

Solutions

08.30am – 10.30am, Monday, May 23, 2016

Problem 1 Write the best **title lines** for the functions that are called by the following main program. **Do not supply blocks for the functions.**

```
int main() {
    double x = 0.0, y = 3.1, z = 2.5;
    int array[5] = {3,1,4,1,5};
    string s;

    cout << middle(x, y, z) << endl;           // (a) prints middle value 2.5
    increase(x); cout << x << endl;           // (b) prints 1.0
    printBoth(y, z);                          // (c) prints 3.1 2.5
    s = allOf(array, 5); cout << s << endl;    // (d) prints 3 1 4 1 5
    increase(array, 5); cout << allOf(array,5) << endl; // (e) prints 4 2 5 2 6
    return 0;
}
```

(a) Title line for **middle**.

Answer:

```
double middle(double a, double b, double c)
```

(b) Title line for **increase**.

Answer:

```
void increase(double &x)
```

(c) Title line for **printBoth**.

Answer:

```
void printBoth(double a, double b)
```

(d) Title line for **allOf**.

Answer:

```
string allOf(int a[], int cap)
```

(e) Title line for **increase**.

Answer:

```
void increase(int x[], int cap)
```

Problem 2 Consider the following C++ program.

```
#include <iostream>
using namespace std;

string fun(string x) {
    if (x.length() <= 4) {
        return "00";
    }
    return fun(x.substr(4)) + x.substr(4);
}

int main() {
    int x = 43;
    int y = x / 10;
    cout << x / 10 + x % 10 << endl;           // line (a)
    if (((x > 40) || (x < 50)) && ((y > 4) || (y < 5)))
        cout << x % y << endl;               // line (b)
    cout << fun("Easy") << endl;             // line (c)
    cout << fun("12345") << endl;           // line (d)
    cout << fun("123456789") << endl;       // line (e)
}
```

(a) What is the output at line (a)?

Answer:

7

(b) What is the output at line (b)?

Answer:

3

(c) What is the output at line (c)?

Answer:

00

(d) What is the output at line (d)?

Answer:

005

(e) What is the output at line (e)?

Answer:

00956789

Problem 3 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```
int main() {
    int a[4] = {1, 2, -3, -4};
    int x = 5, y = 6;
    // (a) Return the cube. Here 8 is printed.
    cout << cube(2) << endl;
    // (b) Return the larger number. Here 6 is printed.
    cout << larger(x, y) << endl;
    // (c) Return the largest element. Here 2 is printed.
    cout << largest(a, 4) << endl;
    // (d) Test whether all array entries are positive. Here: Not all positive
    if (!allPositive(a, 4)) cout << "Not all positive\n";
    // (e) Swap values. Here -3 is printed.
    swap(a[2], x);
    cout << x << endl;
    return 0;
}
```

Answer:

(a)

```
int cube(int x) {
    return x * x * x;
}
```

(b)

```
int larger(int x, int y) {
    if (x > y) return x;
    return y;
}
```

(c)

```
int largest(int x[], int cap) {
    int ans = x[0];
    for (int i = 0; i < cap; i++)
        if (x[i] > ans) ans = x[i];
    return ans;
}
```

(d)

```
bool allPositive(int x[], int capacity) {
    for (int i = 0; i < capacity; i++)
        if (x[i] <= 0) return false;
    return true;
}
```

(e)

```
void swap(int &x, int &y) {
    int temp = x;
    x = y;
    y = temp;
}
```

Problem 4 Write a function called *evenCols* that returns the number of columns of a 2-dimensional array that have an even sum. The array contains integers and has 5 columns.

For example, a program that uses the function *evenCols* follows. The output is 2 because only columns 1 and 4 have even sum.

```
int main() {
    int x[2][5] = {{1, 2, 3, 5, 4}, {2, 2, 2, 2, 2}};
    cout << evenCols(x, 2, 5) << endl;    // prints 2
    return 0;
}
```

Answer:

```
int evenCols(int array[][5], int rows, int cols) {
    int ans = 0;
    for (int c = 0; c < cols; c++) {
        int total = 0;
        for (int r = 0; r < rows; r++)
            total += array[r][c];
        if (total % 2 == 0) ans++;
    }
    return ans;
}
```

Problem 5 Write a function called *not7s* that counts how many digits are not equal to 7 in a positive integer parameter.

For example, a program that uses the function *not7s* follows.

```
int main() {
    cout << not7s(747) << endl;           // prints 1
    cout << not7s(176) << endl;           // prints 2
    cout << not7s(12345) << endl;         // prints 5
    cout << not7s(77777) << endl;         // prints 0
    return 0;
}
```

Answer:

```
int not7s(int x) {
    if (x == 0) return 0;
    if (x % 10 == 7) return not7s(x/10);
    return not7s(x/10) + 1;
}
```

Problem 6 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer n that is between 1 and 23.
2. It repeatedly reads n from the user until the supplied value of n is legal.
3. It prints out a rectangular picture with $2n - 1$ rows and n columns that makes a large 5 as displayed by a digital clock.

Here is an example of how the program should work:

```
Give me an integer between 1 and 23: 4
****
*
*
****
 *
 *
****
```

Answer:

```
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 23: ";
    cin >> n;
    while (n < 1 || n > 23) {
        cout << "Give me an integer between 1 and 23: ";
        cin >> n;
    }

    for (int r = 1; r < 2*n; r++) {
        for (int c = 1; c <= n; c++)
            if (r == 1 || r == 2*n - 1 || r == n) cout << "*";
            else if (r < n && c == 1) cout << "*";
            else if (r > n && c == n) cout << "*";
            else cout << " ";
        cout << endl;
    }

    return 0;
}
```

Solutions

08.30am – 10.30am, Monday, May 23, 2016

Problem 1 Write the best **title lines** for the functions that are called by the following main program. **Do not supply blocks for the functions.**

```
int main() {
    int x = 0, y = 3, z = 2;
    char array[5] = {'a','b','c','d','e'};
    string s;

    cout << biggest(x, y, z) << endl;           // (a) prints biggest: 3
    x = increase(x); cout << x << endl;         // (b) prints 1
    s = printBoth(y, z); cout << s << endl;    // (c) prints 3 2
    allOf(array, 5);                            // (d) prints a b c d e
    upper(array, 5); allOf(array,5);           // (e) prints A B C D E
    return 0;
}
```

(a) Title line for **biggest**.

Answer:

```
int biggest(int a, int b, int c)
```

(b) Title line for **increase**.

Answer:

```
int increase(int x)
```

(c) Title line for **printBoth**.

Answer:

```
string printBoth(int a, int b)
```

(d) Title line for **allOf**.

Answer:

```
void allOf(char a[], int cap)
```

(e) Title line for **upper**.

Answer:

```
void upper(char x[], int cap)
```

Problem 2 Consider the following C++ program.

```
#include <iostream>
using namespace std;

string fun(string x) {
    if (x.length() <= 4) {
        return "XX";
    }
    return fun(x.substr(3)) + x.substr(4);
}

int main() {
    int x = 34;
    int y = x / 10;
    cout << x / 10 + x % 10 << endl;           // line (a)
    if (((x > 30) && (x < 50)) || ((y > 3) && (y < 5)))
        cout << x % y << endl;               // line (b)
    cout << fun("Easy") << endl;             // line (c)
    cout << fun("ABCDE") << endl;           // line (d)
    cout << fun("ABCDEFG") << endl;         // line (e)
}
```

(a) What is the output at line (a)?

Answer:

7

(b) What is the output at line (b)?

Answer:

1

(c) What is the output at line (c)?

Answer:

XX

(d) What is the output at line (d)?

Answer:

XXE

(e) What is the output at line (e)?

Answer:

XXEFG

Problem 3 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```
int main() {
    int a[4] = {1, 2, -3, -4};
    int x = 5, y = 6;
    // (a) Return the cube. Here 8.0 is printed.
    cout << cube(2.0) << endl;
    // (b) Print the larger number. Here 6 is printed.
    larger(x, y);
    // (c) Return the first negative element, or 0 if there is none. Here -3 is printed.
    cout << firstNegative(a, 4) << endl;
    // (d) Test whether array entries increase in size. Here: Not increasing
    if (!increasing(a, 4)) cout << "Not increasing\n";
    // (e) Swap values. Here 6 is printed.
    swap(y, x);
    cout << x << endl;
    return 0;
}
```

Answer:

(a)

```
double cube(double x) {
    return x * x * x;
}
```

(b)

```
void larger(int x, int y) {
    if (x > y) cout << x << endl;
    else cout << y << endl;
}
```

(c)

```
int firstNegative(int x[], int cap) {
    for (int i = 0; i < cap; i++)
        if (x[i] < 0) return x[i];
    return 0;
}
```

(d)

```
bool increasing(int x[], int capacity) {
    for (int i = 1; i < capacity; i++)
        if (x[i - 1] >= x[i]) return false;
    return true;
}
```

(e)

```
void swap(int &x, int &y) {
    int temp = x;
    x = y;
    y = temp;
}
```

Problem 4 Write a function called *positiveCols* that returns the number of columns of a 2-dimensional array that have a positive sum. The array contains doubles and has 6 columns.

For example, a program that uses the function *positiveCols* follows. The output is 2 because only columns 1 and 3 have positive sum.

```
int main() {
    double x[2][6] = {{1.0, 6.0, 3.0, 5.0, 4.0, 2.0},
                     {-4.0, -4.0, -4.0, -4.0, -4.0, -4.0}};
    cout << positiveCols(x, 2, 6) << endl;    // prints 2
    return 0;
}
```

Answer:

```
int positiveCols(double array[][6], int rows, int cols) {
    int ans = 0;
    for (int c = 0; c < cols; c++) {
        double total = 0;
        for (int r = 0; r < rows; r++)
            total += array[r][c];
        if (total > 0) ans++;
    }
    return ans;
}
```

Problem 5 Write a function called *sixesAndSevens* that counts how many digits are equal to 6 or 7 in a positive integer parameter.

For example, a program that uses the function *sixesAndSevens* follows.

```
int main() {
    cout << sixesAndSevens(747) << endl;      // prints 2
    cout << sixesAndSevens(176) << endl;      // prints 2
    cout << sixesAndSevens(666) << endl;      // prints 3
    cout << sixesAndSevens(12345) << endl;    // prints 0
    return 0;
}
```

Answer:

```
int sixesAndSevens(int x) {
    if (x == 0) return 0;
    if (x % 10 == 7 || x % 10 == 6) return sixesAndSevens(x/10) + 1;
    return sixesAndSevens(x/10);
}
```

Problem 6 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer n that is between 1 and 17.
2. It repeatedly reads n from the user until the supplied value of n is legal.
3. It prints out a rectangular picture with $2n - 1$ rows and n columns that makes a large 2 as displayed by a digital clock.

Here is an example of how the program should work:

```
Give me an integer between 1 and 17: 5
*****
 *
 *
 *
*****
*
*
*
*****
```

Answer:

```
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 17: ";
    cin >> n;
    while (n < 1 || n > 17) {
        cout << "Give me an integer between 1 and 17: ";
        cin >> n;
    }

    for (int r = 1; r < 2*n; r++) {
        for (int c = 1; c <= n; c++)
            if (r == 1 || r == 2*n - 1 || r == n) cout << "*";
            else if (r > n && c == 1) cout << "*";
            else if (r < n && c == n) cout << "*";
            else cout << " ";
        cout << endl;
    }

    return 0;
}
```

Solutions

01.45pm – 03.45pm, Monday, May 23, 2016

Problem 1 Write the best **title lines** for the functions that are called by the following main program. **Do not supply blocks for the functions.**

```
int main() {
    int x = 0, y = 3, z = 2;
    string array[5] = {"A","B","C","D","E"};
    string s;

    cout << least(x, y, z) << endl;           // (a) prints least: 0
    x = decrease(y); cout << x << " " << y << endl; // (b) prints 2 2
    s = printBoth(z, z); cout << s << endl; // (c) prints 2 2
    allOf(array, 5);                          // (d) prints A B C D E
    lower(array, 5); allOf(array,5);          // (e) prints a b c d e
    return 0;
}
```

(a) Title line for **least**.

Answer:

```
int least(int a, int b, int c)
```

(b) Title line for **decrease**.

Answer:

```
int decrease(int &x)
```

(c) Title line for **printBoth**.

Answer:

```
string printBoth(int a, int b)
```

(d) Title line for **allOf**.

Answer:

```
void allOf(string a[], int cap)
```

(e) Title line for **lower**.

Answer:

```
void lower(string x[], int cap)
```

Problem 2 Consider the following C++ program.

```
#include <iostream>
using namespace std;

string fun(string x) {
    if (x.length() <= 5) {
        return "00";
    }
    return fun(x.substr(5, 1)) + x.substr(5, 1);
}

int main() {
    int x = 78;
    string y = "Hello";
    cout << x / 10 + x % 10 << endl;           // line (a)
    cout << y.find("l") << endl;             // line (b)
    cout << fun("Easy") << endl;           // line (c)
    cout << fun("234567") << endl;         // line (d)
    cout << fun("23456789") << endl;       // line (e)
}
```

(a) What is the output at line (a)?

Answer:

15

(b) What is the output at line (b)?

Answer:

2

(c) What is the output at line (c)?

Answer:

00

(d) What is the output at line (d)?

Answer:

007

(e) What is the output at line (e)?

Answer:

007

Problem 3 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```
int main() {
    int a[4] = {3, 2, -3, -4};
    double x = 5.0, y = 6.0;
    // (a) Return the cube. Here 8.0 is printed.
    cout << cube(2.0) << endl;
    // (b) Print the larger number. Here 6.0 is printed.
    larger(x, y);
    // (c) Return the last positive element, or 0 if there is none. Here 2 is printed.
    cout << lastPositive(a, 4) << endl;
    // (d) Test whether array entries decrease in size. Here: decreasing
    if (decreasing(a, 4)) cout << "Decreasing\n";
    // (e) Swap values. Here 2 is printed.
    swap(a[0], a[1]);
    cout << a[0] << endl;
    return 0;
}
```

Answer:

(a)

```
double cube(double x) {
    return x * x * x;
}
```

(b)

```
void larger(double x, double y) {
    if (x > y) cout << x << endl;
    else cout << y << endl;
}
```

(c)

```
int lastPositive(int x[], int cap) {
    int ans = 0;
    for (int i = 0; i < cap; i++)
        if (x[i] > 0) ans = x[i];
    return ans;
}
```

(d)

```
bool decreasing(int x[], int capacity) {
    for (int i = 1; i < capacity; i++)
        if (x[i - 1] <= x[i]) return false;
    return true;
}
```

(e)

```
void swap(int &x, int &y) {
    int temp = x;
    x = y;
    y = temp;
}
```

Problem 4 Write a function called *largestCol* that returns the largest sum of the entries in a single column of a 2-dimensional array. The array contains integers and has 5 columns.

For example, a program that uses the function *largestCol* follows. The output is 7 because this is the sum for columns 0 and 4 and the other columns have a smaller sum.

```
int main() {
    int x[2][5] = {{1, 2, 3, 5, 4}, {6, 0, 0, 0, 3}};
    cout << largestCol(x, 2, 5) << endl;    // prints 7
    return 0;
}
```

Answer:

```
int largestCol(int array[][5], int rows, int cols) {
    int ans;
    for (int c = 0; c < cols; c++) {
        int total = 0;
        for (int r = 0; r < rows; r++)
            total += array[r][c];
        if (c == 0 || total > ans) ans = total;
    }
    return ans;
}
```


Problem 5 Write a function called *diff2* that returns the absolute value of the difference of the first two digits in an integer parameter that is at least 10.

For example, a program that uses the function *diff2* follows.

```
int main() {
    cout << diff2(747) << endl;           // prints 3
    cout << diff2(176) << endl;           // prints 6
    cout << diff2(10101) << endl;         // prints 1
    cout << diff2(77777) << endl;         // prints 0
    return 0;
}
```

Answer:

```
int diff2(int x) {
    if (x < 100) {
        int ans = x/10 - x % 10;
        if (ans >= 0) return ans;
        return -ans;
    }
    return diff2(x/10);
}
```

Problem 6 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer n that is between 1 and 23.
2. It repeatedly reads n from the user until the supplied value of n is legal.
3. It prints out a rectangular picture with $2n - 1$ rows and n columns that makes a large 3 as displayed by a digital clock.

Here is an example of how the program should work:

```
Give me an integer between 1 and 23: 5
*****
 *
 *
 *
*****
 *
 *
 *
*****
```

Answer:

```
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 23: ";
    cin >> n;
    while (n < 1 || n > 23) {
        cout << "Give me an integer between 1 and 23: ";
        cin >> n;
    }

    for (int r = 1; r < 2*n; r++) {
        for (int c = 1; c <= n; c++)
            if (r == 1 || r == 2*n - 1 || r == n) cout << "*";
            else if (c == n) cout << "*";
            else cout << " ";
        cout << endl;
    }

    return 0;
}
```

Solutions

01.45pm – 03.45pm, Monday, May 23, 2016

Problem 1 Write the best **title lines** for the functions that are called by the following main program. **Do not supply blocks for the functions.**

```
int main() {  
    double x = 0.0, y = 3.1, z = 2.5;  
    int array[5] = {3,1,4,1,5};  
    string s;  
  
    cout << second(x, x, z) << endl;           // (a) prints second value 0.0  
    increase(x); cout << x << endl;           // (b) prints 1.0  
    printBoth(y, z);                          // (c) prints 3.1 2.5  
    s = allOf(array, 5); cout << s << endl;    // (d) prints 3 1 4 1 5  
    rotate(array, 5); cout << allOf(array,5) << endl; // (e) prints 1 4 1 5 3  
    return 0;  
}
```

(a) Title line for **second**.

Answer:

```
double second(double a, double b, double c)
```

(b) Title line for **increase**.

Answer:

```
void increase(double &x)
```

(c) Title line for **printBoth**.

Answer:

```
void printBoth(double a, double b)
```

(d) Title line for **allOf**.

Answer:

```
string allOf(int a[], int cap)
```

(e) Title line for **rotate**.

Answer:

```
void rotate(int x[], int cap)
```

Problem 2 Consider the following C++ program.

```
#include <iostream>
using namespace std;

string fun(string x) {
    if (x.length() <= 3) {
        return "XX";
    }
    return fun(x.substr(1,2)) + x.substr(1,2);
}

int main() {
    int x = 53;
    string y = "easy";
    cout << x / 10 + x % 10 << endl;           // line (a)
    cout << y.rfind("a") << endl;             // line (b)
    cout << fun(y) << endl;                   // line (c)
    cout << fun("y") << endl;                 // line (d)
    cout << fun("yxwvuts") << endl;          // line (e)
}
```

(a) What is the output at line (a)?

Answer:

8

(b) What is the output at line (b)?

Answer:

1

(c) What is the output at line (c)?

Answer:

XXas

(d) What is the output at line (d)?

Answer:

XX

(e) What is the output at line (e)?

Answer:

XXxw

Problem 3 Write blocks of code to perform the functions used in the following main program. Your blocks must match the given title lines. Each block should be a short function of only a few lines.

```
int main() {
    int a[4] = {3, 2, -3, -4};
    int x = 7, y = 6;
    // (a) Return the cube. Here 8 is printed.
    cout << cube(2) << endl;
    // (b) Is x larger than y?. Here YES is printed.
    if (larger(x, y)) cout << "YES" << endl;
    // (c) Return the smallest element. Here -4 is printed.
    cout << smallest(a, 4) << endl;
    // (d) Test whether all array entries are negative. Here: Not all negative
    if (!allNegative(a, 4)) cout << "Not all negative\n";
    // (e) Swap values. Here -3 is printed.
    swap(a[2], x);
    cout << x << endl;
    return 0;
}
```

Answer:

(a)

```
int cube(int x) {
    return x * x * x;
}
```

(b)

```
bool larger(int x, int y) {
    return x > y;
}
```

(c)

```
int smallest(int x[], int cap) {
    int ans = x[0];
    for (int i = 0; i < cap; i++)
        if (x[i] < ans) ans = x[i];
    return ans;
}
```

(d)

```
bool allNegative(int x[], int capacity) {
    for (int i = 0; i < capacity; i++)
        if (x[i] >= 0) return false;
    return true;
}
```

(e)

```
void swap(int &x, int &y) {
    int temp = x;
    x = y;
    y = temp;
}
```

Problem 4 Write a function called *smallestCol* that returns the smallest sum of the entries in a single column of a 2-dimensional array. The array contains doubles and has 6 columns.

For example, a program that uses the function *smallestCol* follows. The output is 7.0 because this is the sum for columns 0 and 4 and the other columns have a larger sum.

```
int main() {
    double x[2][6] = {{1.0, 9.0, 8.0, 6.0, 4.0, 8.0},
                     {6.0, 0.0, 0.0, 3.0, 3.0, 3.0}};
    cout << smallestCol(x, 2, 6) << endl;    // prints 7.0
    return 0;
}
```

Answer:

```
double smallestCol(double array[][6], int rows, int cols) {
    double ans;
    for (int c = 0; c < cols; c++) {
        double total = 0;
        for (int r = 0; r < rows; r++)
            total += array[r][c];
        if (c == 0 || total < ans) ans = total;
    }
    return ans;
}
```

Problem 5 Write a function called *sum3* that returns the sum of the first three digits in an integer parameter that is at least 100.

For example, a program that uses the function *sum3* follows.

```
int main() {
    cout << sum3(747) << endl;           // prints 18
    cout << sum3(176) << endl;           // prints 14
    cout << sum3(10199) << endl;         // prints 2
    cout << sum3(77777) << endl;         // prints 21
    return 0;
}
```

Answer:

```
int sum3(int x) {
    if (x == 0) return 0;
    if (x < 1000) return sum3(x/10) + x%10;
    return sum3(x/10);
}
```

Problem 6 Write a complete C++ program that does the following. (Programs that correctly carry out some of the tasks will receive partial credit.)

1. It asks the user to enter an integer n that is between 1 and 17.
2. It repeatedly reads n from the user until the supplied value of n is legal.
3. It prints out a rectangular picture with $2n - 1$ rows and n columns that makes a large 4 as displayed by a digital clock.

Here is an example of how the program should work:

```
Give me an integer between 1 and 17: 5
*  *
*  *
*  *
****
*  *
*  *
*  *
```

Answer:

```
#include <iostream>
using namespace std;

int main() {
    int n;
    cout << "Give me an integer between 1 and 17: ";
    cin >> n;
    while (n < 1 || n > 17) {
        cout << "Give me an integer between 1 and 17: ";
        cin >> n;
    }

    for (int r = 1; r < 2*n; r++) {
        for (int c = 1; c <= n; c++)
            if (r == n) cout << "*";
            else if (r < n && c == 1) cout << "*";
            else if (c == n) cout << "*";
            else cout << " ";
        cout << endl;
    }

    return 0;
}
```