# Class 15 

Recursion

## Re-cap:

## Call by value

- When passing values to a function, $\mathrm{C}++$ creates a copy of the values stored in the variable
- The function operates on those copies of values


## Call by reference

-When you want to pass the actual variable to the function, you mark this in the title line by putting an \& between the type and name of the parameter

## Void Function

```
string fullName1 (string first, string last){
    string result = first + " " + last;
    return result;
}
int main(){
    string firstName = "Bob";
    string lastName = "Gallagher";
    // next line prints Bob Gallagher
    cout << fullName1(firstName, lastName);
    // next line stores result of function call in variable
    string fullName = fullName1(firstName, lastName);
    return 0;
}
```


## Void Function

int positiveCube(int a)\{
if(a<0) return a * a * a * -1;
else return a* a * a;
\}

```
int main(){
    int a, b;
    cout << "Enter two numbers: ";
    cin >> a >> b;
    // update each to store the positive cube
    a = positiveCube(a);
    b = positiveCube(b);
    cout << a << " " << b << endl;
    return 0;
}
```

void positiveCubes(int \&a, int \&b)\{
$\operatorname{if}(a<0) a=a * a * a *-1 ;$
else $a=a * a * a ;$
$\operatorname{if}(b<0) b=b * b * b *-1$;
else $b=b *{ }^{*} b$;
\}

```
int main(){
    int a, b;
    cout << "Enter two numbers: ";
    cin >> a >> b;
    // update each to store the positive cube
    positiveCubes(a, b);
    cout << a << " " << b << endl;
    return 0;
}
```


## Recursion

- Use a dictionary to look up an unknown word
- What if the definition in the dictionary contains a word we don't know?
- We use the same dictionary to look up this new word
- Continue looking up unknown words until we have learned the meaning of all the unknown words


## Recursion

- In a similar manner, we might have a function that solves a problem by using itself to solve a smaller version of a problem
- Recursion means "when a thing is defined in terms of itself"
- In programming, recursion happens when a function calls itself within its own definition
- Paradox? How can we tell C++ to perform a task by asking it to use that task?
--> the key is to ask it to use a simpler version of the task.


## Example 1

- Factorial function


## Constructing a recursive function

Recursive functions have two parts:

1. A base case, in which the function can return the result immediately
2. A recursive case, in which the function must call itself to break the current problem down to a simpler level

## Example 2

- Given integer $n$, write function to return left-most digit


## Recursion

- Recursion is a programming technique
- Pro: Sometimes it is easier to write a recursive solution than an iterative solution
- Con: Sometimes the recursive solution requires too much memory to be workable


## Benefits of Recursion

- While it takes a bit of practice to easily recognize how to decompose problems into recursive formulations, it can be one of the quickest ways to design an algorithm
- A recursive version of a function can sometimes be much simpler than an iterative version


## Example 3

- write_vertical
- Writes digits of a number vertically on a screen


## Example 4

- number of digits in an integer


## Summery on constructing a recursive function

- A recursive function contains a call to the function being defined
- The recursive call must accomplish a smaller version of the task ("Progress Condition")
- The function must have one or more cases in which the task is accomplished without using a recursive call ("Base Cases" or "Stopping Conditions")

