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These are some of the solutions to practice problems. Not all problems have solutions here.

Solutions to some older problems might not make use of generics. Generics are now required in this course.

**Problem 1** A generic class *List* is to be programmed as a doubly linked list that begins and ends with a sentinel node. The sentinel is created in the constructor and can never be removed. Assume a standard implementation of a class *DNode* with private instance variables called *data*, *next*, *prev* that are accessed by getter and setter methods only.

The skeleton of code for the class *List* follows:

```
public class List<T> {
    private DNode<T> sentinel;
    private int size;
    public List()
        // initializes the list: to be coded as (a)
    public void insertFirst(T x)
        // adds x at the front of the list, leaving other elements in place: coded as (b)
    public T removeLast() throws Exception
        // removes the last element from the list, returning its data: to be coded as (c)
}
```

(a) Implement the constructor.

Answer:

```
public List() {
    size = 0;
    sentinel = new DNode<T>();
    sentinel.setNext(sentinel);
    sentinel.setPrev(sentinel);
}
```

(b) Implement `insertFirst`.

Answer:

```
public void insertFirst(T x) {
    DNode<T> newNode = new DNode<T>(x, sentinel, sentinel.getNext());
    sentinel.getNext().setPrev(newNode);
    sentinel.setNext(newNode);
    size++;
}
```

(c) Implement `removeLast`.

Answer:

```
public T removeLast() throws Exception {
    if (size == 0) throw new Exception("List Empty");
    size--;
    DNode<T> last = sentinel.getPrev();
    DNode<T> newLast = last.getPrev();
    newLast.setNext(sentinel);
    sentinel.setPrev(newLast);
    return last.getData();
}
```

**Problem 2** Suppose that a doubly linked list is implemented as a class *DoublyLinkedList* that uses sentinel doubly linked nodes *header* and *trailer* and no other instance variables. Write a method of the class called *removeMiddle*

that removes either the middle node from a list of odd length, or the middle two nodes from a list of even length. The method should throw an exception if the required nodes do not exist. Give a  $O$ -estimate for the run time of your method in terms of the number  $n$  of elements in the list.

**Answer:**

```
public void removeMiddle() {
    if (header.getNext() == trailer)
        throw new RuntimeException("Empty");
    removeRecursive(header, trailer);
}

private void removeRecursive(DNode h, DNode t) {
    if (h == t || h.getNext() == t) {
        DNode downOne = h.getPrev();
        DNode upOne = t.getNext();
        downOne.setNext(upOne);
        upOne.setPrev(downOne);
    }
    else removeRecursive(h.getNext(), t.getPrev());
}
```

The run time of this method is  $O(n)$ .

**Problem 3** Consider the following partial implementation of a circular list of singly linked nodes.

```
public class CircularList {
    private Node cursor;
    public CircularList() { cursor = null; }
    public boolean isEmpty() {return cursor == null;}
    public void advance() { cursor = cursor.getNext(); }
    public void addAfter(Object d) { CODE OMITTED TO SAVE SPACE }
    public void addBefore(Object d) {
        addAfter(d);
        swapData(cursor, cursor.getNext());
        cursor = cursor.getNext();
    }
    private void swapData(Node n, Node m) { // helper method for addBefore and remove
        Object temp = n.getData();
        n.setData(m.getData()); m.setData(temp); }
    public Object remove() { CODE OMITTED HERE }
    public String toString() { CODE OMITTED HERE }
}
```

Supply an implementation for the missing method *toString*. The output from your method should match the following format (which indicates a circular list with size 3, stored data A, B, C and the cursor at item A):

A -> B -> C ->

**Answer:**

```
public String toString() {
    if (cursor == null) return "";
    String ans = cursor.getData() + " ->";
    Node n = cursor.getNext();
    while (n != cursor) {
        ans += n.getData();
        ans += " ->";
    }
}
```

```

        n = n.getNext();
    }
    return ans;
}

```

(Extra credit) Write an implementation of the method *remove*. (Hint: Use the *swapData()* method, and apply the trick used in *addBefore()*.)

**Answer:**

```

public Object remove() {
    if (cursor == null) throw new RuntimeException("Empty");
    Object answer = cursor.getData();
    if (cursor.getNext() == cursor) {
        cursor = null;
        return answer;
    }
    swapData(cursor, cursor.getNext());
    cursor.setNext(cursor.getNext().getNext());
    return answer;
}

```

**Problem 4** Suppose that a doubly linked list is made of *DNodes* implemented with the following instance variables and constructor:

```

public class DNode<T> {
    private T data;
    private DNode<T> prev, next;
    public DNode(T d, DNode<T> p, DNode<T> n) { data = d; next = n; prev = p; }
    // standard getter and setter methods for all instance variables omitted
}

```

A doubly linked list class is implemented to use sentinels called *header* and *trailer* using the following instance variables and constructor:

```

public class DList<T> {
    private DNode<T> header, trailer;
    private int size;
    public DList() {
        size = 0;
        header = new DNode<T>(null, null, null);
        trailer = new DNode<T>(null, header, null);
        header.setNext(trailer);
    }
}

```

Write a method with the following title line

```

public T removeBefore(DNode<T> n) throws Exception

```

It should modify the list by removing the node immediately before the *DNode n*. It should return the data that was contained in the removed node. The method should not make any loop through the nodes of the list. You should throw an appropriate exception in case the removal is not allowed or is impossible.

**Answer:**

```

public T removeBefore(DNode<T> n) throws Exception {
    if (n == null || n == header || n.getPrev() == header)

```

```
        throw new Exception("Illegal operation");
    DNode<T> m = n.getPrev();
    DNode<T> l = m.getPrev();
    n.setPrev(l);
    l.setNext(n);
    size--;
    return m.getData();
}
```