## CS320: Problems for Day 8, Winter 2023

Problem 1 Let $M$ be the finite automaton represented by the state diagram on Figure 1, and let $L$ be the language accepted by $M$.
Write a complete formal definition or a state-transition graph of a deterministic finite automaton $M^{\prime}$ that accepts $L$ and show your work. If such automaton does not exist, prove it.


Figure 1:

Problem 2 Let $M$ be the finite automaton represented by the state diagram on Figure 2, and let $L$ be the language accepted by $M$.


Figure 2:
(a) Is the finite automaton $M$ deterministic? Justify briefly your answer.
(b) If $M$ is not deterministic, construct a deterministic finite automaton $M^{\prime}$ that accepts $L$ and show your work. If such an automaton $M^{\prime}$ does not exist, explain why.

Problem 3 Let $L$ be the language defined by the regular expression

$$
b\left(a \cup b^{*}\left(\left(c^{*} \cup(c b)^{*}\right) a c\right)^{*}\right) b
$$

(a) Construct a finite automaton $M$ that accepts $L$. If such an automaton $M$ does not exist, explain why.
(b) If you constructed an automaton $M$ in your answer to part (a), is $M$ deterministic? Justify briefly your answer.

Problem 4 Let $M$ be the finite automaton represented by the state diagram on Figure 3 , and let $L$ be the language accepted by $M$.


Figure 3:
Construct a state-transition graph of a deterministic finite automaton $M_{1}$ that accepts $L$, and show your work. If such automaton does not exist, prove it.

Problem 5 Let $L$ be the language accepted by the finite automaton $M=(Q, \Sigma, \delta, q,\{f\})$, where $\Sigma=\{a\}$, $Q=\{p, q, r, s, t, v, w, x, y, z, f\}$,
and $\delta$ is given by the following table:

|  | $a$ | $\lambda$ |
| :---: | :---: | :---: |
| $p$ | $\{z\}$ | $\varnothing$ |
| $q$ | $\{t, r\}$ | $\{s\}$ |
| $r$ | $\varnothing$ | $\{q, t\}$ |
| $s$ | $\varnothing$ | $\{w\}$ |
| $t$ | $\{z, y\}$ | $\{p, w\}$ |
| $v$ | $\{x\}$ | $\{r\}$ |
| $w$ | $\{y\}$ | $\varnothing$ |
| $x$ | $\{p\}$ | $\{v\}$ |
| $y$ | $\{p\}$ | $\{f\}$ |
| $z$ | $\varnothing$ | $\{v\}$ |
| $f$ | $\varnothing$ | $\varnothing$ |

Compute the $\lambda$-closure of state $v$.

Problem 6 Let $M$ be the finite automaton represented by the state diagram on Figure 4, and let $L$ be the language accepted by $M$.


Figure 4:
Write a complete formal definition of a context-free grammar $G$ that generates $L$. If such grammar does not exist, prove it.

