + 13;
```
Problem 387  Write a complete C++ program that does the following.
1. It asks the user to enter positive integers \( a \) and \( b \) that are each at most 100.
2. The program reads in a table of integers with \( a \) rows and \( b \) columns as entered by the user.
3. The program determines and prints the maximum entry in each column of the table.
4. The program then prints the smallest value among these maximum entries.
For example, the following represents one run of the program.

Enter integers for \( r \) and \( c \) (at most 100):  2 2
Enter 2 rows of 2 integers:
1 4
2 0
The maximum entries in the columns are:  2 4
The smallest of the printed maximum entries is :  2

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int a, b;
    int table[100][100];
    int max[100];
    int minMax;
    cout << "Enter integers for r and c (at most 100): ";
    cin >> a >> b;
    cout << "Enter " << a << " rows of " << b << " integers:\n";
    for (int r = 0; r < a; r++) {
        for (int c = 0; c < b; c++)
            cin >> table[r][c];
    }
    cout << "The maximum entries in the columns are: ";
    for (int c = 0; c < b; c++) {
        max[c] = table[0][c];
        for (int r = 0; r < a; r++)
            if (table[r][c] > max[c]) max[c] = table[r][c];
        cout << max[c] << " ";
    }
    cout << "\nThe smallest of the printed maximum entries is : ";
    cout << endl;
    return 0;
}
```

Problem 388  Write title lines (header lines or prototypes) for the following functions. Do not supply the blocks for the functions.
(a) A function called `middleDigit` which returns the middle digit of an integer.
Answer:

```cpp
int middleDigit(int x)
```

(b) A function called `sqrt` that returns the square root of a double precision parameter.
Answer:

```cpp
double sqrt(double x)
```
(c) A function called `duplicateString` which returns a new copy of string.

**Answer:**

```cpp
string duplicate(string original)
```

(d) A function called `randomFile` which is to return a randomly created name to use for an output file.

**Answer:**

```cpp
string randomFile()
```

(e) A function called `selectionSort` which is to sort an array of strings into alphabetical order.

**Answer:**

```cpp
void selectionSort(string data[], int length)
```

**Problem 389** Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter a positive integer.
2. The program reads a value \( n \) entered by the user. If the value is not legal, the program repeatedly makes the user type in another value until a legal value of \( n \) has been entered.
3. The program prints an \( n \times (2n - 1) \) pattern of * symbols in the shape of a large solid triangle.

For example, if the user enters 4 for \( n \) the program should print the following picture.

```
*  
*** 
***** 
*******
```

**Answer:**

```cpp
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Enter a positive integer: ";
    cin >> n;
    while (n <= 0) {
        cout << "That is not positive. Try again: ";
        cin >> n;
    }

    for (int row = 1; row <= n; r++) {
        int rowSpace = n - row;
        int rowStars = 2 * row - 1;
        for (int c = 1; c <= rowSpace; c++) cout << " ";
        for (int c = 1; c <= rowStars; c++) cout << "*";
        cout << endl;
    }

    return 0;
}
```

**Problem 390** Write a function called `removeFirst` that removes the first digit from a number. The answer should be returned as an integer. (Drop any leading 0 digits in the answer. So that as in the example below, removing the first from 1024 leaves 24.)

A program that uses the function `removeFirst` follows.
int main() {
    int n = 19683;
    int m = removeFirst(n);
    cout << m << endl;  // output 9683
    cout << removeFirst(1024); // output 24
    return 0;
}

Answer:

int removeFirst(int n) {
    if (n < 10) return 0;
    return removeFirst(n / 10) * 10 + n % 10;
}

Problem 391  Consider the following C++ program.

#include <iostream>
using namespace std;

string recursive(string x) {
    if (x.length() <= 1) return x;
    return x.substr(0,2) + recursive(x.substr(1));
}

int main(int argc, char *argv[]) {
    int i = 1, j = 2, k = 3;
    string array[2] = {"A", "hello"};
    cout << ++argc << endl; // line a
    k = ++i * j++;
    cout << i << j << k << endl; // line b
    cout << recursive(array[0]) << endl; // line c
    cout << recursive(array[1]) << endl; // line d
    cout << recursive(argv[3]) << endl; // line e
    return 0;
}

The program is compiled to produce a binary called a.out. The binary is run with the command:

venus> ./a.out CS111 Final Exam

What is the output from the program at each of the following lines:
(a) line a:
5
(b) line b:
234
(c) line c:
A
(d) line d:
heelilloo
Problem 392  Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Include declarations for any variable that you use.

(i) Print the word HELLO to the file out.txt.

```cpp
ofstream f("out.txt");
f << "HELLO";
```

(ii) Print a random upper case letter to the screen. (The random letter should be determined by using an appropriate C++ function.)

```cpp
cout << (char) ('A' + rand() % 26);
```

(iii) Read a line of text from the user and print the word NO if it contains the string Fred.

```cpp
string name;
cin >> name;
if (name.find("Freddy") >= 0) cout << "NO";
```

(iv) Print the first 4 characters of the string s. Assume that the string has length at least 4.

```cpp
cout << s.substr(0, 4) << endl;
```

(v) Swap the values of integer variables called p and q.

```cpp
int temp = p;
p = q;
q = temp;
```

Problem 393  Write a complete C++ program that does the following.

1. It asks the user to enter positive integers a and b that are each at most 20.
2. The program generates random integer values between 1 and 6 as the entries in a table with a rows and b columns.
3. The program then prints the table.
4. The program then prints the diagonal entries from the table.

For example, the following represents one run of the program.

Enter integers for r and c (at most 20): 2 2
The table has been generated as:
6 3
1 2
The diagonal is: 6 2

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int a, b, row, col;
    int table[21][21];
    cout << "Enter integers for r and c (at most 20): ";
    cin >> a >> b;
    ...
for (row = 1; row <= a; row++)
    for (col = 1; col <= b; col++)
        table[row][col] = rand() % 6 + 1;

cout << " The table has been generated as: " << endl;
for (row = 1; row <= a; row++) {
    for (col = 1; col <= b; col++)
        cout << table[row][col] << " ");
    cout << endl;
}

return 0;

Problem 394  Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

int main() {
    string name = "Freddy", secondName = "Fred";
    cout << thirdChar(name);  // print the 3rd character
    if ( !isLegal(name) )       // reject illegal names
        readName(name);        // and reads a name entered by the user
    exchangeNames(name, secondName);   // Swap the two names
    cout << bothNames(name, secondName); // print full name
    return 0;
}

(a) Title line for thirdChar
Answer:
char thirdChar(string name)

(b) Title line for isLegal
Answer:
bool isLegal(string name)

(c) Title line for readName
Answer:
void readName(string &name)

(d) Title line for exchangeNames
Answer:
void exchangeNames(string &name, string &otherName)

(e) Title line for bothNames
Answer:
string bothNames(string name, string otherName)
Problem 395  Write C++ statements to carry out the following tasks. **Do not write complete programs,** just give a single line, or a few lines of C++ instructions. Assume that the following variables have been declared, and if necessary have values, for each part. All other necessary variables should be declared and initialized.

```cpp
int x, y, table[100][100];
string name;
```

(i) Print the remainder when \( x \) is divided into \( y \).

```cpp
cout << y % x;
```

(ii) Print \( name \) to the file \( out.txt \). (In this part you need to declare a variable to access the file.)

```cpp
ofstream fout("out.txt");
ofout << name;
```

(iii) Read a line of text from the file \( out.txt \) into the variable \( name \).

```cpp
ifstream fin("out.txt");
getline(fin, name);
```

(iv) Print the average of all the numbers in row number 17 of the 2-dimensional array called \( table \). (The array \( table \) has 100 rows and 100 columns. As usual the array begins with row number 0.)

```cpp
int sum = 0;
for (int a = 0; a < 100; a++)
    sum += table[17][a];
cout << sum / 100.0;
```

(v) Print a sequence of 20 random integer values each between 1 and 20 (inclusive) to the screen. (The random integers should be determined by using an appropriate C++ function.)

```cpp
for (int a = 0; a < 20; a++)
    cout << rand() % 20 + 1;
```

Problem 396  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter a positive integer.
2. The program reads a value \( n \) entered by the user. If the value is not legal, the program repeatedly makes the user type in another value until a legal value of \( n \) has been entered.
3. The program prints an \( n \times n \) pattern of \( * \) symbols in the shape of an empty right triangle (with the point down).

For example, if the user enters 7 for \( n \) the program should print the following picture.

```
******
 * *
 * *
 * *
 * * *
 **
 * *
```

Answer:

```cpp
#include <iostream>
#include <string>
using namespace std;
int main() {
    int n = -1;
    while (n < 0) {
        cout << "Enter a positive integer: " << flush;
        cin >> n;
        if (n < 0)
            cout << "Invalid value. Try again.\n";  
```
cout << "Enter a positive integer: ";
cin >> n;
}
for (int r = 1; r <= n; r++) {
    for (int c = 1; c <= n; c++) {
        if (r == c || r == 1 || c == n) cout << "*";
        else cout << " ";
    }
    cout << endl;
} //for r
} //main

Problem 397 Write a function called evenUp that uses an integer parameter and returns a result that is found by increasing each even digit in the parameter by 1. For example, if the parameter has value 19683 the returned result would be 19793.

A program that uses the function evenUp follows.

```cpp
int main() {
    cout << evenUp(10) << endl; // prints 11
    cout << evenUp(2662) << endl; // prints 3773
    cout << evenUp(19683) << endl; // prints 19793
    return 0;
}
```

Answer:

```cpp
int evenUp(int x) {
    if (x < 10 && x % 2 == 0) return x + 1;
    if (x < 10 && x % 2 == 1) return x;
    return 10 * evenUp(x / 10) + evenUp(x % 10);
}
```

Problem 398 For each of the following short segments of a program write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)

```cpp
double x = 4, y = 8;
bool z = (x <= y || y <= x);
if (z) cout << y / x;
else cout << x / y;
cout << endl;
```

Answer:

2.0

(ii)

```cpp
char Int = 'C';
Int = Int + 1;
cout << Int << endl;
```

Answer:

D

(iii)
int i = 1;
while (i++ < 10) {
    cout << ++i << endl;
}

Answer:
3
5
7
9
11

(iv)

int x[3][3] = {{1,2,3}, {4,7,10}, {11,15,19}};
for (int i = 0; i <= 2; i++)
    cout << x[i][i];
    cout << endl;

Answer:
1719

(v)

string x[3] = {"Hello", "CS111", "Exam"};
for (int j = 1; j <= 3; j++)
    for (int i = 2; i >= 0; i--)
        cout << x[i][j];
    cout << endl;

Answer:
Hello
CS111
Exam

Problem 399  Write a complete C++ program that does the following.
1. It asks the user to enter a positive integer \( n \) that is at most 20.
2. The program then reads \( n \) words from the user. (You should assume that each word contains between 1 and 10 characters.)
3. The program then prints a summary giving the number of words with each length.
For example, the following represents one run of the program.

Enter an integer \( n \) (at most 20):  3
Enter 3 words: Hello CS111 Exam
Length 4: count 1
Length 5: count 2

In the exam the words Hello and CS111 have length 5, and give the count of 2 words with length 5. No counts are printed for word lengths other than 4 and 5 because no other word lengths are encountered in this example.

Answer:

#include <iostream>
using namespace std;
int main ()
{
    int n;
    cout << "Enter positive integer that is at most 20: ";
    cin >> n;

```cpp
string words[20];
cout << "Enter " << n << " words: ";
for (int a = 0; a < n; a++) cin >> words[a];

int count[11]; // for lengths 1 thru 10 inclusive, nothing of length 0
for (int a = 0; a < 11; a++) count[a] = 0;
for (int a = 0; a < n; a++) {
    int len = words[a].length();
    count[len]++;
} // for
for (int a = 0; a < 11; a++)
    if (count[a] != 0)
        cout << "Length " << a << " : count " << count[a] << endl;
} //main

Problem 400 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

int main() {
    string name = "Freddy", secondName = "Fred";
    fixThirdChar(name); // change the 3rd character to X
    if ( !isLegal(secondName) ) // reject illegal names
        secondName = readName(); // and reads a name entered by the user
    exchangeNames(name, secondName); // Swap the two names
    printBothNames(name, secondName); // print full name
    return 0;
}

(a) Title line for fixThirdChar
Answer:

void fixThirdChar(string &name)

(b) Title line for isLegal
Answer:

bool isLegal(string name)

(c) Title line for readName
Answer:

string readName()

(d) Title line for exchangeNames
Answer:

void exchangeNames(string &name, string &otherName)

(e) Title line for printBothNames
Answer:

void printBothNames(string name, string otherName)

Problem 401 Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Assume that the following variables have been declared, and if necessary have values, for each part. All other necessary variables should be declared and initialized.
```
int x, y, table[100][100];
string name;

(i) Print the remainder when \( y \) is divided by \( x \).

cout << y % x;

(ii) Print \( \text{table}[0][0] \) to the file output.txt. (In this part you need to declare a variable to access the file.)

ofstream fout("output.txt");
fout << table[0][0];

(iii) Read a line of text from the file output.txt into the variable \( \text{name} \).

ifstream fin("output.txt");
getline(fin, name);

(iv) Print the average of all the numbers in column number 37 of the 2-dimensional array called \( \text{table} \). (The array \( \text{table} \) has 100 rows and 100 columns. As usual the array begins with column number 0.)

int sum = 0;
for (int a = 0; a < 100; a++)
    sum += table[a][37];
cout << sum / 100.0;

(v) Print a sequence of 10 random integer values each between 1 and 100 (inclusive) to the screen. (The random integers should be determined by using an appropriate C++ function.)

for (int a = 0; a < 10; a++)
    cout << rand() % 100 + 1;

Problem 402  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter a positive integer.
2. The program reads a value \( n \) entered by the user. If the value is not legal, the program repeatedly makes the user type in another value until a legal value of \( n \) has been entered.
3. The program prints an \( n \times n \) pattern of * symbols in the shape of an empty right triangle (with the point up). For example, if the user enters 7 for \( n \) the program should print the following picture.

*  
** 
* *  
* *  
* *  
* *  
*******

Answer:

#include <iostream>
using namespace std;

int main() {
    int n = -1;
    while (n < 0) {
        cout << "Enter positive integer: ";
        cin >> n;
    }
}
for (int r = 1; r <= n; r++) {
    for (int c = 1; c <= n; c++) {
        if (r == n || c == n || r + c == n + 1) cout << "+";
        else cout << "+";
    }
    cout << endl;
} //for r
} //main

Problem 403  Write a function called \textit{bigDown} that uses an integer parameter. It returns a result that is found from the parameter by subtracting 1 from any digit that is 5 or larger. For example, if the parameter has value 19683 the returned result would be 18573.

A program that uses the function \textit{bigDown} follows.

```cpp
int main() {
    cout << bigDown(10) << endl; // prints 10
    cout << bigDown(2654) << endl; // prints 2544
    cout << bigDown(19683) << endl; // prints 18573
    return 0;
}
```

Answer:

```cpp
int bigDown(int x) {
    if (x < 5) return x;
    if (x < 10) return x - 1;
    return 10 * bigDown(x / 10) + bigDown(x % 10);
}
```

Problem 404  For each of the following short segments of a program write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)

```cpp
double x = 4, y = 8;
bool z = (x <= y && y <= x);
if (z) cout << y / x;
else cout << x / y;
cout << endl;
```

Answer:

0.5

(ii)

```cpp
char Int = 'D';
Int = Int - 1;
cout << Int << endl;
```

Answer:

C

(iii)

```cpp
int i = 1;
while (++i < 10) {
    cout << i++ << endl;
}
```
Problem 405  Write a complete C++ program that does the following.
1. It asks the user to enter a positive integer $n$ that is at most 25.
2. The program then reads $n$ words from the user. (You should assume that each word contains between 3 and 12 characters.)
3. The program then prints a summary giving the number of words with each length.
For example, the following represents one run of the program.

Enter an integer $n$ (at most 20): 3
Enter 3 words: Hello CS111 Exam
Length 4: count 1
Length 5: count 2

In the exam the words Hello and CS111 have length 5, and give the count of 2 words with length 5. No counts are printed for word lengths other than 4 and 5 because no other word lengths are encountered in this example.

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Enter positive integer that is at most 25: ";
    cin >> n;

    string words[25];
    cout << "Enter " << n << " words: ";
    for (int a = 0; a < n; a++) cin >> words[a];

    int count[13]; // lengths upto 12
    for (int a = 0; a < 13; a++) count[a] = 0;
```
Problem 406  Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Assume that the following variables have been declared, and if necessary have values, for each part. All other necessary variables should be declared and initialized.

```cpp
int x, y, table[100][100];
string name;
```

(i) Print the remainder when \(x\) is divided by \(y\).

```cpp
cout << x % y;
```

(ii) Print \(table[1][1]\) to the file \(outfile.txt\). (In this part you need to declare a variable to access the file.)

```cpp
ofstream fout("outfile.txt");
fout << table[1][1];
```

(iii) Read a line of text from the file \(infile.txt\) into the variable \(name\).

```cpp
ifstream fin("outfile.txt");
getline(fin, name);
```

(iv) Print the average of all the numbers in row number 27 of the 2-dimensional array called \(table\). (The array \(table\) has 100 rows and 100 columns. As usual the array begins with row number 0.)

```cpp
int sum = 0;
for (int a = 0; a < 100; a++)
  sum += table[27][a];
cout << sum / 100.0;
```

(v) Print two random integer values each between 100 and 200 (inclusive) to the screen. (The random integers should be determined by using an appropriate C++ function.)

```cpp
cout << rand() % 101 + 100;
cout << rand() % 101 + 100;
```

Problem 407  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter a positive integer.
2. The program reads a value \(n\) entered by the user. If the value is not legal, the program repeatedly makes the user type in another value until a legal value of \(n\) has been entered.
3. The program prints an \(n \times n\) pattern of * symbols in the shape of an empty right triangle (with the point up). For example, if the user enters 7 for \(n\) the program should print the following picture.

```
*
**
* *
* *
* *
* *
******
```
Problem 408 Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Assume that the following variables have been declared, and if necessary have values, for each part. All other necessary variables should be declared and initialized.

- **int x, y, table[100][100];
  string name;**

  (i) Print the remainder when y is divided into x.

  ```cpp
cout << x % y;
```

  (ii) Print x and y to the file `out.txt`. (In this part you need to declare a variable to access the file.)

  ```cpp
ofstream fout("out.txt");
fout << x << y;
```

  (iii) Read a word of text from the file `infile.txt` into the variable `name`.

  ```cpp
ifstream fin("infile.txt");
fin >> name;
```

  (iv) Print the average of all the numbers in column number 27 of the 2-dimensional array called `table`. (The array `table` has 100 rows and 100 columns. As usual the array begins with column number 0.)

  ```cpp
int sum = 0;
for (int a = 0; a < 100; a++)
  sum += table[a][27];
cout << sum / 100.0;
```

  (v) Print two random integer values each between 10 and 99 (inclusive) to the screen. (The random integers should be determined by using an appropriate C++ function.)

  ```cpp
cout << rand() % 90 + 10;
cout << rand() % 90 + 10;
```
Problem 409  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter a positive integer.
2. The program reads a value $n$ entered by the user. If the value is not legal, the program repeatedly makes the user type in another value until a legal value of $n$ has been entered.
3. The program prints an $n \times n$ pattern of * symbols in the shape of an empty right triangle (with the point down). For example, if the user enters 7 for $n$ the program should print the following picture.

```
*******
*   *
*   *
*   *
*   *
*   *
** *
*  *
```

Answer:

```c++
#include <iostream>
using namespace std;

int main(){
    int n = -1;
    while (n < 0) {
        cout << "Enter positive integer: ";
        cin >> n;
    }

    for (int r = 1; r <= n; r++) {
        for (int c = 1; c <= n; c++) {
            if (r == 1 || c == 1 || r + c == n + 1) cout << "*";
            else cout << " ";
        }
        cout << endl;
    } //for r
} //main
```

Problem 410  For each of the following short segments of a program write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)

```
double x = 4, y = 8;
bool z = (x > y || y > x);
if (z) cout << y / x;
else cout << x / y;
cout << endl;
```

Answer:

```
2.0
```

(ii)

```
char Int = 'd';
Int = Int + 1;
cout << Int << endl;
```

Answer:
(iii)

    int i = 1;
    while (i++ < 10) {
        cout << i++ << endl;
    }

Answer:

2
4
6
8
10

(iv)

    int x[3][3] = {{1,2,3},{4,7,10},{11,15,19}};
    for (int i = 0; i <= 2; i++)
        cout << x[i][2 - i];
    cout << endl;

Answer:

3711

(v)

    string x[3] = {"Hello", "CS111", "Exam"};
    for (int j = 1; j <= 3; j++) for (int i = 0; i <= 2; i++)
        cout << x[i][j];
    cout << endl;

Answer:

eSxllal1m

Problem 411  For each of the following short segments of a program write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)

    double x = 4, y = 8;
    bool z = (x > y && y > x);
    if (z) cout << y / x;
    else cout << x / y;
    cout << endl;

Answer:

0.5

(ii)

    char Int = 'b';
    Int = Int - 1;
    cout << Int << endl;

Answer:
(iii)

```c
int i = 1;
while (++i < 10) {
    cout << i++ << endl;
}
```

Answer:

```
2
4
6
8
```

(iv)

```c
int x[3][3] = {{4,7,10}, {11,15,19}, {1,2,3}};
for (int i = 0; i <= 2; i++)
    cout << x[i][2 - i];
    cout << endl;
```

Answer:

```
10151
```

(v)

```c
for (int j = 1; j <= 3; j++) for (int i = 0; i <= 2; i++)
    cout << x[i][j];
    cout << endl;
```

Answer:

```
Sxelall1m1
```

Problem 412 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

```c
int main() {
    string name; int x, y, array[20];
    name = enterName(); // Reads a name entered by the user
    cout << lastChar(name); // Print the last character
    enterNumbers(x, y); // Ask for and read in values for x and y
    cout << power(x, y); // x raised to the power y
                // answer is decimal to allow for negative powers
    cout << reverse(name); // Prints the name backwards
                // so Fred would be printed as derF
    randomize(array, 20); // fill the array with random numbers
    return 0;
}
```

(a) Title line for `lastChar`

```c
char lastChar (string name)
```

(b) Title line for `enterNumbers`
Problem 413 Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Assume that the following variables have been declared, and if necessary have values, for each part:

```c++
int x[10], z[10][10], r, c;
```

(i) Increase every entry of x by 1.
```
for (int i = 0; i < 10; i++) x[i]++;
```

(ii) Set r to be a random integer between c and c + 10. (The random integer should be determined by an appropriate C++ function.)
```
r = rand () % 11 + c;
```

(iii) Print the sum of all 100 entries of the 2-dimensional array z.
```
int sum = 0;
for (int i = 0; i < 10; i++)
    for (int j = 0; j < 10; j++)
        sum += z[i][j];
```

(iv) Print the last 5 entries of the array x.
```
for (int i = 5; i < 10; i++) cout << x[i];
```

(v) Swap column number 2 with column number 3 in the 2-dimensional array z.
```
for (int i = 0; i < 10; i++) {
    int temp = z[i][2];
    z[i][2] = z[i][3];
    z[i][3] = temp;
} //for
```

Problem 414 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter a positive integer.
2. The program reads a value n entered by the user. If the value is not legal, the program repeatedly makes the user type in another value until a legal value of n has been entered.
3. The program prints the first n squares and their sum.

For example, if the user enters 4 for n the program should produce the following output.
1 4 9 16
sum to 30

Answer:

#include <iostream>
using namespace std;

int main ()
{
    int a = -1;
    while (a < 0) {
        cout << "Give me a positive integer: ";
        cin >> a;
    } //while

    int sum = 0;
    for (int i = 1; i <= a; i++) {
        int temp = i * i;
        cout << temp << " ";
        sum += temp;
    } //for
    cout << endl << "sum to " << sum << endl;

    return 0;
} //main

Problem 415  Write a function called boeing that prints a parameter with additional digits of 7 before each
digit and at the end of the number. (So that a parameter 4 would be printed as 747 and a parameter 666 would be
printed as 7676767.)

For example, a program that uses the function boeing follows.

int main() {
    boeing(4); cout << endl; // prints 747
    boeing(66); cout << endl; // prints 76767
    boeing(7); cout << endl; // prints 777
    boeing(1000); cout << endl; // prints 717070707
    return 0;
}

Answer:

void boeing(int n) {
    if (n < 10) cout << 7 << n << 7;
    else {
        boeing(n / 10);
        cout << n % 10 << 7;
    }
}

Problem 416  Consider the following C++ program.

#include <iostream>
using namespace std;
```cpp
int recursive(int x[], int n) {
    if (n <= 0 || n > 10) return 0;
    if (n == 1) return x[0];
    if (n <= 3) return x[n - 1] + recursive(x, n - 1);
    x[0]++;
    return recursive(x, n - 3);
}

int main() {
    int x, a[10] = {1,2,3,4,5,6,7,8,9,10};
    cout << "Enter a number: ";
    cin >> x;
    cout << recursive(a, x) << endl;
    return 0;
}
```

What is the output from the program in response to the following user inputs.

(a) The user enters 0
Answer: 0
(b) The user enters 1
Answer: 1
(c) The user enters 3
Answer: 6
(d) The user enters 5
Answer: 4
(e) The user enters 10
Answer: 4

Problem 417  Write a complete C++ program that does the following.
1. It asks the user to enter positive integers a and b that are each at most 100.
2. The program reads in a table of integers with a rows and b columns as entered by the user.
3. The program determines and prints the minimum entry in each column of the table.
4. The program then prints the average value of these minimum entries.
For example, the following represents one run of the program.

Enter integers for r and c (at most 100):  2 2
Enter 2 rows of 2 integers:
    1 4
    2 0
The minimum entries in the columns are:  1 0
The average minimum entry is :  0.5

Answer:

```cpp
#include <iostream>
using namespace std;

int main () {
    int a, b, r, c, min, sumMin = 0;
    int table [100][100];

    cout << "Give me two integers, each at most 100: ";
    cin >> a >> b;
```
```cpp
cout << "Enter " << a << " rows of " << b << " integers: " << endl;
for (r = 0; r < a; r++)
  for (c = 0; c < b; c++)
    cin >> table[r][c];

cout << "The minimum entries in the columns are: ";
for (c = 0; c < b; c++) {
  min = table[0][c];
  for (r = 0; r < a; r++) if (table[r][c] < min) min = table[r][c];
  cout << min << " ";
  sumMin += min;
} // for c

cout << "\nThe average minimum entry is: ";
cout << ((double) sumMin) / b << endl;

return 0;
} //main

Problem 418 Write title lines for the functions that are called by the following main program. Do not supply the blocks for the functions.

int main() {
  string name;
  name = enterName(); // Reads a name entered by the user
  greet(name); // Says hello to the user
  cout << numberAs(name); // Finds the number of As in the name
  string theClass[20];
  enterNames(theClass, 20); // Enter the names of all students
  sort(theClass, 20, "decreasing"); // sort names into decreasing alphabetical order
  printNames(theClass, 20);
  return 0;
}

(a) Title line for enterName

string enterName()

(b) Title line for greet

void greet(string name)

(c) Title line for numberAs

int numberAs(string name)

(d) Title line for enterNames

void enterNames(string names[], int cap)

(e) Title line for sort

void sort(string names[], int cap, string ordering)

Problem 419 Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Assume that the following variables have been declared, and if necessary have values, for each part. All other necessary variables should be declared and initialized.
```
int x, y, table[100][100];
string name;

(i) Print the larger of integer variables called x and y.

    int larger = x;
    if (y > x) larger = y;
    cout << larger;

(ii) Print the numbers 10 9 8 to the file out.txt. (In this part you need to declare a variable to access the file.)

    ofstream fout ("out.txt");
    fout << 10 << 9 << 8;

(iii) Read a line of text from the user and print the word Yes if it contains the substring Freddy.

    cin >> name;
    if (name.find ("Freddy") != -1) cout << "Yes";

(iv) Print the sum of all the numbers in column number 0 of a 2-dimensional array called table. (The array table has 100 rows and 100 columns.)

    int sum = 0;
    for (int i = 0; i < 100; i++)
        sum += table [i][0];
    cout << sum;

(v) Print 8 random negative integers to the screen. (The random integers should be determined by using an appropriate C++ function.)

    for (int i = 0; i < 8; i++) {
        int num = rand ();
        if (num > 0) num *= -1;
        cout << num << endl;
    } //for

Problem 420 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter a positive integer.
2. The program reads a value n entered by the user. If the value is not legal, the program repeatedly makes the user type in another value until a legal value of n has been entered.
3. The program prints an n × (2n − 1) pattern of * symbols in the shape of a large triangle.
For example, if the user enters 4 for n the program should print the following picture.

    *
    * *
    * * *
    *********

Answer:

#include <iostream>
using namespace std;

int main() {
    int c, r, n;
cout << "Enter a positive integer: ";
cin >> n;
while (n <= 0) {
    cout << "Illegal. Try again: ";
cin >> n;
}
for (r = n; r >= 1; r--) {
    for (c = 1; c <= 2 * n - 1; c++)
        if (r == 1 || c == r || c + r == 2 * n) cout << "*";
    else cout << " ",
    cout << endl;
} return 0;

Problem 421    Write a function called oddDigits that determines the number of odd digits in an integer parameter. For example, a program that uses the function oddDigits follows. (In this example, the number 10 has one odd digit namely 1; the number 26 has no odd digits; the number 19683 has three odd digits namely 1, 9 and 3.)

int main() {
    cout << oddDigits(10) << endl;   // prints 1
    cout << oddDigits(26) << endl;   // prints 0
    cout << oddDigits(19683) << endl; // prints 3
    return 0;
}

Answer:

int oddDigits(int x) {
    if (x == 0) return 0;
    return oddDigits(x/10) + x % 2;
}

Problem 422    For each of the following short segments of a program write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)    int x = 4, y = 5;
    if (x <= y && y <= x) cout << "Yes";
    else cout << "No";

Answer:

No

(ii)    int x = 4, y = 5;
    cout << (x / y + 1.0) << endl;

Answer:

1

(iii)    for (int i = 1; i <= 10; i++) {
        cout << i << endl;
        i++;
    }
(iv)

```cpp
int x[3][3] = {{1,3,5}, {2,4,6}, {7,8,9}};
for (int i = 0; i <= 2; i++) for (int j = 0; j <= 2; j++)
    if (i == j) cout << x[i][j];
```

Answer:

149

(v)

```cpp
int x[3][3] = {{1,3,5}, {2,4,6}, {7,8,9}};
for (int j = 0; j <= 2; j++) for (int i = 0; i <= 2; i++)
    cout << x[i][j];
    cout << endl;
```

Answer:

127348569

Problem 423  Write a complete C++ program that does the following.
1. It asks the user to enter positive integers a and b that are each at most 20.
2. The program generates random integer values between 1 and 6 as the entries in a table with a rows and b columns.
3. The program then prints the table.
4. The program prints a picture with a rows and b columns. The character printed in row i and column j is X or O according as the entry of the table in row i and column j is even or odd.

For example, the following represents one run of the program.

Enter integers for r and c (at most 20):  2 2
The table has been generated as: 
6 3
1 3
The picture is: 
XO
OO

Answer:

```cpp
#include <iostream>
using namespace std;

int main ()
{
    int a, b;
    int table [20][20];

    cout << "Give me two integers, each at most 20: ";
    cin >> a >> b;
```
for (int r = 0; r < a; r++)
    for (int c = 0; c < b; c++)
        table [r][c] = rand () % 6 + 1;

cout << "The table has been generated as:" << endl;
for (int r = 0; r < a; r++)
{
    for (int c = 0; c < b; c++)
        cout << table [r][c] << " ";
    cout << endl;
} //for

cout << "The picture is:" << endl;
for (int r = 0; r < a; r++)
{
    for (int c = 0; c < b; c++)
        if (table [r][c] % 2 == 0) cout << "X";
        else cout << "O";
    cout << endl;
} //for

return 0;
} //main

Problem 424      Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Include declarations for any variable that you use.

(i) Print the word output to the file out.txt.
Answer:
    ofstream out("out.txt");
    out << "output";

(ii) Print a random negative integer to the screen. (The random integer should be determined by using an appropriate C++ function.)
Answer:
    int r = rand();
    while (r == 0) r = rand();
    if (r > 0) r = -r;
    cout << r;

(iii) Read a line of text from the user and print the word Yes if it contains at most 7 characters.
Answer:
    string line;
    getline(cin, line);
    if (line.length() <= 7) cout << "Yes";

(iv) Print the last but one character of the string s.
Answer:
    cout << s[s.length() - 2];

(v) Print the average of integer variables called x and y.
Answer:
    cout << (x + y) / 2.0;
Problem 425  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter a positive integer.
2. The program reads a value \( n \) entered by the user. If the value is not legal, the program repeatedly makes the user type in another value until a legal value of \( n \) has been entered.
3. The program prints an \( n \times (2n - 1) \) pattern of * symbols in the shape of a large upside down triangle.

For example, if the user enters 4 for \( n \) the program should print the following picture.

```
*******  
  * *     
  * *     
   *       
```

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int c, r, n;
    cout << "Enter a positive integer: ";
    cin >> n;
    while (n <= 0) {
        cout << "Illegal. Try again: ";
        cin >> n;
    }
    for (r = 1; r <= n; r++) {
        for (c = 1; c <= 2 * n - 1; c++)
            if (r == 1 || c == r || c + r == 2 * n) cout << "*";
            else cout << " ";
        cout << endl;
    }
    return 0;
}
```

Problem 426  Write a function called \texttt{reverse} that reverses the entries in an array.

For example, a program that uses the function \texttt{reverse} follows.

```cpp
int main() {
    int a[5] = {3, 1, 4, 1, 5};
    reverse(a, 5);
    return 0;
}
```

Answer:

```cpp
void reverse(int a[], int cap) {
    for (int i = 0; i < cap / 2; i++) {
        int temp = a[i];
        a[i] = a[cap - 1 - i];
        a[cap - 1 - i] = temp;
    }
}
```
Problem 427  Write a complete C++ program that does the following.
1. It asks the user to enter positive integers \( r \) and \( c \) that are at most 100.
2. The program reads in a table of integers with \( r \) rows and \( c \) columns as entered by the user.
3. The program prints out all values of an integer \( x \) for which the entries in row \( x \) have a sum of 7.
For example, the following represents one run of the program.

Enter integers for \( r \) and \( c \) (at most 100): 3 2
Enter 3 rows of 2 integers:
3 4
1 0
8 -1
The following rows add to 7: 0 2

Answer:

```cpp
#include <iostream>
using namespace std;

int main ()
{
    int table[100][100], r, c;
    cout << "Enter integers for \( r \) and \( c \) (at most 100): ";
    cin >> r >> c;

    cout << "Enter \( r \) rows of \( c \) integers: ";
    for (int i = 0; i < r; i++)
    for (int j = 0; j < c; j++)
        cin >> table[i][j];

    cout << "The following rows add to 7: ";
    for (int x = 0; x < r; x++)
    {
        int rowS = 0;
        for (int i = 0; i < c; i++) rowS += table[x][i];
        if (rowS == 7) cout << x << " ";
    } //for

    cout << endl << endl;
    return 0;
} //main
```

Problem 428  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

string recursive(string s) {
    if (s.length() < 3) return s;
    if (s.length() < 5) return "a";
    return recursive(s.substr(3));
}

int main() {
    string x;
    cout << "Enter a string: ";
```
What is the output from the program in response to the following user inputs.
(a) The user enters Hi
   Answer:
   Hi

(b) The user enters Hello
   Answer:
   lo

(c) The user enters Goodbye
   Answer:
   a

(d) The user enters 12345678
   Answer:
   78

(e) The user enters 1234 5678
   Answer:
   a

Problem 429 Suppose that a C++ program called prog.cpp is compiled and correctly executed on venus with the instructions:

venus> g++ prog.cpp
venus> a.out input1.txt input2 out.txt

For each of the following short segments of the program prog.cpp write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.

(i)
```cpp
int x = 4, y = 5;
cout << ++x + y--;
```
Answer:
10

(ii)
```cpp
int main(int argc, char *argv[]) {
cout << argv[1];
```
Answer:
input1.txt

(iii)
for (int i = 2; i >= 0; i--) {
    for (int j = 0; j < i; j++) cout << "*";
    cout << endl;
}

Answer:
**
*

(iv)

int c = 4, d = 5;
c = d;
d = c;
cout << c << " " << d;

Answer:
5 5

(v)

for (int i = 2; i >= 0; i--) {
    for (int j = 0; j < i; j++) cout << "*";
    cout << endl;
}

Answer:
***

Problem 430  Write title lines (header lines or prototypes) for the following functions. Do not supply the blocks for the functions.
(a) A function called firstChar which returns the first character of a string.
Answer:
char firstChar(string s)

(b) A function called power that returns an integer power of a double precision decimal number.
Answer:
double power(double x, int n)

(c) A function called As which returns the number of times the letter A appears in a string.
Answer:
int As(string s)

(d) A function called randomEven which is to create and return a random even number.
Answer:
int randomEven()

(e) A function called inOrder which is to determine whether an array of strings is in alphabetical order.
Answer:
bool inOrder(string s[], int cap)
**Problem 431**  Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter a positive integer.
2. The program reads a value \( n \) entered by the user. If the value is not legal, the program repeatedly makes the user type in another value until a legal value of \( n \) has been entered.
3. The program prints an \( n \times (2n - 1) \) pattern of * symbols in the shape of a large letter V.

For example, if the user enters 4 for \( n \) the program should print the following picture.

```
*   *
*   *
* *
*
```

**Answer:**

```cpp
#include <iostream>
using namespace std;

int main() {
    int c, r, n;
    cout << "Enter a positive integer: ";
    cin >> n;
    while (n <= 0) {
        cout << "Illegal. Try again: ";
        cin >> n;
    }
    for (r = 1; r <= n; r++) {
        for (c = 1; c <= 2 * n - 1; c++)
            if (c == r || c + r == 2 * n) cout << "*";
            else cout << " ";
        cout << endl;
    }
    return 0;
}
```

**Problem 432**  Write a function called `sort` that sorts three integer parameters into decreasing order.

For example, a program that uses the function `sort` follows.

```cpp
int main() {  
    int a = 2, b = 7, c = 1;
    sort(a, b, c);
    cout << a << b << c << endl;  // prints 721
    return 0;
}
```

**Answer:**

```cpp
void swap(int &a, int &b) {
    int temp = a;
    a = b;
    b = temp;
}

void order(int &a, int &b) {
    if (a < b) swap(a, b);
}
```
Problem 433  
Write a complete C++ program that does the following:
1. It asks the user to enter positive integers \( r \) and \( c \) that are at most 100.
2. The program reads in a table of integers with \( r \) rows and \( c \) columns as entered by the user.
3. The program prints out all values of an integer \( x \) for which row \( x \) and column \( x \) of the table have the same sum.
For example, the following represents one run of the program.

Enter integers for \( r \) and \( c \) (at most 100): 3 2
Enter 3 rows of 2 integers:
 3 2
 1 0
 1 1
The row and column sums are equal at 0.
(Notethe program prints 0 because row 0 sums to 3 + 2 = 5 and column 0 sums to 3 + 1 + 1 = 5.)
Answer:

```cpp
#include <iostream>
using namespace std;

int main ()
{
    int table[100][100], r, c;
    cout << "Enter integers for \( r \) and \( c \) (at most 100): ";
    cin >> r >> c;
    cout << "Enter \( r \) rows of \( c \) integers: \n";
    for (int i = 0; i < r; i++)
        for (int j = 0; j < c; j++)
            cin >> table[i][j];
    for (int x = 0; x < r && x < c; x++)
    {
        int rowS = 0, colS = 0;
        for (int i = 0; i < c; i++)
            rowS += table[x][i];
        for (int i = 0; i < r; i++)
            colS += table[i][x];
        if (rowS == colS)
            cout << "The row and column sums are equal at \( x \): " << x << endl;
    }
    return 0;
}
```

Problem 434  
Consider the following C++ program.

```cpp
#include <iostream>
```
using namespace std;

string recursive(string s) {
    if (s.length() < 3) return s;
    if (s.length() < 6) return "a";
    return recursive(s.substr(4));
}

int main() {
    string x;
    cout << "Enter a string: ";
    cin >> x;
    cout << recursive(x) << endl;
    return 0;
}

What is the output from the program in response to the following user inputs.
(a) The user enters Hi
Answer:
Hi

(b) The user enters 5
Answer:
5

(c) The user enters five
Answer:
a

(d) The user enters string
Answer:
ng

(e) The user enters recursive
Answer:
a

Problem 435  Suppose that a C++ program called prog.cpp is compiled and correctly executed on venus with the instructions:

venus> g++ prog.cpp
venus> a.out input1.txt input2 out.txt

For each of the following short segments of the program prog.cpp write exactly what output is produced. Each answer should consist of those symbols printed by the given part of the program and nothing else.
(i)

    int x = 4, y = 5;
    if (x < y || y < x) cout << "Yes";
    else cout << "No";

Answer:
Yes

(ii)

int main(int argc, char *argv[]) {
    cout << argc;
    
    Answer:
    4

(iii)

    for (int i = 2; i < 0; i--) {
        for (int j = 0; j < i; j++) cout << ";
        cout << endl;
    }
    
    Answer:

(iv)

    int c = 4, d = 5;
    if (++c < d) cout << ":
    else cout << ":
    
    Answer:
    No

(v)

    string s = "Hello";
    for (int i = s.length(); i > 0; i--) {
        for (int j = 0; j < i; j++) cout << (char) s[j];
        cout << endl;
    }
    
    Answer:
    Hello
    Hell
    Hel
    He
    H

Problem 436    Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter a positive integer $n$.
2. It repeatedly reads $n$ from the user until the supplied value of $n$ is positive.
3. It prints out a large letter $X$ that has height $n$ and width $n$. The locations of the printed characters should lie on the diagonals of the $n \times n$ square region that the letter occupies.
Here is an example of how the program should work:

Give me a positive integer: 7
X   X
X   X
X   X
    X
    X
    X
    X
    X
    X
    X
    X
Problem 437  Write C++ statements to carry out the following tasks.
Do not write complete programs, just give a single line, or a few lines of C++ instructions. Assume that the following variables have been declared, and if necessary have values, for each part:

```
string f, l;
```

Declare any other variables that you use.

(i) Write the strings `f` and `l` as the first two lines of the file `data.txt`.

**Answer:**
```
ofstream out("data.txt");
out << f << endl << l << endl;
```

(ii) Print the message `Hello Freddy` if the input file `input.txt` begins with the string `Freddy`. Otherwise do nothing.

**Answer:**
```
ifstream file("input.txt");
file >> f;
if (f == "Freddy") cout << "Hello Freddy" << endl;
```

(iii) Convert the string `f` to upper case letters and then print it.

**Answer:**
```
for (int i = 0; i < f.size(); i++)
    f[i] = toupper(f[i]);
cout << f << endl;
```

(iv) Print the number of times that the uppercase letter `F` appears in the string `f`.

**Answer:**
```
int count = 0;
for (int i = 0; i < f.size(); i++)
    if (f[i] == 'F') count++;
cout << count << endl;
```
(v) Swap the strings stored in the variables $f$ and $l$.

Answer:

```cpp
string temp = f;
f = l;
l = temp;
```

**Problem 438**  
Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

int main(){
    int i;
    string words[4] = {"zero", "one", "two", "three"};

    for (i = 1; i <= 4; i++) cout << words[4 - i] << " ";  // line A
    cout << endl;
    i = 0;
    while( i + 1 < 4){ cout << words[i+1] << " "; i++; }  // line B
    cout << endl;

    for(i = 0; i < words[1].length(); i++) cout << (words[i])[0];  // line C
    cout << endl;
    return 0;
}
```

(a) What is the output from the loop at line A?

Answer:

three two one zero

(b) What is the output from the loop at line B?

Answer:

one two three

(c) What is the output from the loop at line C?

Answer:

zot

**Problem 439**  
Write a function called `thirdDigit`. The function has an integer parameter and returns the third digit in its parameter. If the parameter is less than 100 the function returns 0 because there is no third digit.

For example, a program that uses the function follows.

```cpp
int main() {
    cout << thirdDigit(777) << " " << thirdDigit(2048) << " " << thirdDigit(500125) << endl;
    return 0;
}
```

It should print: 7 4 0

Answer:
int thirdDigit(int x) {
  if (x < 100) return 0;
  if (x < 1000) return x % 10;
  return thirdDigit(x/10);
}

Problem 440 Write a function called sixCount that returns a count of the number of entries that are equal to 6 in a 2-dimensional array with 6 columns. The function should use a parameter to specify the array and parameters for the row count and column count.
For example, a program that uses the function sixCount follows.

```cpp
int main() {
  int arr[2][6] = {{6,4,3,1,2,2}, {6,6,5,2,3,6}}; // array has 4 entries of 6
  cout << sixCount(arr, 2, 6) << endl; // prints 4
  return 0;
}
```

Answer:

```cpp
int sixCount(int a[][6], int r, int c) {
  int count = 0;
  for (int i = 0; i < r; i++)
    for (int j = 0; j < c; j++)
      if (a[i][j] == 6) count++;
  return count;
}
```

Problem 441 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter a positive integer n.
2. If n is not positive, it prints an error message and exits.
3. Otherwise it calculates and prints the product of the digits of n.

Here is an example of how the program should work:

Enter a positive integer n: 373
The product of its digits is 63

In this example the product is $3 \times 7 \times 3$ which is 63.

Answer:

```cpp
#include <iostream>
using namespace std;

int product(int x) {
  if (x < 10) return x;
  return (x % 10) * product(x/10);
}

int main() {
  int n;
  cout << "Enter a positive integer: ";
  cin >> n;
  if (n <= 0) {
```
Problem 442  Write a complete C++ program that does the following.
1. It asks the user to enter a positive integer \( n \).
2. It reads \( n \) from the user and exits if \( n \) is not positive.
3. It prints out an \( n \times n \) checkerboard pattern made from the characters \( X \) and \( O \).
Here is an example of how the program should work:

Give me a positive integer: 3
XOX
OXO
XOX

In a checkerboard pattern, the horizontal and vertical neighbors of each \( X \) are \( O \)s, and the horizontal and vertical neighbors of each \( O \) are \( X \)s.

Answer:

```c++
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me a positive integer: ";
    cin >> n;
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++)
            if (((i + j) % 2) == 0) cout << "X";
            else cout << "O";
        cout << endl;
    }
    return 0;
}
```

Problem 443  Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Assume that the following variables have been declared, and if necessary have values, for each part:

```c++
string f, l, name;
```

Declare any other variables that you use.

(i) From the input file `data.txt`, read a first name to \( f \) and a last name to \( l \).

Answer:

```c++
ifstream file("data.txt");
file >> f >> l;
```

(ii) Print the second character in \( f \) to an output file `output.txt`.

Answer:
ofstream out("output.txt");
out << f[1] << endl;

(iii) Convert the string $f$ to lower case letters and then print it.

**Answer:**

```c++
for (int i = 0; i < f.size(); i++)
    f[i] = tolower(f[i]);
cout << f << endl;
```

(iv) Check whether the string $f$ contains the letters *Fred* as a substring. If it does, print the message *Hello Freddy*. Otherwise do nothing.

**Answer:**

```c++
if (f.find("Fred") >= 0)
    cout << "Hello Freddy" << endl;
```

(v) Concatenate the strings $f$ and $l$ separated by a space into the string *name*.

**Answer:**

```c++
name = f + " " + l;
```

**Problem 444**  
Consider the following C++ program.

```c++
#include <iostream>
using namespace std;

void mystery(int x[][4], int a, int b, int k) {
    for (int r = 0; r <= a; r++) for (int c = 0; c <= b; c++)
        x[r][c] = k;
}

void print(int x[][4], int s) {
    for (int r = 0; r < s; r++) {
        for (int c = 0; c < s; c++) cout << x[r][c];
        cout << endl;
    }
}

int main() {
    int x[4][4];
    mystery(x, 3, 3, 0); print(x, 4);
    mystery(x, 1, 2, 1); print(x, 4);
    mystery(x, 3, 1, 2); print(x, 3);
    mystery(x, 3, 2, 3); print(x, 1);
    return 0;
}
```

(a) What is the output from the first call to the function print?

**Answer:**

```
0000
0000
0000
0000
```
Problem 445 Write header lines (prototypes) for the following functions. Do not attempt to supply the blocks for the functions.
(a) A function called lastChar which uses a string as input and returns the last character in the string.
Answer:

char lastChar(string x)

(b) A function called isSquare that tests whether an integer is a perfect square. (For example, 16 is a perfect square, but -5 is not.)
Answer:

bool isSquare(int x)

(c) A function called addTwo which uses as input an array of integers. The task of the function is to add 2 to every element in the array.
Answer:

void addTwo(int a[], int capacity)

(d) A function called exchangeArrays which uses two arrays of integers that have the same capacity and exchanges the entries between them.
Answer:

void exchangeArrays(int a[], int b[], int capacity)

(e) A function called exchange which exchanges the values of two integers.
Answer:

void exchange(int &x, int &y)

Problem 446 Write a function called sevenUp. The function has an integer parameter and calculates an answer by turning any digit equal to 7 in the input to an 8.
For example, a program that uses the function follows.
int main() {
    cout << sevenUp(777) << " " << sevenUp(471) << " " << sevenUp(50) << endl;
    return 0;
}

It should print: 888 481 50

Answer:

int sevenUp(int x) {
    if (x == 7) return 8;
    if (x < 10) return x;
    return 10*sevenUp(x / 10) + sevenUp(x % 10);
}

Problem 447

Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter 9 integers as the entries of a 3 × 3 table.
2. The program reads the 9 entries, row by row and prints the table.
3. If every row and column of the table have the same sum then the program adds the message: *MAGIC*.

Here is an example of how the program should work:

Enter 9 entries of a 3 x 3 table: 10 14 18 15 16 11 17 12 13

10 14 18
15 16 11
17 12 13

MAGIC

This example is magic because each row and each column has a sum of 42.

Answer:

#include <iostream>
using namespace std;

int main() {
    int table[3][3];
    cout << "Enter 9 entries of a 3 x 3 table: ";

    int r, c;
    for (r = 0; r < 3; r++) for (c = 0; c < 3; c++)
        cin >> table[r][c];

    for (r = 0; r < 3; r++) {
        cout << endl;
        for (c = 0; c < 3; c++) cout << table[r][c] << " ";
    }
    cout << endl;

    int sum = table[0][0] + table[0][1] + table[0][2];
    bool isMagic = true;
    for (int i = 0; i < 3; i++) {
        int rowSum = 0, colSum = 0;
        for (int j = 0; j < 3; j++)
            rowSum += table[i][j];

            if (rowSum != sum) { isMagic = false; break; }
        }

        for (int j = 0; j < 3; j++)
            colSum += table[i][j];

        if (colSum != sum) { isMagic = false; break; }
    }

    if (isMagic) cout << "MAGIC"; // Check if the table is magic

    return 0;
}
Problem 448  Write a complete C++ program that does the following.
1. It asks the user to enter some positive integers.
2. It reads positive integers from the user.
3. As soon as the user enters a non-positive integer, the program stops reading.
4. The program reports the sum of all the positive numbers that it read.
Here is an example of how the program should work:

Give me some positive integers:  1 12 1 100 -1000
sum: 114

Answer:

```cpp
#include <iostream>
using namespace std;

int main() {
    int sum = 0;
    int n = 1;
    cout << "Give me some positive integers: ";
    while (n > 0) {
        cin >> n;
        if (n > 0) sum += n;
    }
    cout << "sum: " << sum << endl;
    return 0;
}
```

Problem 449  Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Assume that the following variables have been declared, and if necessary have values, for each part:

```
string f, l;
```

(i) Read a first name to \( f \) and a last name to \( l \). Then, print out the string \( f \) followed by the string \( l \) on another line.

Answer:

```
cin >> f >> l;
cout << f << " " << l << endl;
```

(ii) Print the second character in \( f \).

Answer:

```
cout << f[1];
```

(iii) Convert the string \( f \) to upper case letters and then print it.

Answer:
for (int i = 0; i < f.size(); i++) f[i] = toupper(f[i]);
cout << f;

(iv) Read a word into f from a user. If the program can find the smaller string ”reddy” within the string f, print the word ”Hello”, otherwise do nothing.

Answer:

cin >> f;
if (f.find("reddy") >= 0) cout << "Hello";

(v) Print the last character of l.

Answer:

cout << l[l.size() - 1];

Problem 450  Consider the following C++ program.

#include <iostream>
using namespace std;

void mystery(char x[][4], int a, int b, char k) {
    for (int r = a; r <= b; r++) for (int c = a; c <= b; c++)
        x[r][c] = k;
}

void print(char x[][4], int s) {
    for (int r = 0; r < s; r++) {
        for (int c = 0; c < s; c++) cout << x[r][c];
        cout << endl;
    }
    cout << endl;
}

int main() {
    char x[4][4];
    mystery(x, 0, 3, 'X'); print(x, 4);
    mystery(x, 1, 2, 'Y'); print(x, 4);
    mystery(x, 2, 3, 'Z'); print(x, 4);
    mystery(x, 3, 2, '0'); print(x, 4);
    return 0;
}

(a) What is the output from the first call to the function print?

Answer:

XXXX
XXXX
XXXX
XXXX

(b) What is the output from the second call to the function print?

Answer:

XXXX
XYYX
XYYX
XXXX
(c) What is the output from the third call to the function print?

Answer:

XXX
XYYX
XYZZ
XXZZ

(d) What is the output from the fourth call to the function print?

Answer:

XXX
XYYX
XYZZ
XXZZ

Problem 451  Write header lines (prototypes) for the following functions. Do not attempt to supply the blocks for the functions.

(a) A function called isPrime that tests whether an integer is prime. (For example, 7 is prime, but 9 is not.)

Answer:

bool isPrime(int x)

(b) A function called firstChar which uses a string as input and returns the first character in the string.

Answer:

char firstChar(string x)

(c) A function called printThree which uses as input an array of integers. The task of the function is to print the first three elements of the array.

Answer:

void printThree(int x[])

(d) A function called printChess which uses as input an $8 \times 8$ array of characters that represents a chess board. The task of the function is to print the board to output.

Answer:

void printChess(char x[][8], int r, int c)

(e) A function called reverseWord which is to use a string parameter and change it to become the string obtained by reversing its letters. (For example, an input string was would be changed to saw.)

Answer:

void reverseWord(string &x)

Problem 452  Write a function called biggestEntry that uses a two dimensional array (with 3 columns) with integer entries as its first parameter. It also uses parameters representing the row and column capacities. The function should return the value of the biggest entry in the array.

For example, a program that uses the function follows.

```c
int main() {
    int x[2][3] = {{1,2,3},{4,7,3}};
    cout << biggestEntry(x, 2, 3) << endl;
    return 0;
}
```
It should print 7 (since 7 is the biggest entry in the array).

Answer:

```cpp
int biggestEntry(int a[][3], int r, int c) {
    int answer = a[0][0];
    for (int i = 0; i < r; i++) for (int j = 0; j < c; j++)
        if (a[i][j] > answer) answer = a[i][j];
    return answer;
}
```

Problem 453 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter a positive integer value, n.
2. The program reads a value entered by the user. If n is not positive, the program should exit.
3. It prints out the number of digits in n.
4. It prints the number digits in the binary representation of n.

Here is an example of how the program should work:

Enter a positive integer n: 17
Digits in n: 2
Binary digits in n: 5

The number of binary digits is 5 because the binary representation of 17 is 10001. However, it is not necessary for your program to determine this binary representation.

Answer:

```cpp
#include <iostream>
using namespace std;

int length(int x, int base) {
    if (x < base) return 1;
    return 1 + length(x / base, base);
}

int main() {
    int n;
    cout << "Enter a positive integer n: ";
    cin >> n;
    if (n <= 0) exit(1);
    cout << "Digits in n: " << length(n, 10) << endl;
    cout << "Binary digits in n: " << length(n, 2) << endl;
    return 0;
}
```

Problem 454 Write a complete C++ program that does the following.
1. It asks the user to enter 5 single digit positive integers.
2. If any number is out of range, it says: "That is too hard."
3. Otherwise it adds the numbers and prints their sum.

Here is an example of how the program should work:

Give me 5 single digit positive integers: 9 9 9 6 9
42

Answer:
```cpp
#include <iostream>
using namespace std;

int main() {
    int answer = 0, x;
    cout << "Give me 5 single digit positive integers: ";
    for (int i = 1; i <= 5; i++) {
        cin >> x;
        if (x <= 0 || x >= 10) {
            cout << "That is too hard."
                 << endl;
            exit(0);
        }
        answer += x;
    }
    cout << answer << endl;
    return 0;
}
```

**Problem 455** Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Assume that the following variables have been declared, and if necessary have values, for each part:

(i) Read a user’s first name to \( f \) and their last name to \( l \).

**Answer:**

```cpp
cin >> f >> l;
```

(ii) Print out the string \( f \) followed by the string \( l \) with a space between them.

**Answer:**

```cpp
cout << f << " " << l;
```

(iii) Set \( x \) to be \( 1 - 2 + 3 - 4 + 5 - \ldots + 999 \). The formula involves all integers from 1 to 999. Odd numbers are added, even numbers subtracted.

**Answer:**

```cpp
x = 0;
for (int i = 1; i < 1000; i++)
    if (i % 2 == 0) x -= i;
    else x += i;
```

(iv) Repeatedly double \( x \), until the value of \( x \) exceeds 1024.

**Answer:**

```cpp
while (x <= 1024) x *= 2;
```

(v) Read a word into \( f \) from a user. If the word is "Freddy", print output saying "Hello", otherwise do nothing.

**Answer:**

```cpp
cin >> f;
if (f == "Freddy") cout << "Hello" << endl;
```

**Problem 456** Consider the following C++ program.
```cpp
#include <iostream>
using namespace std;

void mystery(string array[], int p[], int q) {
    if (q < 0) cout << "Help!" << endl;
    else if (q <= 2) cout << p[q] << endl;
    if (q > 2) {
        for (int i = 0; i <= q; i++) cout << array[p[i]] << " ";
        cout << endl;
    }
}

int main() {
    string x[5] = {"This", "is", "a", "dumb", "question"};
    int a[10] = {0, 4, 1, 3, 3, 3, 2, 2, 2, 2};
    mystery(x, a, -10);
    mystery(x, a, 0);
    mystery(x, a, 1);
    mystery(x, a, 3);
    mystery(x, a, 5);
    return 0;
}
```

(a) What is the output from the first call to the function `mystery`?  
Answer:  
Help!

(b) What is the output from the second call to the function `mystery`?  
Answer:  
0

(c) What is the output from the third call to the function `mystery`?  
Answer:  
4

(d) What is the output from the fourth call to the function `mystery`?  
Answer:  
This question is dumb

(e) What is the output from the fifth call to the function `mystery`?  
Answer:  
This question is dumb dumb dumb

**Problem 457** Write header lines (prototypes) for the following functions. **Do not attempt to supply the blocks for the functions.**

(a) A function called `isLeapYear` that tests whether an integer represents a leap year. (For example, 2008 is a leap year, but 2007 is not.)

Answer:

```cpp
bool isLeapYear(int y)
```

(b) A function called `temperatureDifference` which uses as input two double precision values that represent the temperature in New York measured in degrees Fahrenheit and the temperature in Paris measured in degrees Celsius. The function is to calculate and return the difference between the temperatures in degrees Fahrenheit.

Answer:
double temperatureDifference(double n, double p)

(c) A function called **addCurve** which uses as input an array of integer test scores. The task of the function is to add 10 to every score in the array.

**Answer:**

```c
void addCurve(int s[], int capacity)
```

(d) A function called **printTicTacToe** which uses as input a $3 \times 3$ array of characters that represents a Tic-Tac-Toe game. The task of the function is to print the board to output.

**Answer:**

```c
void printTicTacToe(char [][])
```

(e) A function called **reverseDigits** which is to use an integer parameter and return the integer obtained by reversing the digits in the parameter.

**Answer:**

```c
int reverseDigits(int x)
```

**Problem 458** Write a function called **biggestDigit** that uses an integer input parameter and returns the largest digit in the input. The input should be assumed to be positive.

For example, a program that uses the function follows.

```c
int main() {
    cout << biggestDigit(1760) << endl;
    return 0;
}
```

It should print 7 (since 7 is the biggest digit in 1760).

A little extra credit will be given for good recursive solutions.

**Answer:**

```c
int biggestDigit(int x) {
    if (x < 10) return x;
    int b = biggestDigit(x/10);
    if (x % 10 > b) return x % 10;
    return b;
}
```

**Problem 459** Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter a positive integer value, $n$ that is at most 100.
2. The program reads a value entered by the user. If $n$ is not positive, or $n$ is greater than 100, the program should exit.
3. It prints out all numbers between 1 and 1000 for which the sum of the digits is exactly $n$.

For example, if the user chooses 13 for $n$, the program should print out 49 because $4 + 9 = 13$. It would also print 58, 67, and other numbers with the same digit sum. It would not print 48 or 50.

(Suggestion: It might be convenient to write a function called *digitSum*.)

**Answer:**

```c
#include <iostream>
using namespace std;

int digitSum(int x) {
```
if (x < 10) return x;
return x % 10 + digitSum(x/10);
}

int main() {
    int n;
    cout << "Enter a value of n that is at most 100:";
    cin >> n;
    if (n <= 0 || n > 100) exit(0);

    for (int x = 1; x <= 1000; x++)
        if (digitSum(x) == n) cout << x << " ";
    cout << endl;
    return 0;
}

Problem 460 Write a complete C++ program that does the following.
1. It asks the user to enter a (single) first name.
2. The program stores the name, but if it is "Freddy", the program changes it to "you".
3. The program says hello to the user, using their name (or changed version).

Here is an example of how the program should work:

Who are you? Max
Hello Max.

Answer:

#include <iostream>
using namespace std;

int main() {
    string name;
    cout << "Who are you? ";
    cin >> name;
    if (name == "Freddy") name = "you";
    cout << "Hello " << name << "." << endl;
    return 0;
}

Problem 461 Write C++ statements to carry out the following tasks. Do not write complete programs, just give a single line, or a few lines of C++ instructions. Assume that the following variables have been declared, and if necessary have values, for each part:

int x;
string s;

(i) Read a user's first name to s and their age to x.

Answer:

cout << "Enter your name and age: ";
cin >> s >> x;

(ii) Print out the number of characters in the string s.

Answer:

cout << s.size();
(iii) Set \( x \) to be \( 1^3 + 2^3 + \ldots + 71^3 \), the sum of the cubes of the numbers from 1 to 71.

**Answer:**

\[
x = 0;
for \ ( \text{int} \ i = 1; \ i <= 71; \ i++)
\quad x += i \times i \times i;
\]

(iv) Repeatedly generate and add a random value between 1 and 6 to \( x \), until the value of \( x \) exceeds 100.

**Answer:**

\[
x = 0;
while \ (x <= 100)
\quad x += (\text{rand()} \ % \ 6 \ + \ 1);
\]

(v) Read a complete line of text into \( s \) from a user. If their text includes a substring "Queens", print output saying "College", otherwise do nothing.

**Answer:**

```cpp
getcin, s);
if (s.find("Queens", 0) >= 0) cout << "College";
```

**Problem 462**  
Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

void mystery(int &p, int q) {
    int temp = p;
    p = q;
    q = temp;
}

int main() {
    int p, q;
    for (p = 0; p < 5; p++) cout << p; cout << endl;
    for (q = 0; q < 5; ++q) cout << q;
    cout << endl;
    for (p = 3; p < 6; p++)
        for (q = 1; q <= 3; q++)
            cout << p - q;
    cout << endl;
    p = 4; q = 14;
mystery(q, p);
cout << p << " " << q << endl;
    p = 4; q = 14;
cout << ++p - q-- << endl;
return 0;
}
```

What is the output from the program?

**Answer:**

01234
01234
210321432
4 4
-9
Write header lines (prototypes) for the following functions. Do not attempt to supply the blocks for the functions.

(a) A function called `numberDigits` that is to return the number of digits of an integer.

   Answer:
   
   ```cpp
   int numberDigits(int x)
   ```

(b) A function called `differenceMax` which is to return the difference between the maximum entries in two arrays of integers. (Do not assume that the arrays have the same capacities.)

   Answer:
   
   ```cpp
   int differenceMax(int a[], int capA, int b[], int capB)
   ```

(c) A function called `swap` which is used to swap two values of type double.

   Answer:
   
   ```cpp
   void swap(double &x, double &y)
   ```

(d) A function called `firstCharacter` which is to return the first character in a string.

   Answer:
   
   ```cpp
   char firstCharacter(string s)
   ```

(e) A function called `median` which is to return the median (middle valued) entry in an array that holds an odd number of integer entries.

   Answer:
   
   ```cpp
   int median(int a[], int cap)
   ```

Problem 464  
Write a function called `plusTax` that uses parameters that specify a price (in cents) and a tax rate (as a percentage). The function calculates the amount of tax, rounded to the nearest cent. (Half cents must round up.) It adds the tax to the price and returns the result.

For example, a program that uses the function follows.

```cpp
int main() {
    int cost = 100;  // cost is 100 cents
    double taxRate = 4.8;  // tax is at 4.8 percent
    cout << "With tax that is \"" << plusTax(cost, taxRate) << " cents.\"" << endl;
    return 0;
}
```

It should find a tax of 4.8 cents, round up to 5 cents and print:

```
With tax that is 105 cents.
```

Answer:

```cpp
int plusTax(int price, double rate) {
    double tax = price * rate / 100;
    int rounded = (int) (tax + 0.5);
    return price + rounded;
}
```

Problem 465  
Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter a positive integer value, \( n \) that is at most 100.
2. The program reads a value entered by the user. If \( n \) is not positive, or \( n \) is greater than 100, the program should exit.
3. The program reads \( n \) integers from the user and then prints their last digits in reverse order of input.

For example, a run of the program might be as follows:
What is n? 7
Enter 7 numbers: 143 259 63 17 12 8 9
9 8 2 7 3 9 3

Answer:

#include <iostream>
using namespace std;

int main() {
  int i, n;
  int numbers[100];
  cout << "What is n? ";
  cin >> n;
  if (n <= 0 || n > 100) exit(1);

  cout << "Enter " << n << " numbers: ";
  for (i = 0; i < n; i++) cin >> numbers[i];
  for (i = n - 1; i >= 0; i--) cout << numbers[i] % 10 << " ";
  cout << endl;
  return 0;
}

Problem 466  Write a complete C++ program that first asks a user to do a simple math problem of your choosing. The user enters an answer and the program grades it as right or wrong. For example the program might ask about 6 \times 9 and respond to an incorrect answer of 42 as follows:

What is 6 x 9?
  42
Wrong!

Your program can always ask the same question. Answer:

#include <iostream>
using namespace std;

int main() {
  int x;
  cout << "What is 6 x 9? ";
  cin >> x;
  if (x != 54) cout << "Wrong! " << endl;
  else cout << "Right! " << endl;
}

Problem 467  Write a complete C++ program that asks a user to enter the prices of 100 different grocery items (each price as a decimal showing dollars and cents). The program calculates and prints the total cost of the items. Answer:

#include <iostream>
using namespace std;

int main() {
  double prices[100];
  cout << "Enter 100 item costs: " << endl;
  for (int i = 0; i < 5; i++) {
    cin >> prices[i];
Problem 468
Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter a positive integer value, x.
2. The program reads a value entered by the user. If the value is not positive, the program repeatedly makes the user type in another value until a positive value of x has been entered. (Note positive means greater than 0.)
3. The program prints out x squares on top of each other, the first with size 1, the second with size 2, and so on.
For example, if the user enters 3 for x the program should print:

* 
** 
*** 

Answer:

```cpp
#include <iostream>
using namespace std;

void square(int s) {
    for (int row = 1; row <= s; row++) {
        for (int col = 1; col <= s; col++)
            cout << "*";
        cout << endl;
    }
    cout << endl;
}

int main() {
    int x;
    cout << "What is x? ";
    cin >> x;

    while (x <= 0) {
        cout << "Please give a positive value for x: ";
        cin >> x;
    }

    for (int i = 1; i <= x; i++) square(i);
}
```

Problem 469   Write a function called percent that uses two parameters x and y and returns the ratio $x/y$ as a percentage.
For example, a program that uses the function percent follows.
int main() {
    double z;
    z = percent(1.5, 3.0);
    cout << z << endl;
}

It should print:

50.0

because 1.5/3 = 1/2 = 50%.

Answer:

double percent(double a, double b) {
    return 100 * a / b;
}
Problem 470  Write a C++ function called range that returns the difference between the largest and smallest elements in an array.

It should be possible to use your function in the following program. (The output from this program is 10 because the difference between the largest element 13 and the smallest element 3 is 13 – 3 = 10).

```cpp
main() {
    int data[6] = {11, 12, 11, 3, 12, 13};
    int x;
    x = range(data, 6);
    // data is the array to search, 6 is the number of elements of the array
    cout << "The range is: " << x << endl;
}

Answer:

```cpp
int range(int d[], int c) {
    int min = d[0];
    int max = d[0];
    for (int i = 1; i < c; i++) {
        if (d[i] < min) min = d[i];
        if (d[i] > max) max = d[i];
    }
    return max - min;
}
```

Problem 471  Consider the following C++ program.

```cpp
#include <iostream>
using namespace std;

void mystery(int data[], int p, int q) {
    data[p] = data[q];
    data[q] = 0;
}

void print(int data[], int p) {
    for (int i = 0; i < p; i++)
        cout << data[i] << " ";
    cout << endl;
}

main() {
    int scores[8] = {3, 1, 4, 1, 5, 9, 2, 6};
    int quiz[7] = {0, 1, 2, 3, 4, 5, 6};
    print(quiz, 4);
    print(scores, 4);
    mystery(scores, 3, 4);
    print(scores, 8);
    for (int i = 0; i < 3; i++)
        mystery(quiz, i, i+ 1);
    print(quiz, 7);
}
```

What is the output from the program?

Answer:

```
0 1 2 3
3 1 4 1
3 1 4 5 0 9 2 6
1 2 3 0 4 5 6
```
**Problem 472** Write C++ functions called `elementSwap` and `swap` that swap either the values of two elements of an array or the values of two variables. It should be possible to use your function in the following program. (The output from this program is: 4 3 because the values of $x$ and $y$ are exchanged.)

```cpp
main() {
    int a[6] = {11, 12, 11, 3, 12, 13};
    int x = 3, y = 4;
    elementSwap(a, 0, 5);
    swap(x, y);
    cout << x << " " << y << endl;
}

Answer:

```cpp
def elementSwap(int a[], int x, int y):
    int temp = a[x];
    a[x] = a[y];
    a[y] = temp;

def swap(x, y):
    int temp = x;
    x = y;
    y = temp;
```

**Problem 473** Write a complete C++ program that asks a user to enter the 10 quiz scores for each student in a class of 30 students. For each of the 10 quizzes, the program decides which student(s) have got the highest scores and prints their numbers. (Hint: Store quiz data in a table.)

Sample output might look like:

```
Top Scores:
Quiz 0: Students: 5 17 23
Quiz 1: Students: 2 11 17 26
Quiz 2: Students: 2 17 23 26 27
```

and so on....

**Answer:**

```cpp
#include <iostream>
using namespace std;

void topScores(int quiz[][10], int n, int q) {
    int max = quiz[0][q];
    int s;
    for (s = 1; s < n; s++)
        if (quiz[s][q] > max) max = quiz[s][q];
    cout << "Quiz " << q << " Students: ";
    for (s = 0; s < n; s++)
        if (quiz[s][q] == max) cout << s << " ";
    cout << endl;
}

int main() {
```
int quiz[30][10];
int s, q;

for (s = 0; s < 30; s++) {
    cout << "Enter 10 quiz scores for student " << s << " : ";
    for (q = 0; q < 10; q++)
        cin >> quiz[s][q];
}

for (q = 0; q < 10; q++) topScores(quiz, 30, q);
return 0;
}

Problem 474   Consider the following C++ program. What is the output?

Problem 475   Write a complete C++ program that does the following:
1. It generates two random numbers $x$ and $y$ each between 1 and 100. (You should use the functions `rand` and `srand`.)
2. It adds $x$ and $y$ to make a secret code.
3. It prints the secret code.
For example, if the program generated the numbers $x = 11$ and $y = 13$ which add to 24, the output would be:

The secret code is 24.

Answer:
int main() {
    srand(time(NULL));
    int x, y;
    x = rand() % 100 + 1;
    y = rand() % 100 + 1;
    int code = x + y;
    cout << " The secret code is " << code << endl;
    return 0;
}

Problem 476   Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)
1. It asks the user to enter a positive integer value, x.
2. The program reads the value entered by the user.
3. If the value is not positive, the program terminates. Otherwise, the program prints a checkerboard pattern that forms a square of side x.
For example, if the user enters 5 for x the program should print the following diagram with 5 lines.

* * *
* *
* * *
* *
* * *

(Hint: How is an even numbered row printed? How about an odd numbered row?)
Answer:

#include <iostream>
using namespace std;

int main() {
    int x;
    cout << "Enter a positive integer value, x:";  
    cin >> x;
    if (x <= 0) exit(1);

    for (int r = 1; r <= x; r++) {
        for (int c = 1; c <= x; c++) {
            if ((r + c) % 2 == 0) cout << "*";  
            else cout << " ";
        }
        cout << endl;
    }

    return 0;
}

Problem 477   Write a C++ function called negSum that returns the sum of all negative elements in an array of integers.
It should be possible to use your function in the following program. (The output from this program is −12 because the negative elements −5, −4, and −3 have a sum of −12 = −5 + (−4) + (−3).)

main() {
    int data[6] = {-5, -4, 1, 3, 2, -3};
    int x;
x = negSum (data, 6);
    // data is the array to search, 6 is the number of elements of the array
    cout << "The negative sum is: " << x << endl;
}

Answer:

int negSum(int array[], int cap) {
    int answer = 0;
    for (int i = 0; i < cap; i++)
        if (array[i] < 0) answer += array[i];
    return answer;
}

Problem 478  Write header lines (prototypes) for the following functions. Do not supply the blocks for the functions.
(a) A function called isOdd that is used to decide whether an integer is odd.
Answer:

bool isOdd(int x)

(b) A function called max which determines the largest of 3 double precision values.
Answer:

double max(double x, double y, double z)

(c) A function called swap which is used to swap two integer values.
Answer:

void swap(int &x, int &y)

(d) A function called total which is to find the sum of all entries in an array of integers.
Answer:

int total(int array[], int cap)

(e) A function called maxIndex which is to find the index of the largest element in an array of double precision values.
Answer:

int maxIndex(double array[], int cap)

(f) A function called sort which is to sort an array of integers into order.
Answer:

void sort(int array[], int cap)

Problem 479  Write a complete C++ program that:
1. Asks a user to enter the number of students in a class and the number of quizzes taken by the class.
2. If either of these numbers is less than 1 or more than 99 the program should exit.
3. The program should then prompt the user to enter all of the scores for each of the quizzes, starting with all scores for Quiz 1, followed by all scores for Quiz 2 and so on.
4. The program should print the number of the student with the highest total.
Number students and quizzes starting at 1.
A sample run of the program might look like:
How many students: 3
How many quizzes: 4

Enter scores for Quiz 1: 10 7 0
Enter scores for Quiz 2: 10 10 0
Enter scores for Quiz 3: 10 6 0
Enter scores for Quiz 4: 10 9 0

Student 1 got the highest total.

Answer:

#include <iostream>
using namespace std;

int main() {
    int score[100][100];
    int r, c;
    int totals[100];
    int numStudents, numScores;

    cout << "Enter the number of students and the number of quizzes: ";
    cin >> numStudents >> numScores;
    if (numStudents <= 0 || numStudents >= 100
        || numScores <= 0 || numScores >= 100) exit(1);

    for (r = 1; r <= numScores; r++) {
        cout << "Enter the scores for Quiz " << r << ": ";
        for (c = 1; c <= numStudents; c++) cin >> score[r][c];
    }

    for (c = 1; c <= numStudents; c++) totals[c] = 0;
    for (r = 1; r <= numScores; r++) {
        for (c = 1; c <= numStudents; c++)
            totals[c] += score[r][c];
    }

    int topStudent = 1;
    for (c = 1; c <= numStudents; c++)
        if (totals[c] > totals[topStudent])
            topStudent = c;
    cout << "Student " << topStudent << " got the highest total."
        << endl; return 0;
}